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PRF SAMPLING STRATEGIES FOR SWARMSAR SYSTEMS

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ABSTRACT

The work investigates staggered and random PRF (Pulse Repetition Frequency) strategies for a close formation of small Synthetic Aperture Radar (SAR) satellites operating in a multistatic configuration. The satellites are positioned within a fraction of the along-track critical baseline, hence allowing for the application of Displaced Phase Center image formation approaches. The performance of regular and random pulse sampling schemes is in particular assessed for a single-input multiple-output (SIMO) S-Band constellation, whose feasibility is further analyzed in relation to the number of satellites and their antenna size.

Index Terms— SAR system design, Multi-static geometry, pulse repetition frequency, staggered PRF, S-Band.

1. INTRODUCTION

The concept of Displaced Phase Center (DPC) antenna processing is not novel to the spaceborne radar community. Such spatio-temporal processing solution can either be used to identify ground moving targets (GMTI) or to augment the spatial resolution and the swath width of the system. The technique leverages on the use of multiple antennas, that can either be provided by independent subapertures of the same physical antenna or by multiple platforms, such as in the satellite configuration herewith debated. In the GMTI application scenario, the choice of the pulse repetition frequency is not stringent, as the multiple channels can be coregistered by means of post-processing/interpolation. Conversely, in the case of its application for high-resolution enhancements, a perfect pulse interleave scenario shall be sought. In the simple case of $N = 2$ antennas, a half pulse repetition interval (PRI) offset should be ideally accounted between the antenna phase centers to attain a uniformly sampled signal with double PRF, as well as the most optimal ambiguity rejection conditions. For instance, in the case of a canonical system with a single physical antenna splitted in 2 subapertures, the PRI (or more precisely, its spatial equivalent) shall be set to one half of the antenna length. Such DPC condition is however more challenging to achieve with antennas hosted by different satellites, mainly because of the uncertainty on the along-track baselines. A multi-satellite formation demands therefore to handle irregularly sampled pulses, that

must undergo an additional signal reconstruction phase.

Non-uniform sampling in spaceborne SAR has been mainly debated for the two following staggered PRF scenarios: (a) multi-channel configurations, with channels characterized by the same constant PRF and with arbitrary phase center positions, not necessarily perfectly interleaved; (b) single-channel [1] and multi-channel [2] systems where the PRI is continuously varied, although with periodic patterns. The first scenario demands to merge N uniform grids with irregular offsets, and has been already covered by a few notable contributors [3][4]. A reconstruction strategy based on signal inversion in the frequency domain has been for instance suggested in [3]. An undesirable system singularity occurs when one or more offsets are equal to multiples of the PRI and hence no resolution enhancement can be obtained. The second staggered configuration is the one embraced by next generation DBF-capable systems [5][6] because of its capability of drifting the blind ranges along the aperture and hence to illuminate large swaths with a single pulse. In the context of this paper, however, the PRF continuous variation is itself the feature of interest because of its intrinsic performance invariance (in a statistical sense) to the phase center displacements. As illustrated in Fig. 1, the work here presented is indeed aimed at constellations of N satellites flying in close formation and operating in a MISO (Multiple Rx - Single Tx) configuration, where 1 monostatic and $N - 1$ bistatic stripmap images are produced. The study overlooks for the moment the synchronization and cross-track baseline challenges to focus on the azimuth sampling aspects. Two PRF strategies are in particular introduced and analyzed: a constant PRF strategy (associable to scenario (a)) where the performance is assessed as a function of the uncertainty on the along-track baselines; a continuously varying PRI strategy with completely randomic pattern.

2. METHODOLOGY

Let consider a swarm of N satellites flying on the same orbit with velocity a v_s and along-track baselines $b_{ij} = |x_j - x_i| \ll B_c^{AT}$. The distance between the two azimuth positions x_i and x_j is hence much shorter than the critical baseline B_c^{AT} , this latter depending on the antenna size L_a , assumed identical for all satellites. On a hypothetic MIMO scenario, the signal received by the ij channel can be re-

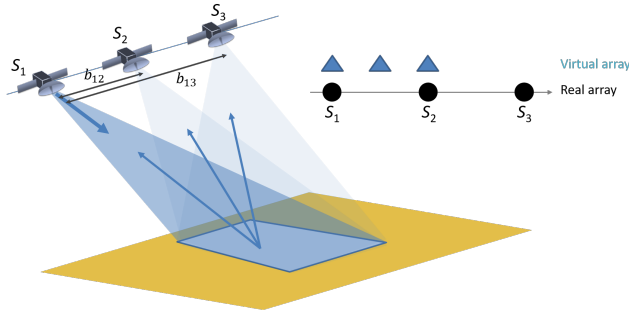


Fig. 1. Representation of the MISO swarmSAR configuration for $N = 3$ satellites. The phase center location (virtual array) of the 3 channels is schematically reported on the right.

lated with a good approximation to the signal received by a different channel pq through

$$u_{ij}(t) \cong u_{kl} \left(t - \frac{\Delta b}{2v_s} \right) \exp \left(-j\pi \frac{\Delta b^2}{\lambda \rho_{kl}(t)} \right) \quad (1)$$

where $\Delta b = (x_p + x_q) - (x_i + x_j)$ is the equivalent monostatic baseline between the two acquisitions and the last term accounts for the difference physical baselines and hence the different two-way distances ρ from the target (valid only for small baselines). In the case of the MISO configuration of Fig. 1, where only the first satellite is transmitting, and further compensating the signals for the baseline differences, equation (1) can be re-written as

$$u_i(t) \cong u_1 \left(t - \frac{b_i}{2v_s} \right) \quad (2)$$

where $u_i = u_{i1}$, $b_i \equiv b_{i1}$ and y_1 is the monostatic signal. The active satellite transmits pulses at azimuth times

$$t_n = \sum_{k=1}^n \text{PRI}(k) + t_0, \quad n \geq 1 \quad (3)$$

where the initial time t_0 is the first pulse of the considered synthetic aperture. A few configurations of the function $\text{PRI}(k)$ are now investigated.

2.1. Constant PRF

In such configuration the pulse interval is a constant value $\text{PRI}(k) \equiv 1/\text{PRF}$. The frequency domain representation of (2) takes the form

$$U_i(f) = U_1(f) \exp \left(-j\pi f \frac{b_i}{v_s} \right) \quad (4)$$

with $u(t) \xrightarrow{\mathcal{F}} U(f)$. Since the signal is not continuous but it shall be instead addressed as discrete with PRI sampling interval, the observed spectrums become

$$Y(f) = \sum_{k=-\infty}^{+\infty} U(f - k \cdot \text{PRF}) \quad (5)$$

where each folding k represents a ghost of the scene, shifted in the image by an azimuth offset [7]

$$\tau = \frac{\text{PRF}}{f_R} k \quad \text{with} \quad f_R = \frac{2v_s^2}{\lambda r_0} \quad (6)$$

function of the Doppler rate f_R and hence on the target zero-Doppler distance r_0 . In the case $N = 2$, by deriving the reconstructed signal expression through matched filter approach, i.e. unraveling the terms in $S(f) = Y_1(f)Y_1^*(f) + Y_2(f)Y_2^*(f)$, the power of the first ghost can be analytically approximated with

$$S_{amb}(k=1) \propto \cos \left(+\pi \text{PRF} \frac{b_2}{2v_s} \right). \quad (7)$$

The cosine argument confirms that a perfect rejection is achieved for interleaved pulses. Besides, the notch behaviour suggests that small errors in the PRF selection lead to significant degradation in the ambiguity performance. The same analytical method can be extended to a generic N -satellite case, yielding for the k -th ambiguity

$$S_{amb}(k) \propto \left| \sum_{n=1}^N \exp \left(-j\pi k \text{PRF} \frac{b_n}{v_s} \right) \right| \quad (8)$$

with $b_1 = 0$. When the baselines are known, the intensity of the first K ambiguities can hence be obtained by the sub-optimal estimate

$$\hat{\text{PRF}} = \underset{\text{PRF}}{\text{argmin}} \sum_{k=1}^K \left| \sum_{n=1}^N \exp \left(-j\pi k \text{PRF} \frac{b_n}{v_s} \right) \right|^2 \quad (9)$$

that can be found through exhaustive search since the domain is monodimensional.

2.2. Random PRF

In this configuration, the pulse repetition interval is not defined by a function, but it is randomly drawn from the interval

$$\text{PRI}_{min} < \text{PRI} < \text{PRI}_{max} \quad (10)$$

where only the valid PRI values (i.e. not causing blind echoes) are accepted. The lower boundary on the PRI is given by the antenna size in elevation, L_e . Note that the technological implementation of completely random patterns is here neglected in order to focus on the theoretical concept comparison. Analogously to the patterned PRI scenarios discussed in [1], a random PRI system does not generate ambiguities

that appear as clear shifted replicas of the image, but rather it defocuses the ambiguities, spreading them on a larger area, or, for high $\Delta\text{PRI} = \text{PRI}_{max} - \text{PRI}_{min}$, on the whole scene. A notable advantage of a fully random PRI strategy is the invariance of the performance on the azimuth target position. Differently from the uniform PRF configuration, the choice of the two parameters, $\text{PRI}_{mean} = (\text{PRI}_{min} + \text{PRI}_{max})/2$ and ΔPRI , is not dependent on the baselines and hence can be done once for the whole mission.

2.3. Signal reconstruction

The signal reconstruction can be performed either in the frequency or in the time domain. The latter approach, proposed in [1], has been herewith adopted. The samples from the different channels must be then weighted and interpolated to a regular and denser grid. This is done in through the Best Linear Unbiased (BLU) estimation that applies in practice a Kriging interpolation based on the PSD of the system. After the interpolation procedure, the interpolated signal is then compressed via the matched filter approach. If a uniformly illuminated antenna aperture is used in transmission as well as in reception, the azimuth PSD of $u(t)$ is given by

$$P_u(f) = \text{sinc}^4\left(\frac{L_a}{2v_s}f\right) \quad (11)$$

The normalized auto-correlation function $R_u(t)$ of the complex random process $u(t)$ is proportional to the inverse transform of $P_u(f)$ and takes the closed form

$$R_u(t) = \begin{cases} 0 & t \leq -\frac{2}{a} \\ \frac{a^3 t^3}{4} + \frac{3a^2 t^2}{2} + 3at + 2 & t \in]-\frac{2}{a}, -\frac{1}{a}] \\ -\frac{3a^3 t^3}{4} - \frac{3a^2 t^2}{2} + 1 & t \in]-\frac{1}{a}, 0] \\ \frac{3a^3 t^3}{4} - \frac{3a^2 t^2}{2} + 1 & t \in]0, \frac{1}{a}] \\ -\frac{a^3 t^3}{4} + \frac{3a^2 t^2}{2} - 3at + 2 & t \in]\frac{1}{a}, \frac{2}{a}] \\ 0 & t > \frac{2}{a} \end{cases} \quad (12)$$

where $a = \frac{2v_s}{L_a}$. The samples are hence assumed uncorrelated for $|t| > \frac{L_a}{v_s}$.

3. RESULTS AND DISCUSSION

A constellation of small satellites operating in S-Band is discussed. The relevant system concept specifications are reported in Table 1. Two different azimuth antenna lengths are tested: 1 m for system A and 1.5 m length for system B. The antenna size in elevation is fixed to 1.5 m. Such configuration leads to a swath width of 20 km in slant range and 30 km in ground range. Accounting for a duty cycle of 0.2, it readily follows that the maximum allowed PRF, in order to accommodate the swath width, amounts to 4600 Hz approximately. In an ideally interleaved DPC system, three satellites would

Table 1. Relevant specifications of the swarmSAR system

Parameter	System A	System B
Frequency	3.2 GHz	
Orbit height	514 km	
Along-track baselines	200 m	
Antenna type	Planar array	
Antenna size, azimuth	1 m	1.5 m
Antenna size, elevation	1.5 m	
Antenna tilt, elevation	26	
Incidence angle near	26.3	
Incidence angle far	30.2	
Slant range near	568 km	
Skant range far	588 km	

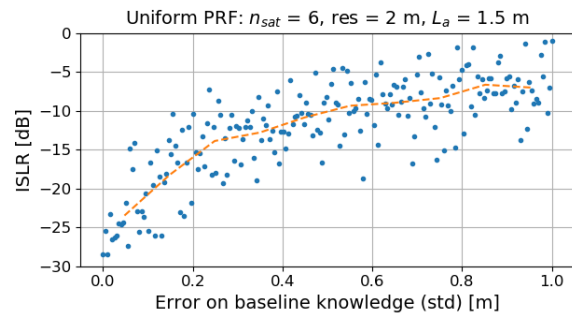


Fig. 2. Performance of a swarm system with uniform PRF = 4030 Hz for different uncertainties in the baseline estimates.

hence be sufficient to achieve an optimal ambiguity rejection. In the presented concept, two consecutive satellites are separated by an average (along-track) baseline of 200 m. In the simulations, an additional perturbation with 5 meter standard deviation is introduced on their position for a statistical performance assessment over 20 baseline realizations.

The analysis will focus on the azimuth ambiguity performance. In order to compare the uniform and random PRF strategies the Integrated Side-Lobe Ratio (ISLR) metric will be adopted. The canonical azimuth ambiguities to signal ratio expressions are in fact not suited for continuously varying PRI systems. Note that a Hann window has applied during the focusing process in order to improve the ISLR performance. Consequently, a decrease in the resolution by a factor 2 has to be accounted on the top of the processed bandwidth. Besides, the first sidelobes are not accounted in the integral computation.

In the uniform PRF scenario the performance is dependent on the effectiveness of (9) and hence on the uncertainties on the satellite positions before the acquisition. It is shown in Fig. 2 that a standard deviation of 20 cm on the baseline knowledge can raise the ISLR to -15 dB with 6 satellites. For the next simulations we will however assume perfect a-posteriori baseline knowledge. In the random sampling sce-

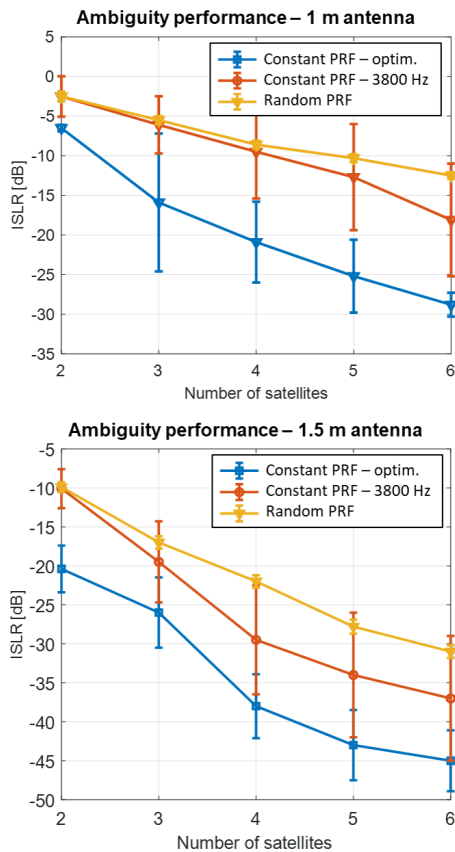


Fig. 3. Performance of system A (top) and system B (bottom), differing in azimuth antenna length. The same azimuth bandwidth, corresponding to a 2 meter resolution, has been processed in both systems.

nario, a PRF range of 400 Hz between 3600 and 4000 Hz is selected, where the PRI is randomly drawn being careful not to transmit during receive echo windows. The performance of the random PRF configuration is compared to that of two uniform PRF scenarios. The first scenario assumes no a-priori (pre-acquisition) information on the baselines. In this configuration, the PRF is set to a fixed PRF = 3800 Hz value for all the simulations. Conversely, the second scenario is that of perfect a-priori baseline knowledge, enabling hence a correct application of (9). The results are reported in Fig. 3 for the two different antenna configurations in Table 1. The 1 meter antenna configuration, whose appeal is that of saving stowage volume (a key aspect for small satellites), performs significantly (5 dB) worse than the 1.5 m configuration, making its implementation critical for $N < 6$. In the 1.5 m scenario 4 satellites are enough to guarantee a good azimuth ambiguity performance (< -20 dB). The random PRF strategy performs worst than the uniform PRF scenarios, however it has the advantage of delivering products with more stable and predictable quality. Finally, the PRF optimization strat-

egy performs very well in presence of perfect online baseline knowledge, however the technological solutions demanded to achieve such information accuracy and to apply such technique in real-time is deemed extremely challenging.

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