

**Assessment of GRACE monthly solutions by quantifying the noise level in mass anomaly time-series with the variance component estimation (PPT)**

Ditmar, Pavel; Brussee, Marenka; Sun, Yu; Riva, Riccardo

**Publication date**

2018

**Document Version**

Final published version

**Citation (APA)**

Ditmar, P., Brussee, M., Sun, Y., & Riva, R. (2018). *Assessment of GRACE monthly solutions by quantifying the noise level in mass anomaly time-series with the variance component estimation (PPT)*. GSTM 2018: GRACE / GRACE-FO Science Team Meeting 2018, Potsdam, Germany.

**Important note**

To cite this publication, please use the final published version (if applicable). Please check the document version above.

**Copyright**

Other than for strictly personal use, it is not permitted to download, forward or distribute the text or part of it, without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license such as Creative Commons.

**Takedown policy**

Please contact us and provide details if you believe this document breaches copyrights. We will remove access to the work immediately and investigate your claim.

# **Assessment of GRACE monthly solutions by quantifying the noise level in mass anomaly time-series with the variance component estimation**

**Pavel Ditmar<sup>1</sup>, Marenka Brussee<sup>1</sup>, Yu Sun<sup>1,2</sup>, and Riccardo Riva<sup>1</sup>**

*<sup>1</sup>Delft University of Technology, Delft, The Netherlands*

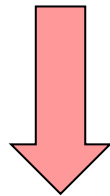
*<sup>2</sup>Fuzhou University, Fuzhou, China*

# Considered GRACE RL06 solutions

- Solution variants: JPL, CSR, ITSG
- Time interval: Jan. 2003 – Mar. 2016
- $L_{\max} = 60$
- Degree-1 and  $C_{20}$  SH coefficients: from a combination of OBP estimates and other GRACE-based coefficients (Sun et al, GJI, 2016)
- 400-km Gauss filter is applied

# Joint regularized data processing

**Unknown parameters**



$$\left\{ \begin{array}{l} \cancel{A^{(1)}} x = d^{(1)} \\ \dots \\ \cancel{A^{(n)}} x = d^{(n)} \\ Dx = 0 \end{array} \right. \quad \left. \begin{array}{l} \text{Observations} \\ \\ \text{Pseudo-observations} \\ \text{(define the regularization} \\ \text{condition applied)} \end{array} \right.$$

# Possible regularization conditions (case of a continuous function $x(t)$ in the time domain)

Zero-order Tikhonov regularization:  $\Omega[x] = \int (x(t))^2 dt$

---

First-order Tikhonov regularization:  $\Omega[x] = \int (\dot{x}(t))^2 dt$


---

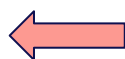
Minimization of

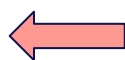
Year-to-year

Differences:

Let  $x(t) = \begin{pmatrix} \xi_1(t) \\ \xi_2(t) \\ \dots \\ \xi_K(t) \end{pmatrix}$

 Unknown function in year 1

 Unknown function in year 2

 Unknown function in year  $K$

$$\Omega[x] = \sum_{k=1}^{K-1} \int_0^1 \left( \xi_{k+1}(t) - \xi_k(t) \right)^2 dt$$

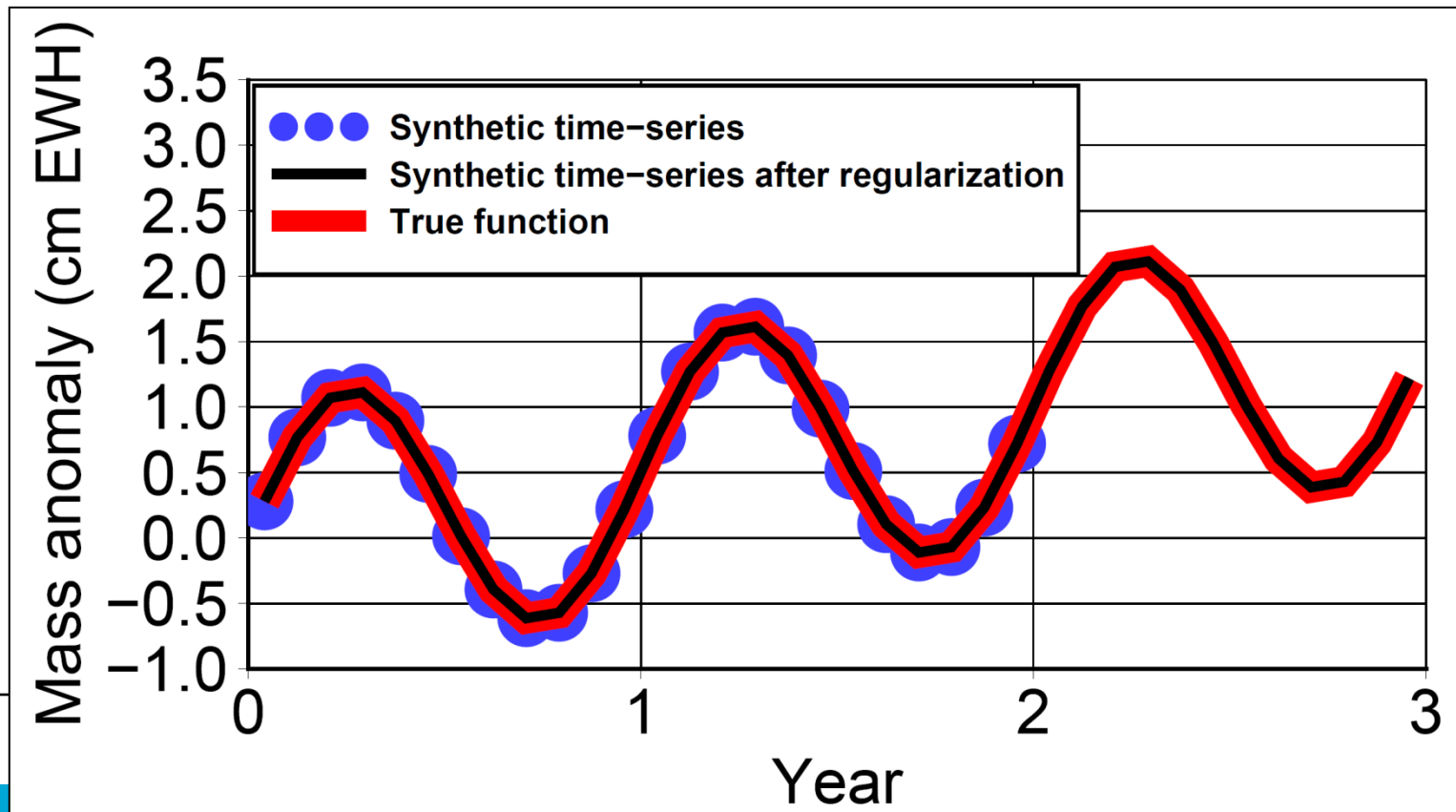
( $t$  – time in years)

# Example: Climatology-tailored regularization in the absence of noise and penalized signals

$$x(t) = \sin 2\pi t + 0.5 \cdot t$$

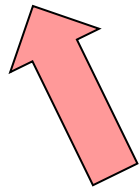
$t$  – time in years

$x(t)$  – Equivalent water heights (EWH) in cm

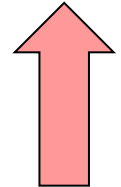
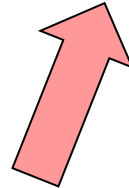


# Minimization functional

$$\Phi[x] = \frac{1}{\sigma_1^2} \sum_i \left( x(t_i) - d_i^{(1)} \right)^2 + \dots + \frac{1}{\sigma_n^2} \sum_i \left( x(t_i) - d_i^{(n)} \right)^2 + \frac{1}{\sigma_s^2} \Omega[x]$$



**Data noise variances**



**Signal variance**

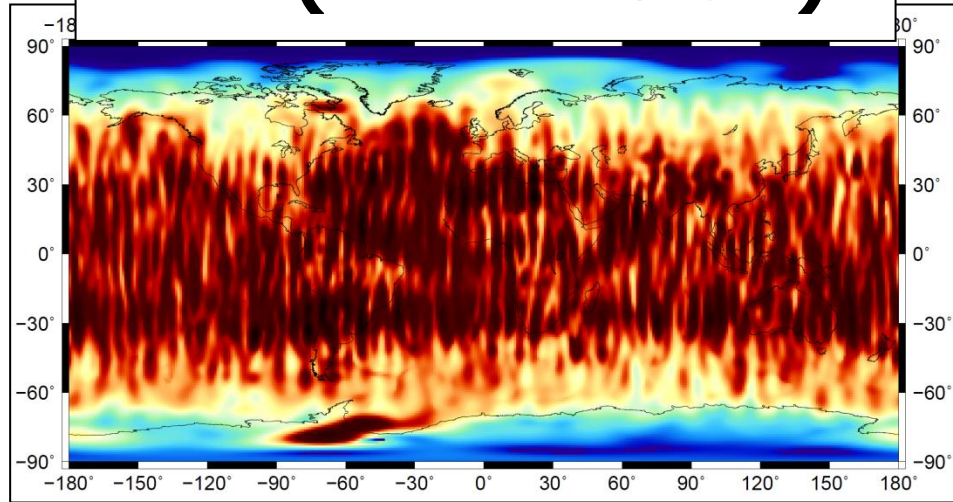
Estimation of noise and signal variances:

Variance Component Estimation (VCE) method

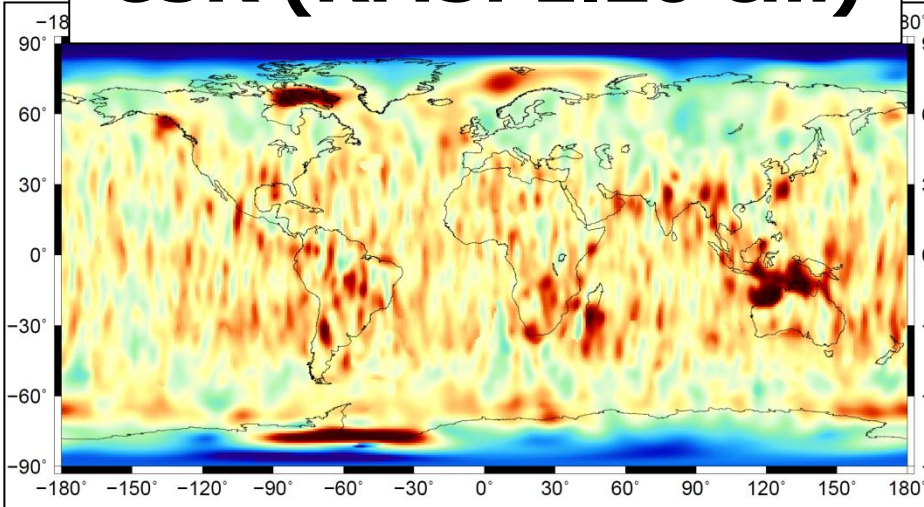
(Koch & Kusche, JoG, 2002)

Estimated noise of  
GRACE monthly  
solution time-series  
(standard deviation,  
cm EWH)

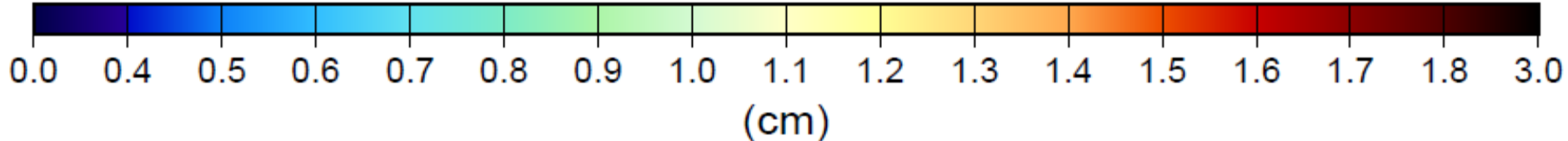
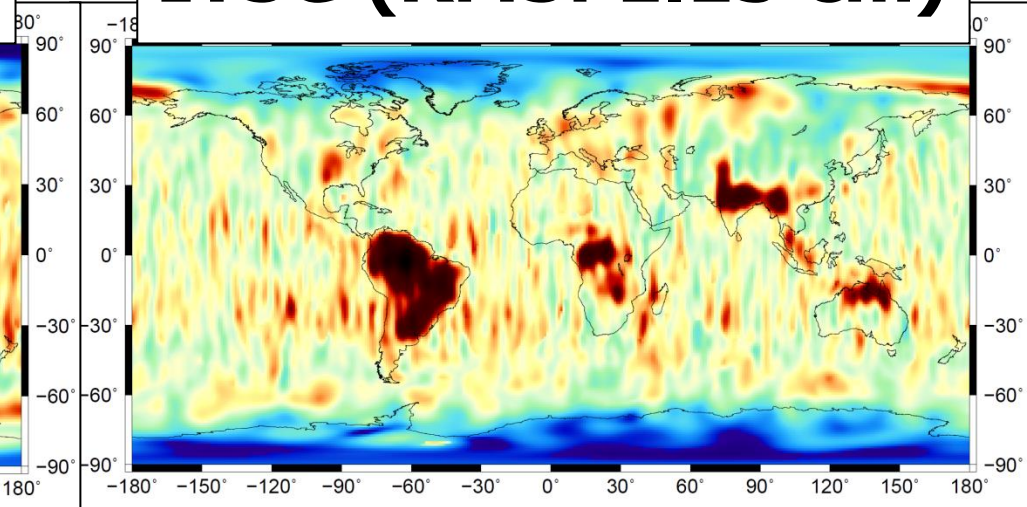
**JPL (RMS: 1.6 cm)**



**CSR (RMS: 1.20 cm)**

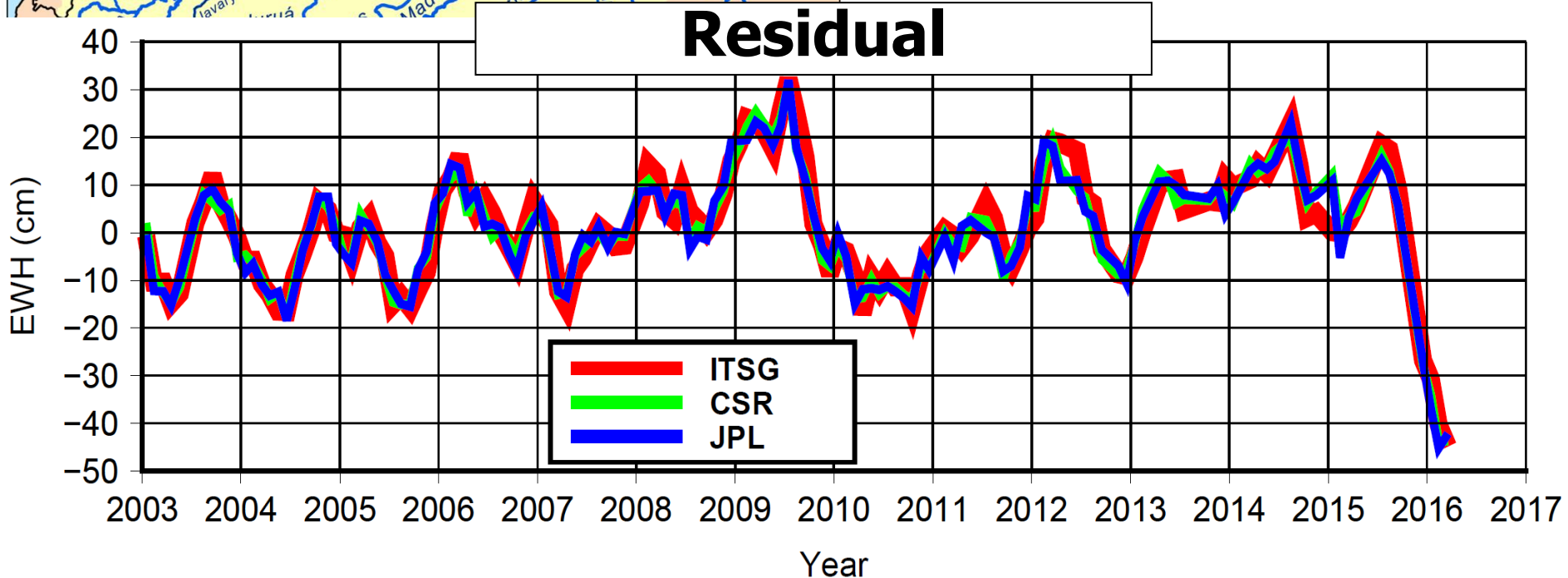
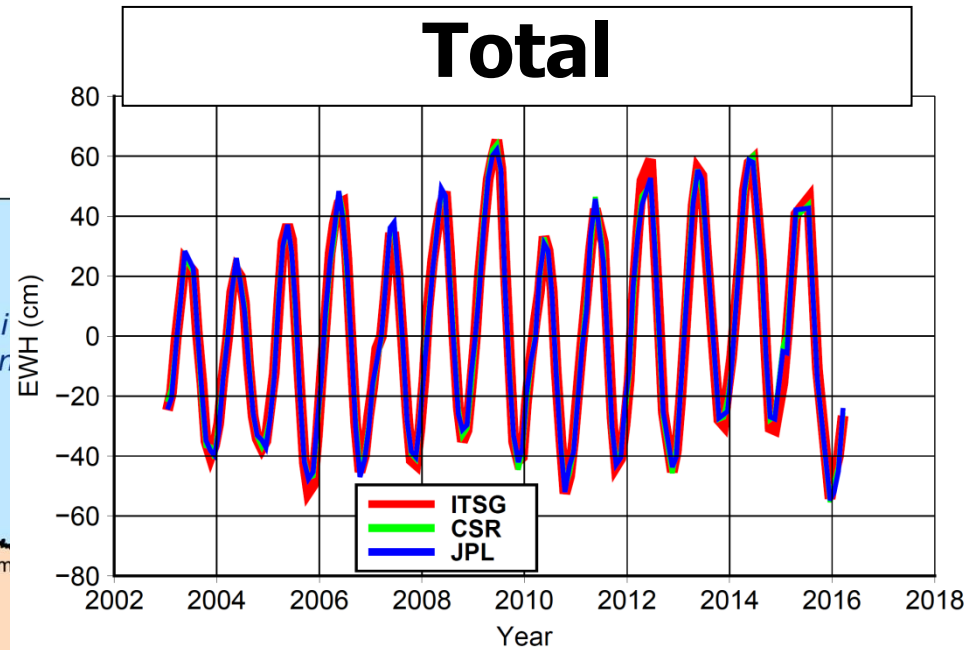


**ITSG (RMS: 1.15 cm)**





# Mass anomaly time-series at Manaus

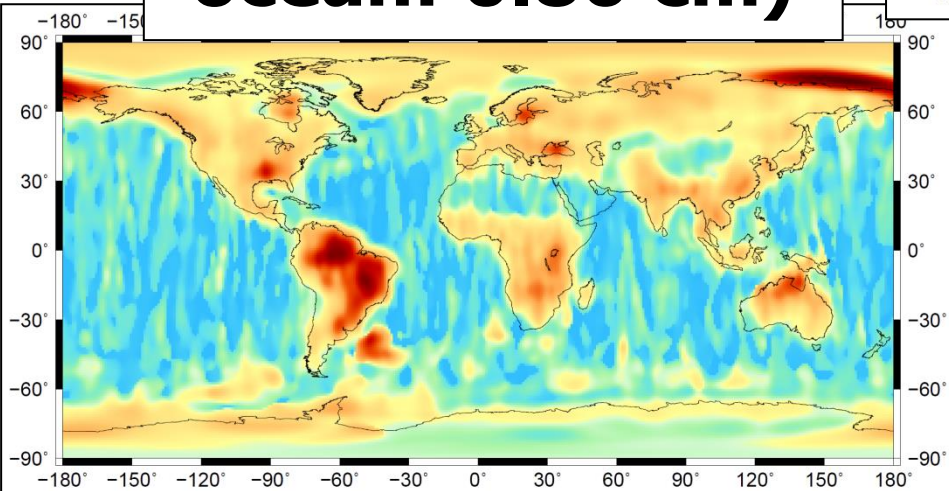


# Estimated noise of GRACE monthly solution time-series (RMS, cm EWH)

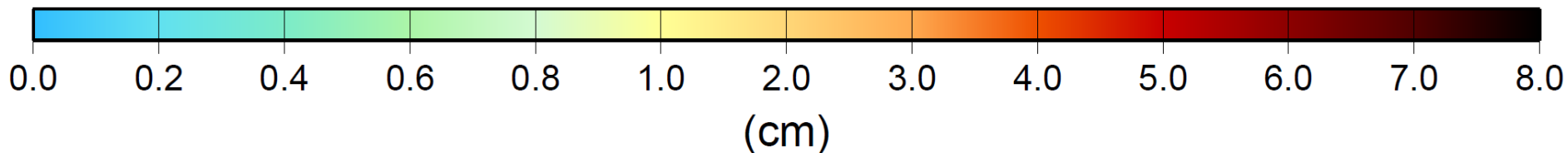
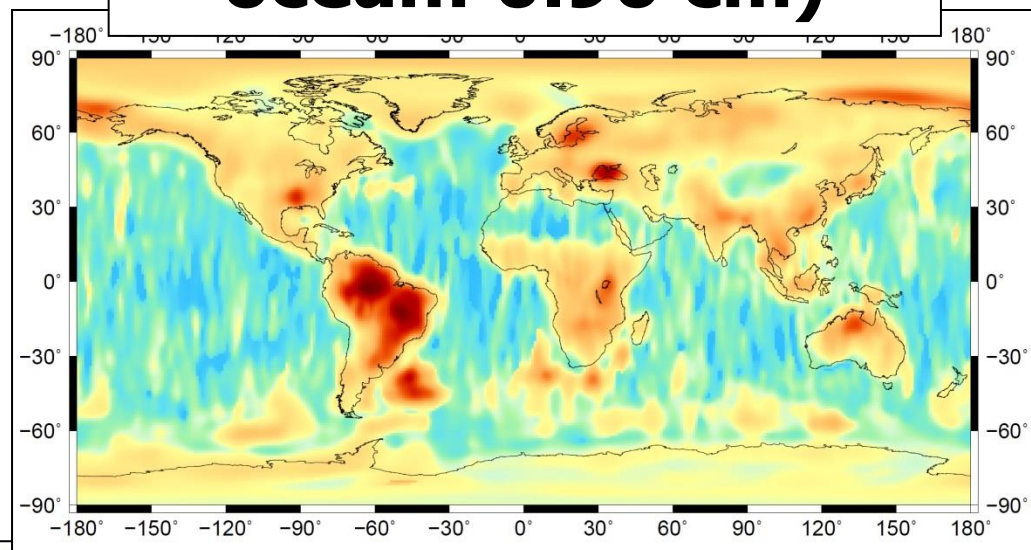
	<b>CSR</b>	<b>ITSG</b>	<b>JPL</b>
<b>Global</b>	<b>1.20</b>	<b>1.15</b>	<b>1.63</b>
<b>Only Ocean</b>	<b>1.21</b>	<b>1.11</b>	<b>1.66</b>
<b>Only land</b>	<b>1.18</b>	<b>1.24</b>	<b>1.64</b>
<b>Antarctica</b>	<b>0.92</b>	<b>0.57</b>	<b>0.81</b>
...			
<b>Australia</b>	<b>1.35</b>	<b>1.26</b>	<b>1.81</b>
<b>South America</b>	<b>1.31</b>	<b>1.89</b>	<b>1.84</b>
<b>Arctic ocean</b>	<b>1.00</b>	<b>0.87</b>	<b>0.85</b>
...			
<b>South Atlantic</b>	<b>1.20</b>	<b>1.16</b>	<b>1.71</b>
<b>Southern Ocean</b>	<b>1.23</b>	<b>0.92</b>	<b>1.24</b>

Estimated MYDD  
signal (standard  
deviation, cm EWH)

**RL05 (RMS over  
ocean: 0.86 cm)**

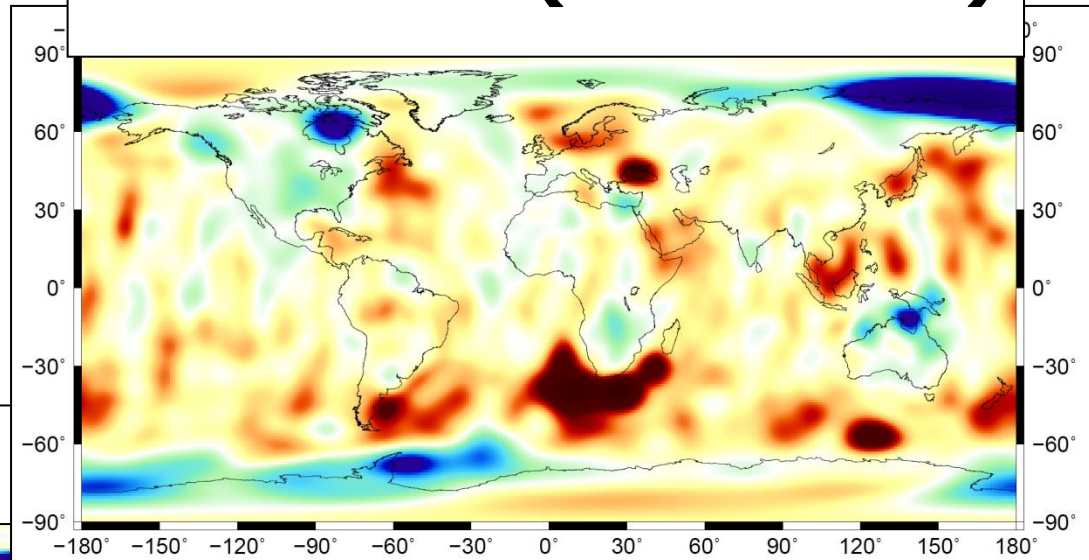


**RL06 (RMS over  
ocean: 0.96 cm)**

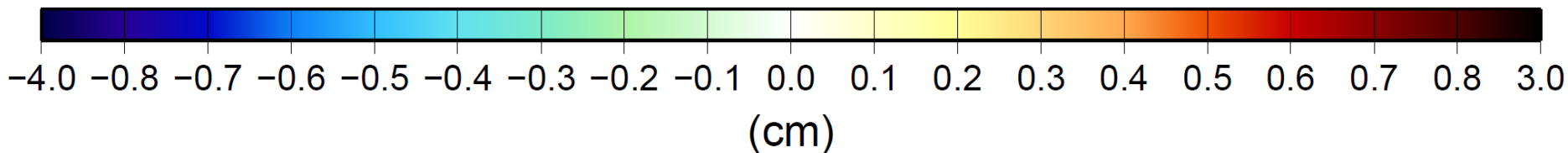
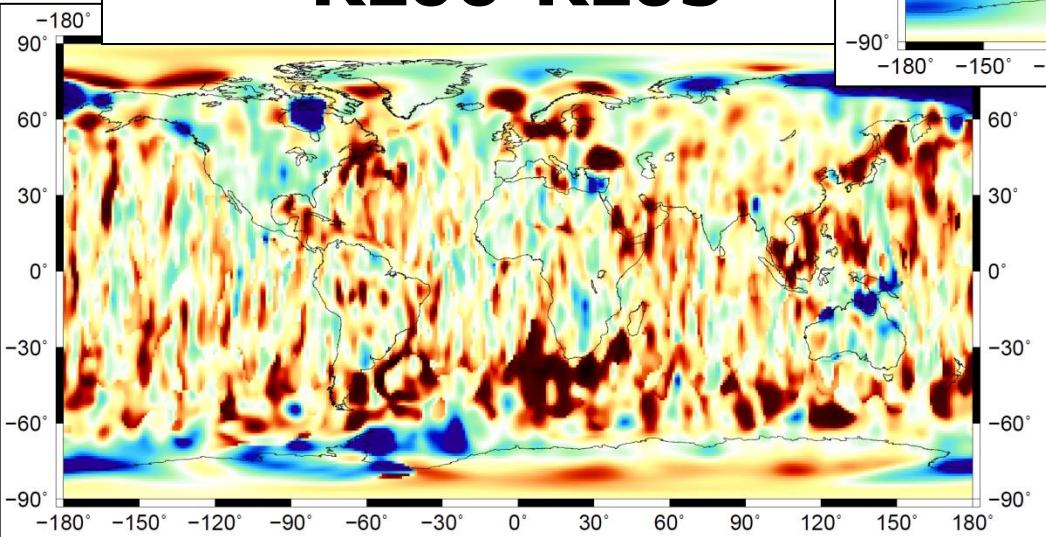


Estimated MYDD  
signal (difference  
of standard  
deviations, cm  
EWH)

**RL06-RL05 (Gauss-400)**



**RL06-RL05**



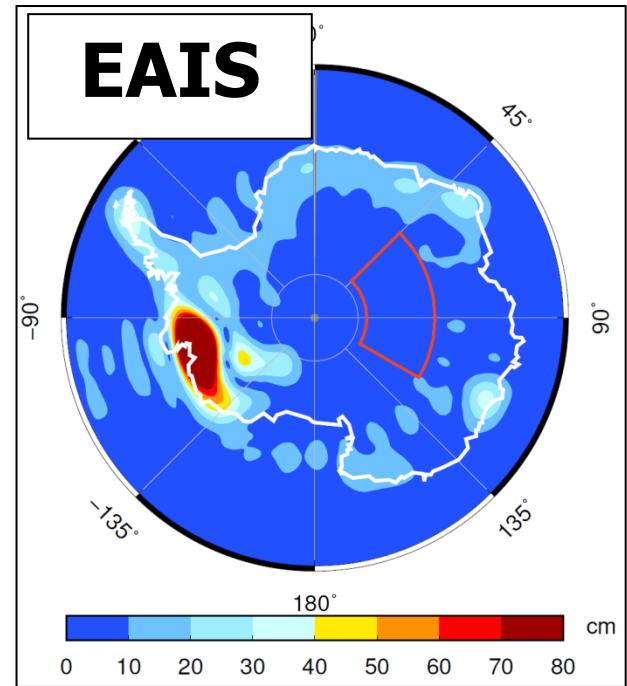


# (Re-)definition of degree-1 and C20 coefficients in GRACE RL06 monthly solutions

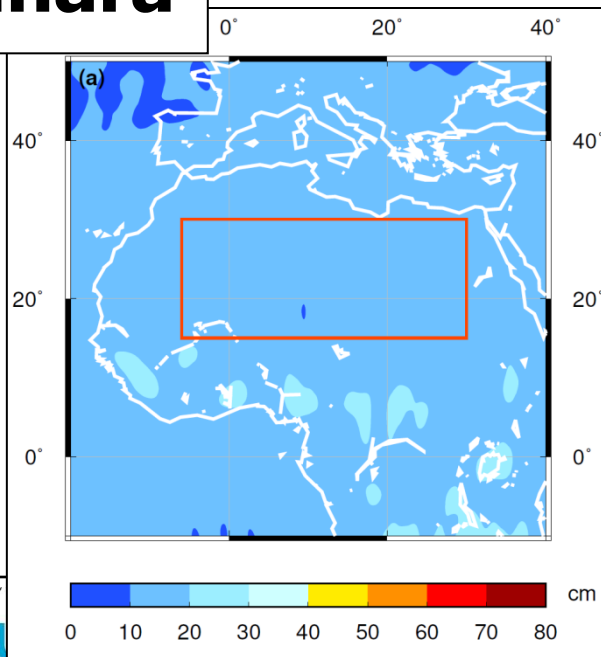
- Major input (Sun et al, GJI, 2016):
  - OBP estimates
  - Other GRACE-based coefficients
- Major differences with respect to (Swenson et al, 2008):
  - $C_{20}$  coefficients are co-estimated
  - SAL effects are taken into account
  - 150-km buffer zone along the coasts is excluded

# Considered test areas

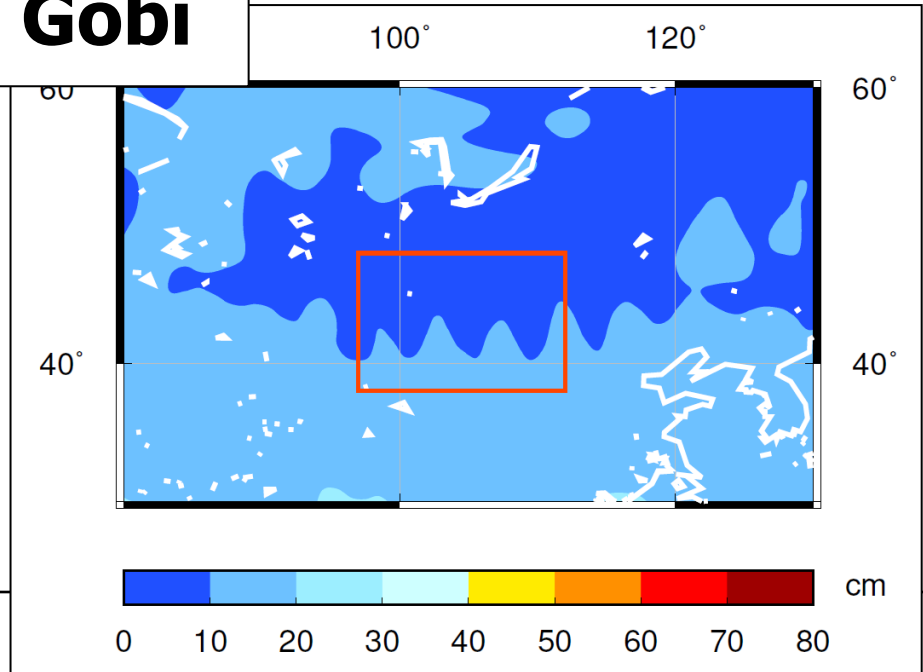
## EAIS



## Sahara

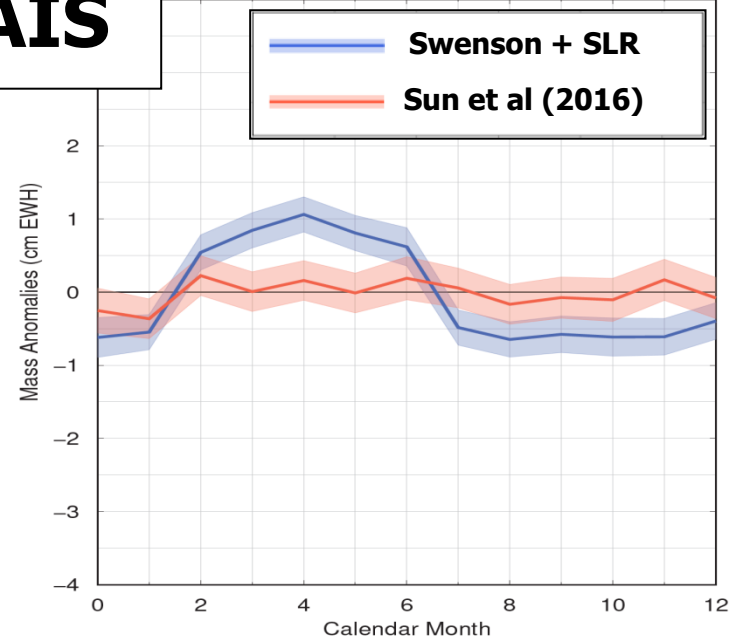


## Gobi

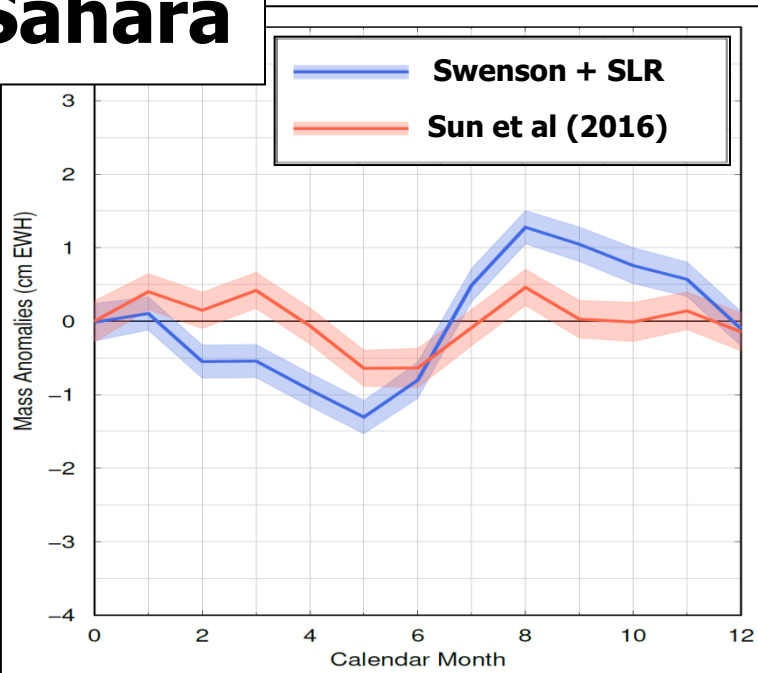


Seasonal cycle of mass anomalies in test areas: Sun et al (2016) vs Swenson et al (2008) + SLR (Cheng et al)

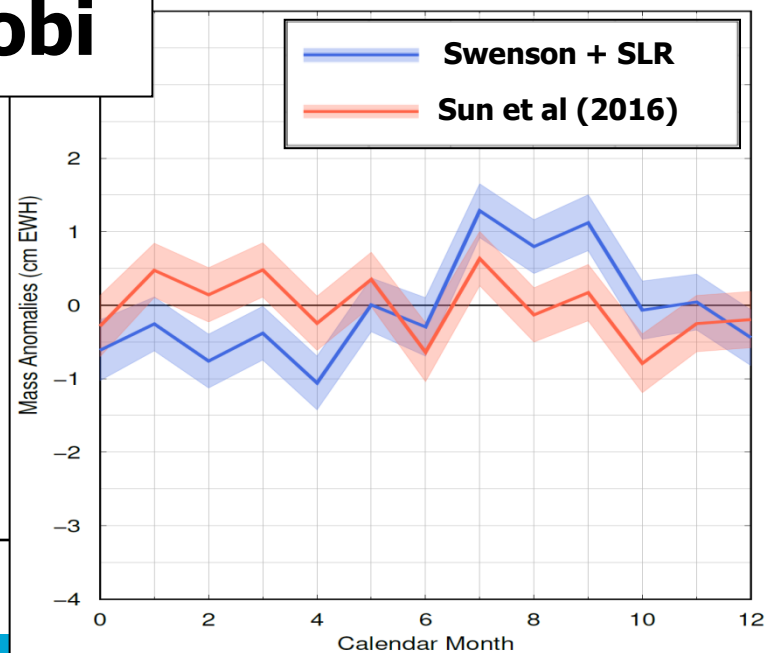
## EAIS



## Sahara



## Gobi



# Conclusions

- The developed technique is a promising tool to quantify noise in mass anomaly time-series in the absence of 'ground truth'
- Application of this techniques allows one to identify various points of concern, e.g.:
  - insufficiently suppressed sensor noise
  - an insufficient accuracy of background ocean tide models
  - temporal offsets in the produced gravity field solutions
- The estimated signal magnitude (in terms of Month-to-month Year-to-year Double Differences) is another way to assess the performance of background ocean models (e.g. the performance of RL05 and RL06 at different geographical locations can be compared in this way)
- The technique of Sun et al (2016) allows for a accurate and internally consistent estimation of degree-1 and  $C_{20}$  SH coefficients