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## Dynamics of the Wave-Driven Circulation in the Lee of Nearshore Reefs

Renan F. da Silva<sup>1,2,3,4,5</sup> , Jeff E. Hansen<sup>1,2,3,5</sup> , Ryan J. Lowe<sup>1,2,3,4,5</sup> , Dirk P. Rijnsdorp<sup>6</sup> , and Mark L. Buckley<sup>7</sup> 

<sup>1</sup>School of Earth Sciences, The University of Western Australia, Crawley, WA, Australia, <sup>2</sup>UWA Oceans Institute, The University of Western Australia, Crawley, WA, Australia, <sup>3</sup>Marine Energy Research Australia, The University of Western Australia, Crawley, WA, Australia, <sup>4</sup>ARC Centre of Excellence for Coral Reef Studies, The University of Western Australia, Crawley, WA, Australia, <sup>5</sup>Oceans Graduate School, The University of Western Australia, Crawley, WA, Australia, <sup>6</sup>Environmental Fluid Mechanics Section, Faculty of Civil Engineering and Geosciences, Delft University of Technology, Delft, The Netherlands, <sup>7</sup>U.S. Geological Survey, St. Petersburg Coastal and Marine Science Center, St. Petersburg, FL, USA

### Key Points:

- Phase-resolved model simulations were used to understand circulation patterns that occur in the lee of small-scale reefs
- Two-cell and four-cell circulation patterns were primarily driven by alongshore pressure gradients, which depend on the setup dynamics
- A four-cell pattern generally developed if the shoreline wave setup in the lee of the reef was less than the adjacent nonreef fronted beach

### Supporting Information:

Supporting Information may be found in the online version of this article.

### Correspondence to:

R. F. da Silva,  
[renan.silva@uwa.edu.au](mailto:renan.silva@uwa.edu.au)

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### Author Contributions:

**Conceptualization:** Renan F. da Silva, Jeff E. Hansen, Ryan J. Lowe, Dirk P. Rijnsdorp, Mark L. Buckley

**Formal analysis:** Renan F. da Silva

**Funding acquisition:** Jeff E. Hansen, Ryan J. Lowe

**Investigation:** Renan F. da Silva

**Methodology:** Renan F. da Silva

**Software:** Renan F. da Silva

**Supervision:** Jeff E. Hansen, Ryan J. Lowe, Dirk P. Rijnsdorp

**Validation:** Renan F. da Silva

**Visualization:** Renan F. da Silva

**Abstract** Nearshore rocky reefs with scales of order 10–100 m are common along the world's coastline and often shape wave-driven hydrodynamics and shoreline morphology in their lee. The interaction of waves with these reefs generally results in either two or four-cell mean circulation systems (2CC and 4CC, respectively), with diverging flows behind the reefs and at the shoreline in the 2CC case and flows that diverge in the lee and converge at the shoreline in the 4CC case. By applying a phase-resolving wave-flow model to conduct a detailed analysis of mean momentum balances for waves interacting with nearshore reefs, we develop an understanding of the drivers of 2CC and 4CC flow dynamics and how they vary for different reef geometries and wave and water level conditions. The 2CC or 4CC patterns were primarily driven by alongshore pressure gradients toward the exposed (nonreef fronted) or reef-fronted beach. These alongshore pressure gradients were dependent on the cross-shore setup dynamics governed by the balance between pressure (i.e., related to the setup) and radiation stress gradients, and mean bottom stresses exerted on the water column. If shoreline wave setup in the lee of the reef was less than the exposed beach, a 4CC pattern developed with convergent flow at the shoreline in the lee of the reef; otherwise, a 2CC emerged with divergent flow at the shoreline. Across the parameter space investigated, reef roughness, distance to the shoreline, and beach slope were the three parameters most likely to change the flow patterns between 2CC and 4CC.

**Plain Language Summary** Small-scale nearshore rocky reefs are found worldwide along a variety of sandy and rocky coastlines. Wave breaking over small reefs drives mean alongshore circulation patterns in their lee that may cause shoreline accretion or erosion. In this study, we apply a wave-flow model to investigate the physical drivers of the mean currents in the lee of small reefs. The alongshore circulation was primarily driven by the differences of the mean water levels between the lee and the adjacent nonreef fronted beaches. Mean water levels increased by wave breaking; however, the onshore-directed mean flows over the reef created offshore-directed bottom stresses that reduced the mean water levels in the reef lee. If the shoreline mean water levels in the lee were less than the adjacent beach, alongshore currents that converged from the adjacent beaches toward the reefs were developed. If the shoreline mean water levels in the lee of the reef exceeded the adjacent beach, alongshore currents that diverged from the reef toward the adjacent beach occurred. The improved understanding of the circulation drivers developed in this study enhances our ability to characterize and predict wave-driven flows in small-scale nearshore reef systems.

## 1. Introduction

Submerged rocky and coral reefs influence the hydrodynamics and coastal processes of many wave-dominated coastlines worldwide. While coral reef systems are typically found at low latitudes, rocky reefs can be found worldwide along a variety of sandy and rocky coastlines (Pondella et al., 2015). For reefs with limited alongshore extent, the alongshore gradients in wave setup (the increase in mean water level due to wave dissipation) result in corresponding alongshore pressure gradients between the lee of the reef and adjacent shorelines not fronted by reefs (hereafter referred to as “exposed” shorelines). These alongshore pressure gradients can be a primary driver of mean alongshore currents in the lee of reefs and can thus influence alongshore sediment fluxes and shoreline changes. Shoreline erosion is typically thought to occur in the lee of reefs (or similar scaled artificial submerged

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**Writing – original draft:** Renan F. da Silva, Jeff E. Hansen, Ryan J. Lowe, Dirk P. Rijnsdorp, Mark L. Buckley  
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structures) in the case of diverging alongshore currents and sediment transport, whereas converging alongshore currents and sediment transport would promote shoreline accretion (Ranasinghe et al., 2006). A detailed understanding of the dynamics of wave-driven flows in the lee of reefs are thus critical for predicting how the presence of reef structures affect coastal morphodynamics.

While the dynamics of wave-driven flows over reefs have been extensively investigated, most studies have focused on coral reef systems (Lowe et al., 2009; Monismith, 2007), which are typically long and wide (lengths and widths in the order of 1,000 m) (Falter et al., 2013; Quataert et al., 2015). Conversely, smaller scale nearshore rocky reefs have limited alongshore lengths and narrower reef flats (e.g., order of 10–100 m). The hydrodynamics of these smaller reef systems are still not well understood (Segura et al., 2018; Winter et al., 2017), which motivates this study. Unlike fringing coral reefs that extend over large scales (cross-shore dimensions of order of 100–1,000 m, e.g., Buckley et al., 2015) or rocky shore platforms that are attached to the shoreline (Poate et al., 2020), here we focus on small submerged reefs that are detached from the shore, and have geometries that resemble artificial reefs (Black & Mead, 2001) and submerged breakwaters (Dean et al., 1997). Small nearshore rocky reef systems can be found around the world, for example, along the west coast of North America (Pondella et al., 2015), the southeast coast of South America (Duarte Nemes et al., 2019), south of Australia (Segura et al., 2018) and New Zealand (Black & Andrews, 2001).

Several studies have analyzed the mean momentum balances to understand the dynamics of the mean flows and setup in coral reef systems (Buckley et al., 2015; da Silva et al., 2020; Rijnsdorp et al., 2021; Sous et al., 2020). However, for smaller reef systems, existing studies have primarily focused on describing the wave-driven flows (Mulligan et al., 2010) and infragravity wave dynamics (Winter et al., 2017) rather than understanding the flow dynamics as they apply to small reefs generally. For alongshore uniform reefs (e.g., shoreline attached fringing coral reefs), the wave-driven setup tends to be approximately constant shoreward of the reef crest where breaking occurs (Buckley et al., 2015, 2016). Conversely, for reefs with alongshore variability in bathymetry (e.g., small reefs and barrier reefs) water can more readily return to the ocean through onshore flows over shallower portions of a reef that in their lee diverge toward the sides and result in lower setup at the shoreline. Alongshore pressure gradients are driven by the larger setup in the lee of a reef compared to the typically deeper exposed profile, where most waves do not break, or break closer to shore. The net forcing of alongshore pressure and radiation stress gradients together with other momentum terms (e.g., advective accelerations) results in alongshore currents near the shoreline (e.g., Hansen et al., 2015).

The drivers of wave-driven nearshore flows have been studied for diverse coastal morphological features through the analysis of mean momentum balances using laboratory experiments (Haller et al., 2002), field measurements (Aptosos et al., 2008; Feddersen et al., 1998, 2011; Hansen et al., 2014), and numerical modeling (da Silva et al., 2021; Hansen et al., 2013, 2015; Long & Özkan-Haller, 2005; Moulton et al., 2017). Momentum balance analysis using experimental observations or phase-averaged wave models have mostly relied on linear wave theory (LWT) to estimate radiation stresses (e.g., Haller et al., 2002), which may limit their accuracy in describing the drivers of mean flow and setup (particularly for complex reef structures). By intrinsically accounting for the nonlinearities in their governing equations, phase-resolved numerical models are able to represent the range of nonlinear wave motions (e.g., Rijnsdorp et al., 2015; Smit et al., 2014), which makes them suitable to calculate full momentum balances, particularly in the lee of nearshore reefs.

Several studies have applied numerical modeling to reproduce the hydrodynamics over reefs with geometries consistent with existing submerged breakwaters (da Silva et al., 2022; Ranasinghe et al., 2006, 2010). These studies have found that the interaction of waves and reefs drive two-cell or four-cell mean circulation patterns depending on the wave conditions and structure geometries. A two-cell circulation (2CC) pattern is characterized by the presence of diverging currents in their lee extending up to the shoreline (Bellotti, 2004; Haller et al., 2002; Moulton et al., 2017). For a four-cell circulation (4CC) pattern, diverging currents occur at the immediate lee of the reef, but converging currents occur at the shoreline. The circulation patterns 2CC and 4CC have been generally associated with erosive and accretive shorelines, respectively, in the lee of reefs (Ranasinghe et al., 2006). Observations of the beach morphology in the lee of small reefs show that natural sites can oscillate between eroding and accreting shorelines depending on water levels (which influence the reef submergence depth) and wave conditions, with a salient sometimes seasonally occurring in the lee of the reefs (Duarte Nemes et al., 2019; Segura et al., 2018). Given their influence in determining the hydrodynamics and morphologic variability it is important to understand the dynamical linkages between water levels, waves, and flow patterns, particularly given that sea level rise will result in a greater submergence depth of most reefs.

While empirical predictive formulations have been proposed based on numerical simulations to predict whether 2CC or 4CC will occur (i.e., as a function of wave and reef parameters) (da Silva et al., 2022; Ranasinghe et al., 2010), these studies have not investigated the detailed dynamical links between reef and wave parameters to explain the resulting circulation patterns. Existing studies have hypothesized that the difference between 2CC and 4CC relates to the reversal of alongshore pressure gradients (Ranasinghe et al., 2006; Villani et al., 2012), with the alongshore pressure gradients being based on the cross-shore setup profiles over the reef and at the exposed beach. However, a detailed momentum balance analysis is required to understand the role of these pressure gradients relative to other terms in the momentum balance as has been done in other nearshore environments (e.g., Hansen et al., 2015).

Here we study the drivers of the wave-induced flow patterns in the lee of small nearshore reefs, with a focus on explaining the physical mechanisms differentiating 2CC and 4CC circulation patterns observed behind reefs. We apply a phase-resolved wave-flow model to calculate the wave-driven flow over idealized submerged reefs and we consider an extensive parameter space, including a range of wave conditions, water levels, reef geometries, roughness, shapes, and beach slopes (Section 3). Through a detailed momentum balance analysis, we describe the dynamics governing 2CC and 4CC (Section 4.1). Next, we study how the wave, reef, and bed properties influence the overall aspects of the flow patterns (Sections 4.2 and 4.3). Finally, we discuss how our findings help advance knowledge of wave-driven flow dynamics in natural reef systems more broadly (Section 5).

## 2. Background: Mean Momentum Balances

To investigate the dynamical drivers of the mean circulation behind the reefs, we analyze the mean (wave-averaged) momentum balance. The steady wave-averaged and depth-integrated momentum equation can be written as (e.g., Mei et al., 2005),

$$(d + \eta)U_j \frac{\partial U_i}{\partial x_j} = - \overbrace{g(d + \eta) \frac{\partial \eta}{\partial x_i}}^{PG} - \overbrace{\frac{\partial S_{ij}}{\partial x_j}}^{RSG} + \overbrace{\langle q_B \rangle \frac{\partial d}{\partial x_i}}^{HRB} + \frac{\overbrace{\partial \left\langle \int_{-d}^{\zeta} \tau_{T,ij} dz \right\rangle}^{TRSG}}{\partial x_j} - \overbrace{\langle \tau_{B,i} \rangle}^{BS} \quad (1)$$

where  $x_i$  and  $z$  denote horizontal ( $i = 1, 2$  being the Einstein summation convention) and vertical directions, respectively,  $t$  is time, the  $\langle \rangle$  indicates time averaging over many wave periods, the subscript  $B$  indicates bed,  $u_i$  is the horizontal velocity component in  $i$  direction,  $d$  is the still water depth,  $\zeta$  is the instantaneous water level deviation from  $d$ ,  $\eta$  is the mean water level deviation from  $d$ ,  $\tau_{T,ij}$  and  $\tau_B$  are the turbulent Reynolds stresses and bottom stress, respectively,  $g$  is the acceleration due to gravity and  $q$  is the nonhydrostatic pressure divided by the seawater density ( $q = p - g(\zeta - z)$ , where  $p$  is the total pressure divided by the density). The velocity signal is decomposed into a mass-flux velocity  $U_i$  (Mei et al., 2005):

$$U_i = \left\langle \int_{-d}^{\zeta} u_i dz \right\rangle / (d + \eta) \quad (2)$$

and a fluctuating (wave) component  $\tilde{u}_i$  ( $\tilde{u}_i = u_i - U_i$ ). The left-hand side of Equation 1 is the advective acceleration ( $AA = (d + \langle \zeta \rangle)U_j \partial U_i / \partial x_j$ ). The right side is composed of a pressure gradient term ( $PG = g(d + \eta) \partial \eta / \partial x_i$ ), a radiation stress gradient (wave force) term ( $RSG = \partial S_{ij} / \partial x_j$ ), where the radiation stress  $S_{ij}$  is

$$S_{ij} = \left\langle \int_{-d}^{\zeta} \tilde{u}_i \tilde{u}_j dz \right\rangle + \left\langle \int_{-d}^{\zeta} p dz \right\rangle - 0.5 g(d + \eta)^2 \quad (3)$$

a term describing the mean hydrodynamic reaction at the bottom ( $HRB = \langle q_B \rangle \partial d / \partial x_i$ ), a turbulent Reynolds stress gradient term ( $TRSG = \partial \left\langle \int_{-d}^{\zeta} \tau_{T,ij} dz \right\rangle / \partial x_j$ ), and a bottom stress term ( $BS = \langle \tau_{B,iz} \rangle$ ). Using our terminology, Equation 1 can be rewritten as:

$$AA_i = -PG_i - RSG_i + HRB_i + TRSG_i - BS_i \quad (4)$$

Based on the cross-shore direction convention where positive  $x$  is directed offshore from the still water shoreline at  $x = 0$  m, a shoreward-directed forcing by radiation stress gradients, pressure gradients and bottom stresses that all contain negative values in their definition in Equation 4, correspond to positive values of  $RS G_x$ ,  $PG_x$ , and  $BS_x$ .

### 3. Methods

#### 3.1. Three-Dimensional Wave-Flow Numerical Model

We applied the nonhydrostatic phase-resolved model SWASH version 6.01 (Zijlema & Stelling, 2005, 2008) to simulate the nearshore hydrodynamics. SWASH is a numerical implementation of the Reynolds Averaged Navier Stokes (RANS) equations,

$$\frac{\partial u_j}{\partial x_j} + \frac{\partial w}{\partial z} = 0 \quad (5)$$

$$\frac{\partial u_i}{\partial t} + \frac{\partial u_i u_j}{\partial x_j} + \frac{\partial u_i w}{\partial z} + \frac{\partial p}{\partial x_i} = \frac{\partial \tau_{r,ij}}{\partial x_j} + \frac{\partial \tau_{iz}}{\partial z} \quad (6)$$

$$\frac{\partial w}{\partial t} + \frac{\partial w u_j}{\partial x_j} + \frac{\partial w w}{\partial z} + \frac{\partial p}{\partial z} = -g + \frac{\partial \tau_{r,zj}}{\partial x_j} + \frac{\partial \tau_{zz}}{\partial z} \quad (7)$$

where  $w$  is the vertical velocity. The depth-integration of the continuity equation, Equation 5, results in,

$$\frac{\partial \zeta}{\partial t} + \frac{\partial \int_{-d}^{\zeta} u_j dz}{\partial x_j} = 0 \quad (8)$$

With the multilevel approach, the fluid domain between the bottom  $z = -d(x_i)$  and the free surface  $z = \zeta(x_i, t)$  is divided into  $K$  layers ( $k = 1$  and  $K$  at the bottom and water surface, respectively), where the governing equations, Equations 5–7, together with the global continuity equation, Equation 8, are resolved. To parameterize the instantaneous bottom stresses  $\tau_B$ , we used the quadratic friction law,

$$\tau_{B,i} = c_f (U_{dep}^2 + V_{dep}^2) \frac{u_{B,i}}{\sqrt{u_B^2 + v_B^2}} \quad (9)$$

where  $c_f$  is the dimensionless friction coefficient,  $U_{dep,i}$  is the horizontal depth-averaged velocity,

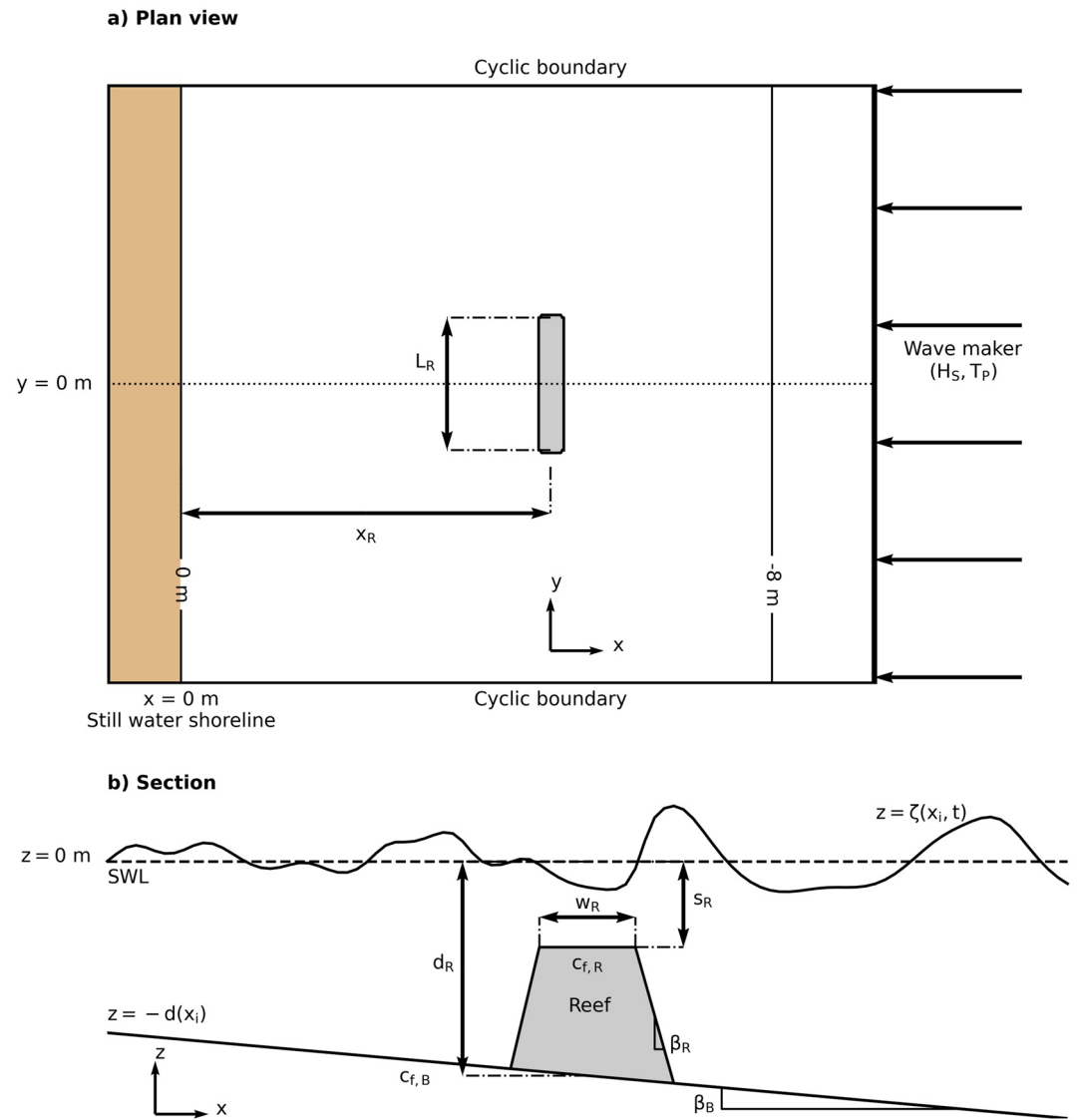
$$U_{dep,i} = \frac{\int_{-d}^{\zeta} u_i dz}{d + \zeta} \quad (10)$$

and  $u_{B,i}$  is the near-bed horizontal velocity (calculated at  $k = 1$ ). Horizontal turbulent mixing was modeled with a Smagorinsky-type formulation. As we used two vertical layers in the simulations ( $K = 2$ ), which was found to be appropriate to resolve the wave-driven hydrodynamics (see Section 3.3), no additional turbulence closure model was used for vertical mixing.

#### 3.2. Reef Layouts and Parameter Space

We simulated the wave-driven flow across a range of small-scale reefs with geometries consistent with nearshore rocky reefs (Duarte Nemes et al., 2019; Pondella et al., 2015). The reefs were idealized as rectangle-shaped (Figure 1). However, in Section 5.2 other reef shapes with similar crest areas and locations are shown to have overall similar flow patterns. We varied the following reef geometry parameters (see Figure 1 for schematic of the reef, Table 1 for notation, Table 2 for parameter space):

- the distance offshore, measured from the shoreline at  $x = 0$  m to the center of the reef crest  $x_R$  (subscript  $R$  indicates reef) ( $100 \leq x_R \leq 250$  m);



**Figure 1.** Diagram of the model domain and reef in (a) plan view and (b) cross section with key reef variables labeled.

- the depth  $d_R$  of the base of each reef ( $2 \leq d_R \leq 12.5$  m);
- the cross-shore crest widths  $w_R$  ( $10 \leq w_R \leq 50$  m);
- the alongshore crest lengths  $L_R$  ( $100 \leq L_R \leq 400$  m); and
- the crest level submergence  $s_R$  ( $-1 \leq s_R \leq -0.5$  m; relative to the still water level (SWL) and negative downward). Note that  $s_R$  can also be interpreted as a proxy for the SWL, thus changing  $s_R$  could indicate variations of water levels (e.g., tidal fluctuations).

Each reef had a constant 1:1 slope along its perimeter. To investigate the influence of enhanced bottom roughness of the reef relative to adjacent areas, the friction coefficient  $c_{f,R}$  of the reefs was varied over the simulations ( $0.01 \leq c_{f,R} \leq 0.1$ ). Note that because we used a phase-resolved model, the  $c_f$  relates the instantaneous bottom shear stresses and depth-averaged velocities (Equation 9). Most existing characterizations of friction (or bottom drag) coefficients have focused on those based on mean flow dynamics rather than instantaneous (combined mean and wave orbital currents); thus, we adopted the range of  $c_{f,R}$  based on studies of mean momentum balances associated with mean currents observed on reefs (e.g., Rosman & Hench, 2011). In Section 5.1, we briefly discuss implications for uncertainty in  $c_{f,R}$  in further detail. The friction coefficient for the surrounding area and beach was kept constant at  $c_{f,B} = 0.005$  across simulations, typical for a sandy seabed. The nearshore and beach profile (excluding the reef) had a uniform linear slope  $\tan \beta_B$  (i.e., a constant linear slope for the entire shoreface up

**Table 1**  
*Notation*

Symbol	Definition	Units
$c_f$	Dimensionless friction coefficient	–
$d$	Still water depth	m
$d_R$	Reef base depth (at midcrest) (Figure 1)	m
$g$	Gravitational acceleration	$\text{m s}^{-2}$
$h$	Total water depth	m
$H_S$	Significant wave height	m
$H_{S,0}$	Deep water significant wave height	m
$L$	Distance between reef center and exposed beach	m
$L_{P,0}$	Deep water peak wavelength	m
$L_{P,wm}$	Peak wavelength at the wave maker	m
$L_R$	Reef alongshore crest length (Figure 1)	m
$p$	Total pressure divided by density	$\text{m}^2 \text{s}^{-2}$
$q$	Nonhydrostatic pressure divided by density	$\text{m}^2 \text{s}^{-2}$
$Q_i$	Mass-flux	$\text{m}^2 \text{s}^{-1}$
$s_R$	Reef crest level (Figure 1)	m
$T_P$	Peak wave period	s
$u_{B,i}$	Bottom-layer horizontal velocity	$\text{m s}^{-1}$
$u_i$	Instantaneous horizontal velocity	$\text{m s}^{-1}$
$\tilde{u}_i$	Oscillatory horizontal velocity (calculated by subtracting $U$ from $u$ )	$\text{m s}^{-1}$
$U_i$	Mass-flux velocity	$\text{m s}^{-1}$
$U_{dep,i}$	Instantaneous depth-averaged velocity	$\text{m s}^{-1}$
$x$	Cross-shore position	m
$w$	Vertical velocity	$\text{m s}^{-1}$
$x_i$	Horizontal position	m
$x_R$	Distance from reef crest center to still water shoreline (Figure 1)	m
$w_R$	Reef width (Figure 1)	m
$y$	Alongshore position	m
$z$	Vertical position	m
$\beta_B$	Beach slope (Figure 1)	–
$\beta_R$	Reef slope (Figure 1)	–
$\Delta\eta$	Shoreline setup difference between reef center and exposed profile.	m
$\Delta x_i$	Grid size	m
$\zeta$	Water level deviation from $d$	m
$\eta$	Mean water level deviation from $d$	m
$\eta_E$	Shoreline setup at the exposed profile	m
$\eta_R$	Shoreline setup at the reef center	m
$\sigma_\zeta$	Water level standard deviation	m
$\tau_{B,i}$	Bottom shear stress divided by density	$\text{m}^2 \text{s}^{-2}$

to land, which are hereafter referred to as beach slope). The range of simulated slopes ( $0.01 \leq \tan \beta_B \leq 0.05$ ) spanned mild-sloping ( $\tan \beta_B = 0.01$ ) to steeply sloping ( $\tan \beta_B = 0.05$ ) beach profiles. We note that the variations of reef friction coefficients and beach slopes have not been explored in previous studies (e.g., da Silva et al., 2022; Ranasinghe et al., 2010).

**Table 2**  
*Parameter Space*

Type	Variable	Notation	Values (reference)	Units
Reef properties	Reef crest submergence	$s_R$	−1 to −0.5 (−0.5)	m
	Distance from reef crest to shoreline	$x_R$	100–250 (100 <sup>a</sup> and 250 <sup>b</sup> )	m
	Reef length	$L_R$	100–400 (200)	m
	Reef width	$w_R$	10–50 (25)	m
	Reef base depth (at midcrest)	$d_R$	2–5 (2 <sup>a</sup> and 5 <sup>b</sup> )	m
	Reef friction coefficient	$c_{f,R}$	0.01–0.10 (0.01)	–
Wave parameters	Offshore significant wave height	$H_{S,0}$	0.5–2 (1)	m
	Peak wave period	$T_P$	5–15 (10)	s
Bed properties	Beach slope	$\tan \beta_B$	0.01–0.05 (0.02)	–

<sup>a</sup>Two-cell circulation (2CC) representative case. <sup>b</sup>Four-cell circulation (4CC) representative case.

To represent common wave conditions found along wave-dominated coastlines, we imposed irregular shore-normal long-crested waves (with one-sided directional spread of 10°) by varying the following wave parameters:

- Offshore significant wave height  $H_{S,0}$  ( $0.5 \leq H_{S,0} \leq 2$  m); and
- Peak wave periods  $T_P$  ( $5 \leq T_P \leq 15$  s).

Overall, for this multivariate parameter space we conducted a total of 261 individual simulations. Note that we only considered waves that break over the reefs (roughly indicated by  $H_{S,0}/|s_R| > 1$ ) given their ability to induce stronger nearshore currents (e.g., da Silva et al., 2022).

### 3.3. Model Setup

The model domain included a single shore-parallel reef superimposed on an otherwise alongshore uniform bathymetry (Figure 1). The wave maker was placed in a flat region with a depth of 8 m, followed by the linearly sloping bed (except at the reef). At the offshore weakly reflective wave maker, we imposed irregular waves with a JONSWAP spectrum including bound waves (Rijnsdorp et al., 2015). At the boundary, shoaling from offshore deep water to the wave maker was accounted for using LWT. At the alongshore boundaries we imposed cyclic conditions, with which the flows recirculate from one side to the other. To minimize boundary effects, the flat region adjacent to the wave maker had a length of 2 times the peak wavelength at the wave maker  $L_{P,ums}$ , and the distance from the reef to the lateral boundaries was 10  $L_{P,um}$  (e.g., da Silva et al., 2022). This modeling approach represents the effect of a single reef due to the long distances from the reef to the model lateral boundaries (i.e., limited edge effects, see da Silva et al., 2022).

All simulations had a cross-shore grid resolution  $\Delta x$  of 1.0–1.5 m (with higher resolutions near the beach) and a uniform alongshore grid resolution  $\Delta y$  of 4 m (e.g., da Silva et al., 2022), which resulted in at least 20 cells per peak wavelength at the outer edge of the surf zone. We used two vertically equidistant sigma layers ( $K = 2$ ) that ensured an accurate representation of wave dispersion (Zijlema et al., 2011). Wave breaking was represented with the use of the hydrostatic front approximation (Smit et al., 2013). By using a target Courant number (CFL) of 0.4–0.8 and an initial time step of 0.05 s, SWASH can continuously adjust the time step to ensure model stability.

We adopted a simulation length of 500  $T_P$ . The first 200  $T_P$  served as spin-up before reaching quasi steady hydrodynamic state, and the remaining 300  $T_P$  was used for the model output. For a  $T_P = 10$  s, these periods correspond to a simulation length of 1 hr 23 min, with a spin-up time of 33 min and analysis period of 50 min. The spin-up length was calculated by ensuring that the domain-integrated energy and enstrophy reached quasi steady conditions (Feddersen et al., 2011).

### 3.4. Momentum Balance Analysis

The water level time series were used to calculate the significant wave height  $H_S = 4\sigma_\zeta$ , where  $\sigma_\zeta$  is the water level standard deviation, and the mean water levels  $\eta$  (i.e., the time-averaged difference from SWL), hereafter



referred to as setup. For the mean flow properties, we calculated the mass-flux velocity  $U_i$  (Equation 2) and the mean depth-averaged velocity  $U_{dep}$  (Equation 10). For simplicity, hereafter we refer to mass-flux velocity  $U_i$  as mean currents, whereas specific references to  $U_{dep}$  are indicated.

For the momentum balance analysis, we calculated each term in Equation 1 in both the cross-shore ( $x$ ) and along-shore ( $y$ ) directions. These momentum terms were calculated according to the method of da Silva et al. (2021), where each term was calculated internally within the model, consistent with SWASH's numerical discretization, ensuring a closure of Equation 1 at computational precision (i.e., effectively no residual errors). As SWASH solves the RANS equations (Section 3.1), we have access to the intrawave (instantaneous) variables (i.e.,  $u_i$ ,  $\zeta$ ,  $\tau_T$ ,  $\tau_B$ ,  $p$ , and  $q$ ) that are needed to calculate each term in Equation 1 as per their definition. As the RANS equations intrinsically compute nonlinear wave motions, the calculation of radiation stresses  $S_{i,j}$  considers the nonlinear effects on the oscillatory velocities  $\bar{u}_i$  without the need to rely on often assumed LWT approximations. Given that in this method all mean variables are calculated within SWASH, the mean momentum terms were calculated by considering a sample frequency equal to the inverse of the time step ( $\sim 20$  Hz) without the need to output and store a large amount of data.

### 3.5. Model Validation

While the overall lack of laboratory or field measurements in similar small rocky reef systems prevents a direct validation of our cases, SWASH has previously been successfully validated in the lee of artificial reef systems (da Silva et al., 2022). Their validation against the wave basin experiments with V-shaped reefs from Ranasinghe et al. (2006) demonstrated the model skills in reproducing the wave-driven flows (note that in this study we use similar reef layout and model setup). In addition, SWASH has been validated in barred beaches with rip channels (da Silva et al., 2021; Villani et al., 2012; Zijlema et al., 2011), whose mean flow patterns (i.e., 2CC and 4CC) are comparable to those observed in reef systems.

## 4. Dynamics of the Wave-Driven Flows

### 4.1. Momentum Balances of Representative 2CC and 4CC Patterns

To explain the flow dynamics of 2CC and 4CC patterns, and in particular to understand the dominant drivers of diverging and converging currents along the shoreline, we explored the depth-integrated mean momentum balances for representative 2CC and 4CC cases, shown in Figures 2 and 3, respectively. Using these two examples, we can characterize the overall wave-driven flow patterns resulting from waves breaking on top of reefs. These 2CC and 4CC cases had the same wave conditions ( $H_{S,0} = 1$  m,  $T_P = 10$  s) imposed over a 1/50 beach slope (Figure 1). For both cases, a reef with width  $w_R$  of 25 m, length  $L_R$  of 200 m, crest submergence  $s_R$  of  $-0.5$  m, and friction coefficient  $c_{f,R}$  of 0.01 was considered. The only difference between the representative 2CC and 4CC is the reef distance to the shoreline  $x_R$  (which also alters the associated crest base depths  $d_R$ ), with the reef located at  $x_R = 100$  m ( $d_R = 2$  m) for the 2CC case and at  $x_R = 250$  m ( $d_R = 5$  m) for the 4CC case.

#### 4.1.1. Cross-Shore Momentum Balances

For both of the representative cases, waves are attenuated by breaking over the reef (Figures 2a and 3a), which establishes setup gradients (Figures 2b and 3b) and onshore flows across the reef (Figures 2c and 3c). Wave reflection at the reef results in node and antinode patterns of wave heights and setup that are visible offshore of the reef (Figures 2a, 2b, 2d, 2e and Figures 3a, 3b, 3d, 3e). To calculate the reflection coefficient ( $H_{S,R}/H_{S,I}$ , where the subscripts R and I designate reflected and incident, respectively), we separated the incident and reflected components of the wave with a frequency domain algorithm using LWT (Buckley et al., 2015). The reflection coefficient for the representative cases varied from 0.3 to 0.5 within 100 m offshore of the seaward edge of the reef (not shown). For both cases, the cross-shore flow dynamics over the reef are primarily governed by a balance between shoreward radiation stress gradients (positive  $RSG_x$ ) resulting from wave breaking (Figures 2d and 3d), and seaward pressure gradients (negative  $PG_x$ ) associated with the setup (Figures 2e and 3e). The net of these terms is balanced by the advective acceleration  $AA_x$  (Figures 2f and 3f) and seaward bottom stresses  $BS_x$  (Figures 2g and 3g). Consistent with the variable velocities over the reef,  $AA_x$  can be both shoreward and seaward directed and is dominated by  $(d + \langle \zeta \rangle)U \frac{\partial U}{\partial x}$  (not shown).

Next, we examined the significance of each of the dominant forcing terms in driving currents (Figure 4). We calculated the magnitude of the dominant forcing terms, the  $PG$ ,  $RSG$ , and  $AA$  normalized by their sum. With these normalized magnitudes, the red ( $AA$ ), green ( $PG$ ), and blue ( $RSG$ ) are combined to form colors, whose

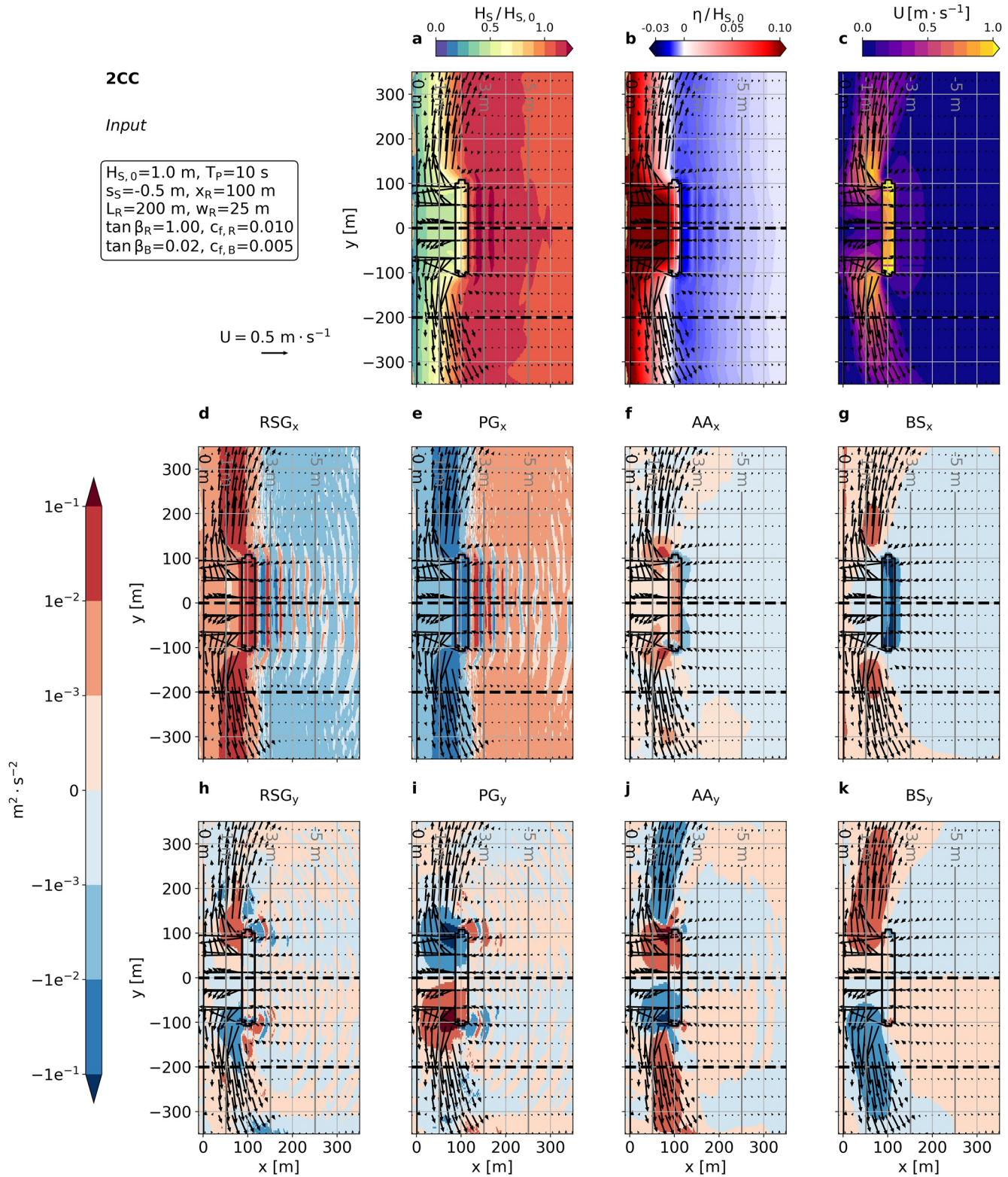


Figure 2.

spatial variations inform where each term (or their combination) dominates. In regions with the basic colors (red, green, and blue), a single momentum term dominates and is counteracted by  $BS$ , whereas in regions with no currents (thus with zero  $BS$ ), the combination of terms driving the balance equals zero. We included numbered markers in Figure 4 to represent places with well-established momentum regimes. The overall dominance of the  $PG_x$  and  $RSG_x$  is observed both offshore and onshore of the reef (markers 1 and 2, respectively, in Figures 4a and 4c). For the 4CC case, parts of the lee of the reef are partially dominated by  $AA_x$  (e.g., marker three in Figure 4c), which occurs where the cross-shore currents reverse from onshore to offshore.

#### 4.1.1.1. Cross-Shore Profiles Over Reef Center and Exposed Profile

The cross-shore profiles over the reef center ( $y = 0$  m) and at the exposed profile (calculated at  $y = -L_R/2 - x_R$ , where alongshore currents near the shoreline are limited—see dashed lines in Figures 2 and 3) indicate that waves rapidly break over the reef (Figure 5a) and drive an increase in the setup in the immediate lee of the reef (Figure 5b). This is in contrast to the more mild wave breaking and gradual increase in setup across the exposed profile (Figures 5a and 5b). At the center of the reef ( $y = 0$  m), the flow accelerates over the seaward reef slope and decelerates over the shoreward slope (Figures 2f and 3f). While their cross-shore balances are qualitatively similar, the 2CC case is characterized by weaker onshore flow and larger setup than the 4CC case for the same wave forcing (Figures 5a and 5c).

To understand the mechanisms responsible for the different cross-shore setup profiles between the 2CC and 4CC cases, we investigated the role of different momentum terms in driving setup. With the physical mechanisms driving the setup dynamics for 2CC and 4CC cases, we can estimate the alongshore pressure gradients that largely influence the alongshore flow dynamics (Section 4.1.2). According to Equation 1, the cross-shore pressure gradient  $PG_x$  is balanced by all remaining cross-shore momentum terms and thus allows us to reconstruct the setup using different combinations of cross-shore momentum terms. By comparing the reconstructed and modeled setup, we assessed the relative importance of each term in driving setup. With a zero setup offshore as a boundary condition, the reconstructed setup was calculated iteratively from the offshore boundary shoreward. We analyzed the setup profile at the reef center ( $y = 0$  m) and exposed beach ( $y = -L_R/2 - x_R$ ) for the representative 2CC and 4CC cases.

The setup reconstruction using only the  $RSG_x$  term (denoted  $\eta_{RSG_x}^{recon}$ ) results in increased setup in the reef lee extending up to the shoreline for both cases (Figure 5b). The setup profile reconstructed with both  $RSG_x$  and  $BS_x$  terms ( $\eta_{RSG_x+BS_x}^{recon}$ ) reduces the bias and approaches the actual model predicted setup (Figure 5b), consistent with the dominance of these terms (along with  $PG_x$ ) in the cross-shore momentum balance. Due to the seaward mean bottom stresses (Figure 5d) that arise in response to onshore flows  $U_{dep}$  (Figure 5c), the reef roughness acts as a sink of momentum and reduces the setup. In contrast to over the reef, the setup at the exposed profile can be accurately reconstructed with only  $RSG_x$  ( $\eta_{RSG_x}^{recon}$ ; Figure 5b) that characterizes a classic balance between  $RSG_x$  and  $PG_x$  (Longuet-Higgins & Stewart, 1964). Unlike the reef profile, a shoreward-directed  $BS_x$  develops in response to the undertow approaching the shoreline ( $x < 10$  m, Figures 5c and 5d); however, the setup contribution from the  $BS_x$  term is negligible (note that in Figure 5b the black dashed and dotted lines coincide). The shoreline setup is larger for 2CC than for 4CC cases (Figure 5b) because of the more efficient momentum transfer from  $RSG_x$  to  $PG_x$  (under similar offshore wave forcing) combined with the lower setup reduction due to weaker  $U_{dep}$  and  $BS_x$  for the 2CC (Figures 5c and 5d). As a result, the setup at the exposed profile exceeds the 4CC reef setup at  $x = 80$  m and the larger setup near the shoreline results in alongshore pressure gradients and converging flows, which do not occur for the 2CC (Figure 5b).

#### 4.1.2. Alongshore Momentum Balances

For the 2CC case, in the reef lee and near the shoreline ( $0 < x < 80$  m), the wave heights are lower and the setup larger than at the exposed profile (Figures 5a and 5b). As a consequence, when considering the alongshore

**Figure 2.** Plan views of (a) normalized significant wave height  $H_S/H_{S,0}$ , (b) normalized setup  $\eta/H_{S,0}$ , (c) mass-flux velocity magnitude  $U$ , and (d–k) depth-integrated mean momentum terms for a representative case of two-cell circulation (2CC) resulting from waves interacting with reefs. In all panels, vectors indicate the mass-flux velocities  $U_i$ , whereas colors indicate each variable. (d, h) Radiation stress gradient  $RSG$  in the  $x$ - (d) and  $y$ - (h) directions. (e, i) Pressure gradients  $PG$  in the  $x$ - (e) and  $y$ - (i) directions. (f, j) Advective acceleration  $AA$  in the  $x$ - (f) and  $y$ - (j) directions. (g, k) Bottom stress  $BS$  in the  $x$ - (g) and  $y$ - (k) directions. The definition of each momentum term is given in Equation 1 and we note that the remaining terms had negligible contributions. The gray and black lines give the depth and reef contours, respectively. The dashed black lines give the reef center and exposed beach transects (see Section 4.1). The simulation input conditions are listed on the upper left table (see Figure 1 and Table 1 for definition of each variable).

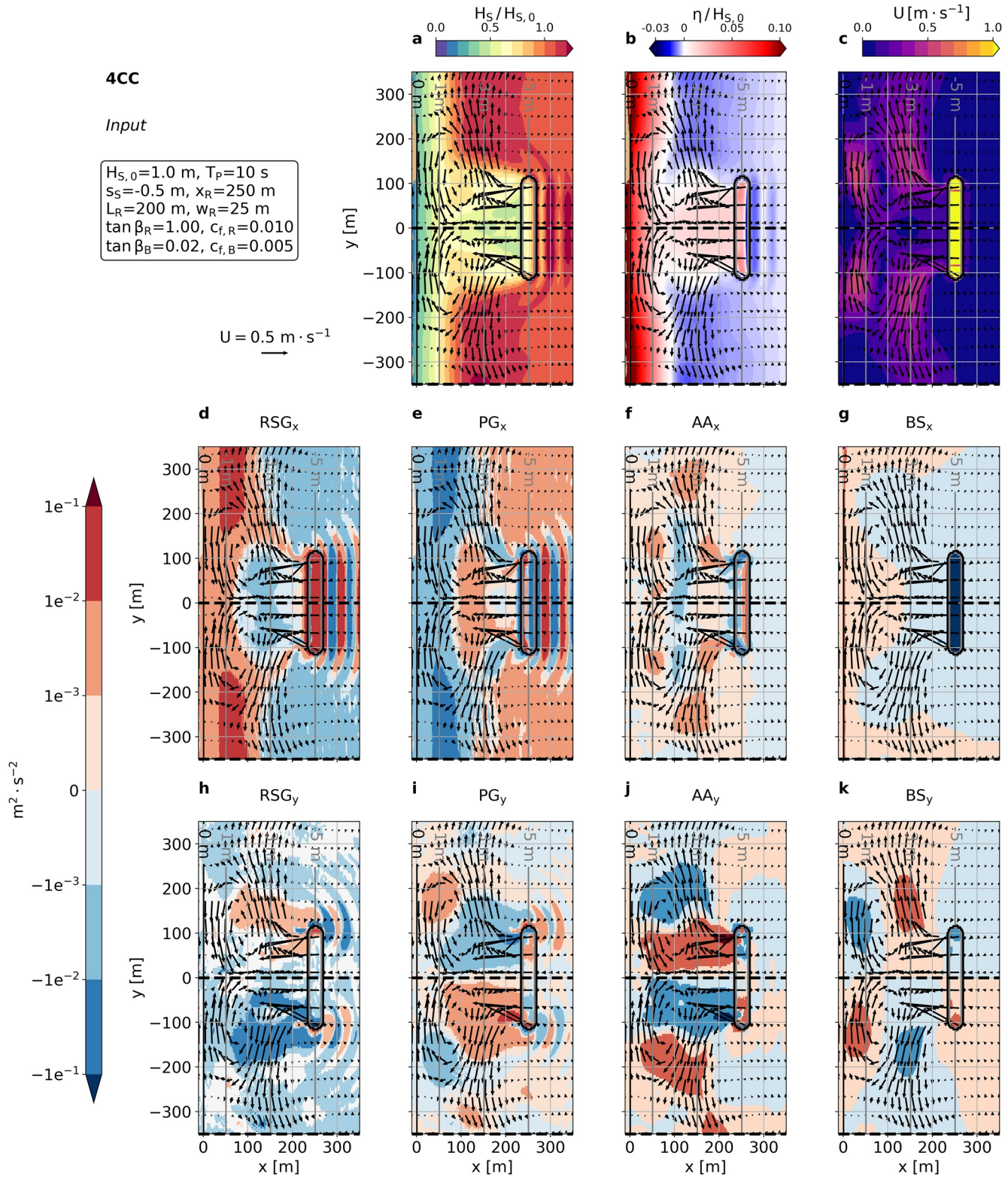
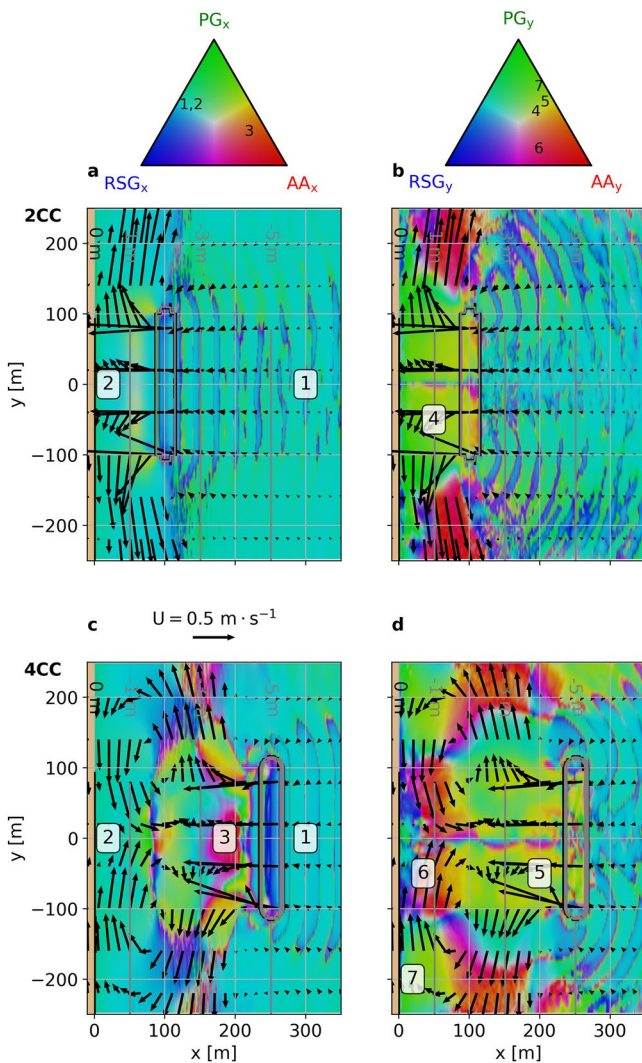


Figure 3.

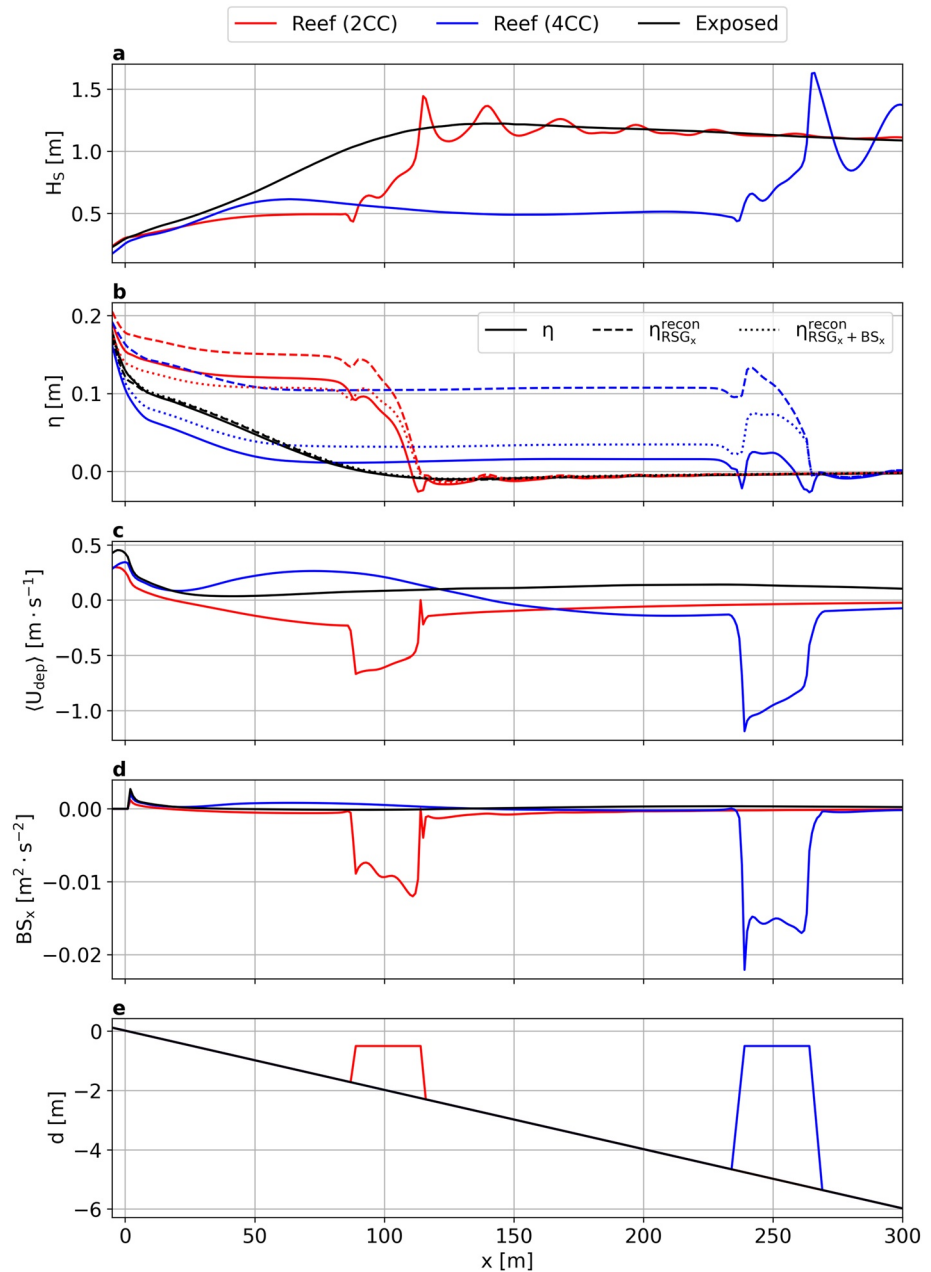


**Figure 4.** Map views of relative contribution of depth-integrated mean momentum terms for (a, b) a representative case of two-cell circulation (2CC) and (c, d) four-cell circulation (4CC) in (a, c)  $x$ - and (b, d)  $y$ -directions resulting from waves interacting with reefs. Vectors indicate the mass-flux velocities  $U_i$  whereas the (RGB) colors are calculated from the ratio of the absolute values of pressure gradients  $PG$  (green), advective acceleration  $AA$  (red), and radiation stress gradient  $RSG$  (blue), and the sum of their absolute values, normalized by their maximum values. The definition of each momentum term is given in Equation 1. The gray and black lines give the depth and reef contours, respectively. The numbered markers indicate key positions referenced in the text.

momentum balances, diverging (away from the reef)  $PG_y$  (Figure 2i) and converging (toward the reef)  $RSG_y$  (Figure 2h) are opposite in sign, with the former being larger in magnitude than the latter (marker four in Figure 4b). The net of  $PG_y$  and  $RSG_y$  is balanced by converging  $AA_y$  (Figure 2j) and diverging  $BS_y$  (Figure 2k), with the latter a response to the diverging currents (Figure 2c). The converging  $AA_y$  is dominated by the contribution from  $(d + \langle \zeta \rangle) V \partial V / \partial y$  (not shown). For the 4CC, the diverging flows in the immediate lee of the reef ( $100 < x < 230$  m) are qualitatively driven by similar dynamics to the 2CC (Figures 3h–3k; notice general dominance of  $PG_y$  represented by marker 5 in Figure 4d). However, close to the shoreline ( $0 < x < 50$  m) converging currents develop due to different dynamics. Wave breaking over the exposed profile (breaking initiates at  $x \sim 120$  m, Figures 5a and 3a, 3d) results in converging  $PG_y$  (Figures 5b and 3i) and also converging  $RSG_y$  (Figure 3h), with the former being generally larger in magnitude than the latter (marker seven in Figure 4d). Together with  $AA_y$  (Figure 3j), their net drives converging  $BS_y$  (Figure 3k) due to the converging mean currents (Figure 3c).

To evaluate the importance of each term in driving alongshore currents, we compared how the  $BS_y$ , which is assumed as a proxy for the mean alongshore currents (see Equation 9), can be described by the sum of different combinations of other terms in Equation 1 (e.g., Hansen et al., 2015). Specifically, we compared the sum of different terms and  $BS_y$  to the 1:1 line. The 1:1 line represents the perfect closure of the balance that occurs in case a given sum of terms exactly matches  $BS_y$ , therefore these terms drive alongshore flows. Linear slopes closer to one indicate better skill and lower errors, whereas  $R^2$  close to one indicates less variance. To be able to represent the local balances, we used a regular output grid with  $x$ -grid and  $y$ -grid sizes of 4 m, and we considered the entire lee of reefs from  $-L_R < y < L_R$  for the representative 2CC ( $x < \sim 100$  m) and 4CC ( $x < \sim 250$  m) cases. We first examined how well the net of  $PG_y$  and  $RSG_y$ , which typically dominate balances, represents  $BS_y$  ( $R^2 = 0.1$ – $0.2$ ), and the slopes of 1.53–1.70 indicate that accounting for  $PG_y + RSG_y$  alone would overestimate the alongshore currents (Figures 6a and 6b). Including  $AA_y$  significantly improves the correlation ( $R^2 \geq 0.67$ , Figures 6c and 6d) and results in regression lines with slopes close to one (1.04–1.06), which demonstrates the overall importance of  $AA_y$  in the alongshore transfer of momentum. For the 4CC case, the advective acceleration  $AA_y$  is particularly important in the lee of the reef close to the shoreline ( $20 < x < 100$  m; marker 6 in Figure 4d). The fact that a perfect correlation ( $R^2 = 1$ ) necessitates the inclusion of the turbulent Reynolds stress gradients,  $TRSG_y$ , and hydrodynamic reaction at the bottom,  $HRB_y$  (Figures 6e–6h), establishes the importance of these terms for accurate local balances and attests to the complexity of the general balances. However, their importance for the overall alongshore flow dynamics is relatively limited due to their typically much lower magnitudes ( $TRSG_y$  and  $HRB_y$  are of order  $10^{-5}$  to  $10^{-4}$   $m^2 s^{-2}$  while  $BS_y$  is of order  $10^{-3}$   $m^2 s^{-2}$ ).

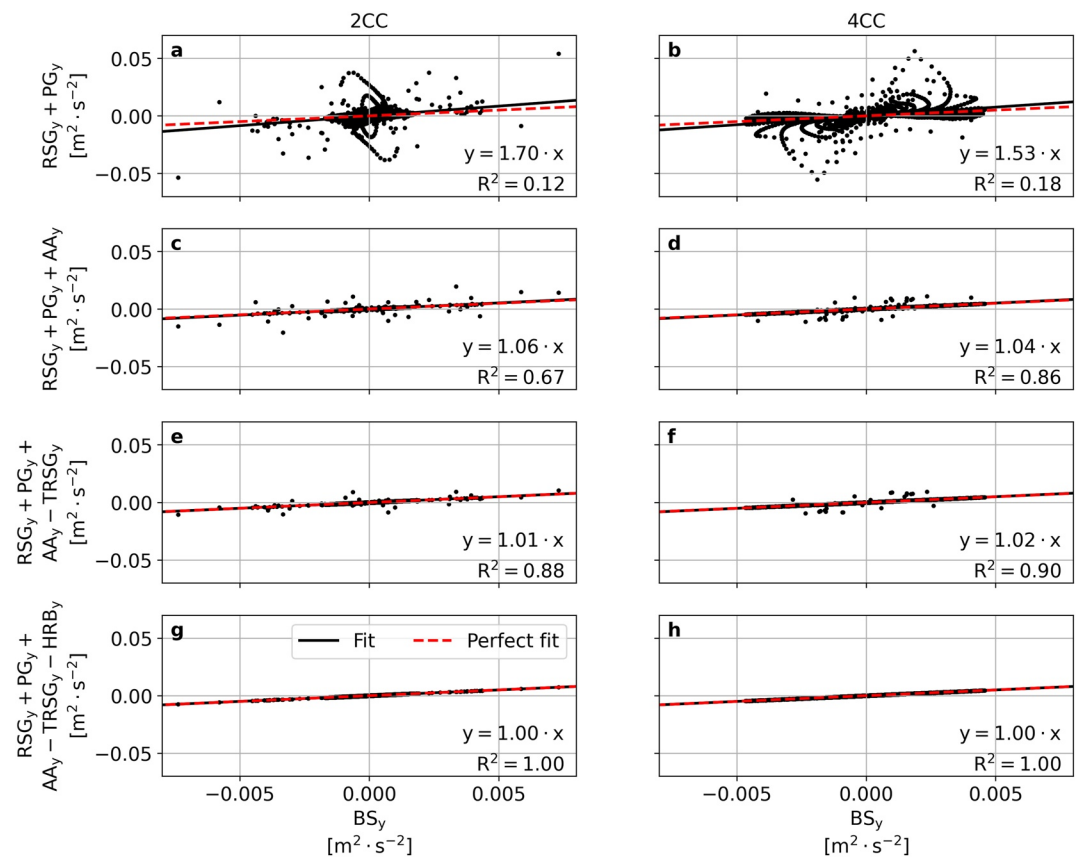
**Figure 3.** Plan views of (a) normalized significant wave height  $H_S/H_{S,0}$ , (b) normalized setup  $\eta/H_{S,0}$ , (c) mass-flux velocity magnitude  $U$ , and (d–k) depth-integrated mean momentum terms for a representative case of four-cell circulation (4CC) resulting from waves interacting with reefs. In all panels, vectors indicate the mass-flux velocities  $U_i$  whereas colors indicate each variable. (d, h) Radiation stress gradient  $RSG$  in the  $x$ - (d) and  $y$ - (h) directions. (e, i) Pressure gradients  $PG$  in the  $x$ - (e) and  $y$ - (i) directions. (f, j) Advective acceleration  $AA$  in the  $x$ - (f) and  $y$ - (j) directions. (g, k) Bottom stresses  $BS_x$  in the  $x$ - (g) and  $y$ - (k) directions. The definition of each momentum term is given in Equation 1 and we note that the remaining terms had negligible contributions. The solid gray and black lines give the depth and reef contours, respectively. The dashed black lines give the reef center and exposed beach transects (see Section 4.1). The simulation input conditions are listed on the upper left table (see Figure 1 and Table 1 for definition of each variable).



**Figure 5.** Cross-shore view of (a) significant wave height  $H_s$ , (b) setup  $\eta$ , (c) mean depth-averaged current  $\langle U_{dep} \rangle$ , (d) bottom stresses  $BS_x$  and (e) still water depth  $d$  at the reef center ( $y = 0$  m) for the representative two-cell circulation (2CC, red lines; Figure 2) and four-cell circulation (4CC, blue lines; Figure 3) cases and at the exposed profile ( $y = -L_R/2 - x_R$ , black lines; note that we only show the exposed profile for the 4CC (black lines) because the 2CC and 4CC results were similar). In addition to the calculated shoreline setup (solid lines), the shoreline setup reconstructed by radiation stress gradients  $RSG_x$  (dashed lines) and net of  $RSG_x$  and bottom stresses  $BS_x$  (dotted lines) are also shown in (b). To reconstruct the shoreline setup  $\eta^{recon}$ , we assumed the balance between pressure gradients ( $g(d + \eta) \frac{\partial \eta}{\partial x_i}$ ) and each forcing term (indicated as subscripts; i.e.,  $RSG_x$  and  $BS_x$ ) (see Section 4.1.1).

#### 4.1.2.1. Alongshore Flow Dynamics Near the Shoreline

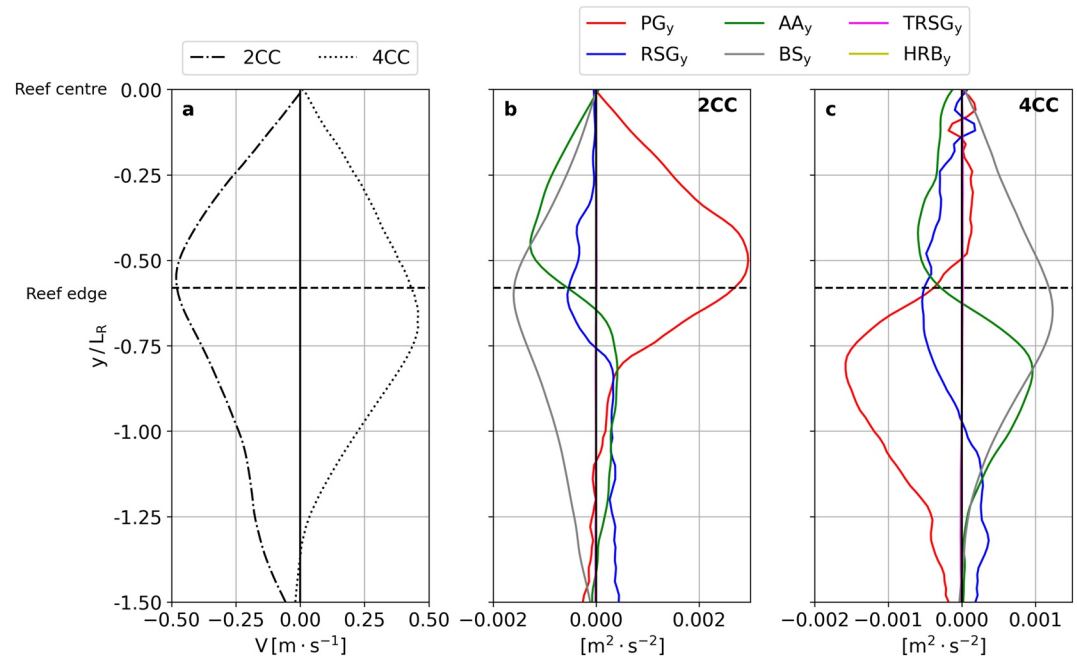
Here we conduct detailed analysis of the alongshore flow dynamics close to the shoreline, where the flow would more likely be able to drive sediment transport and coastal changes, and with which we can differentiate 2CC and 4CC cases. We calculated the cross-shore averaged values of the alongshore mass-flux velocities  $V$  (Figure 7a) and alongshore momentum terms from onshore (taken at  $x = -10$  m) to a depth  $d = 1$  m ( $x < 50$  m), for the



**Figure 6.** (a, b) Alongshore net forcing of radiation stress gradient  $RS_{G_y}$  and pressure gradient  $PG_y$  versus bottom stresses  $BS_y$  for (a) the representative two-cell circulation (2CC) and (b) four-cell circulation (4CC) cases. In all panels each momentum term was calculated over the reef lee ( $x < \sim 100$  m for the 2CC and  $x < \sim 250$  m 4CC) and from  $-200 < y < 200$  m (Figures 2 and 3), with the output from each grid cell shown (x-output and y-output grid sizes of 4 m). (c, d) Alongshore net forcing of  $RS_{G_y}$ ,  $PG_y$  and advective acceleration  $AA_y$  versus  $BS_y$  for the (c) 2CC and (d) 4CC cases. (e, f) Alongshore net forcing of  $RS_{G_y}$ ,  $PG_y$ ,  $AA_y$ , and turbulent Reynolds stresses gradients  $TRSG_y$  versus  $BS_y$  for the (e) 2CC and (f) 4CC cases. (g, h) Alongshore net forcing of  $RS_{G_y}$ ,  $PG_y$ ,  $AA_y$ ,  $TRSG_y$ , and hydrodynamic reaction at the bottom  $HRB_y$  versus  $BS_y$  for the (g) 2CC and (h) 4CC cases. The black line provides the linear fit between each forcing and  $BS_y$ , whereas the red lines represent the perfect closure that occurs in case a given sum of terms exactly match  $BS_y$ . The definition of each momentum term is given in Equation 1.

representative 2CC (Figure 7b) and 4CC cases (Figure 7c) (note that we only show the lower part of the domain  $y \leq 0$  m because results are symmetrical). The alongshore currents  $V$  for the representative 2CC had a similar parabolic pattern as  $BS_y$  (Figures 7a and 7b). For the 2CC (Figure 7b), the diverging  $PG_y$  are much larger in magnitude than converging  $RS_{G_y}$  in the lee of the reef. The advective accelerations  $AA_y$  oppose  $PG_y$  and are larger than  $RS_{G_y}$  in the reef lee. The gap between the location of maximum absolute  $V$  and  $PG_y$  reveals the role of  $RS_{G_y}$  and  $AA_y$  in shifting the location where the maximum  $V$  is observed (where  $RS_{G_y}$  peak) to about 15 m away from the reef. The net of  $PG_y$ ,  $RS_{G_y}$ , and  $AA_y$  is thus responsible for driving the converging  $BS_y$ .

The alongshore currents and bottom stresses of the 4CC case also display similar parabolic profiles (Figures 7a and 7c). Wave breaking over the exposed profile results in converging (negative)  $PG_y$  values that are always much larger than the also converging  $RS_{G_y}$  values ( $-200 < y < -115$  m) (Figure 7c). The net of  $PG_y$  and  $RS_{G_y}$  drives converging  $BS_y$ . In the lee of the reef,  $PG_y$  values are close to zero, which result from averaging the diverging (farther offshore) and converging (closer to the shoreline)  $PG_y$  (Figure 3i). Therefore, the local driver of the converging currents in the lee of the reef is the net of  $AA_y$  and  $RS_{G_y}$ . The fact that  $AA_y$  generally exceeds  $RS_{G_y}$  and become the largest momentum term (marker six in Figure 4d) shows that currents in the lee of the reef are predominantly driven by momentum transported from the exposed region. While the combined effect of  $PG_y$ ,  $RS_{G_y}$ , and  $AA_y$  is crucial for predicting the local drivers of  $BS_y$  and currents, the converging currents are mainly driven by the converging  $PG_y$  resulting from wave breaking over the exposed profile (marker seven in Figure 4d). The remaining terms



**Figure 7.** (a) Mean (over the cross-shore) of alongshore mass-flux velocity  $V$  as a function of alongshore location for the representative two-cell circulation (2CC, Figure 2) and four-cell circulation (4CC, Figure 3) cases. In all panels each momentum term was averaged from land until the still water depth  $d = 1$  m ( $x < 50$  m). (b, c) Mean (over the alongshore) of alongshore pressure gradient  $PG_y$ , radiation stress gradient  $RSG_y$ , advective acceleration  $AA_y$ , bottom stresses  $BS_y$ , turbulent Reynold stress gradient  $TRSG_y$ , and hydrodynamic reaction at the bottom  $HRB_y$ , for the (b) 2CC and (c) 4CC cases. Note that we only show the lower half ( $y < 0$  m) of the plot because results are symmetrical. The horizontal black line indicates the reef edge. The definition of each momentum term is given in Equation 1.

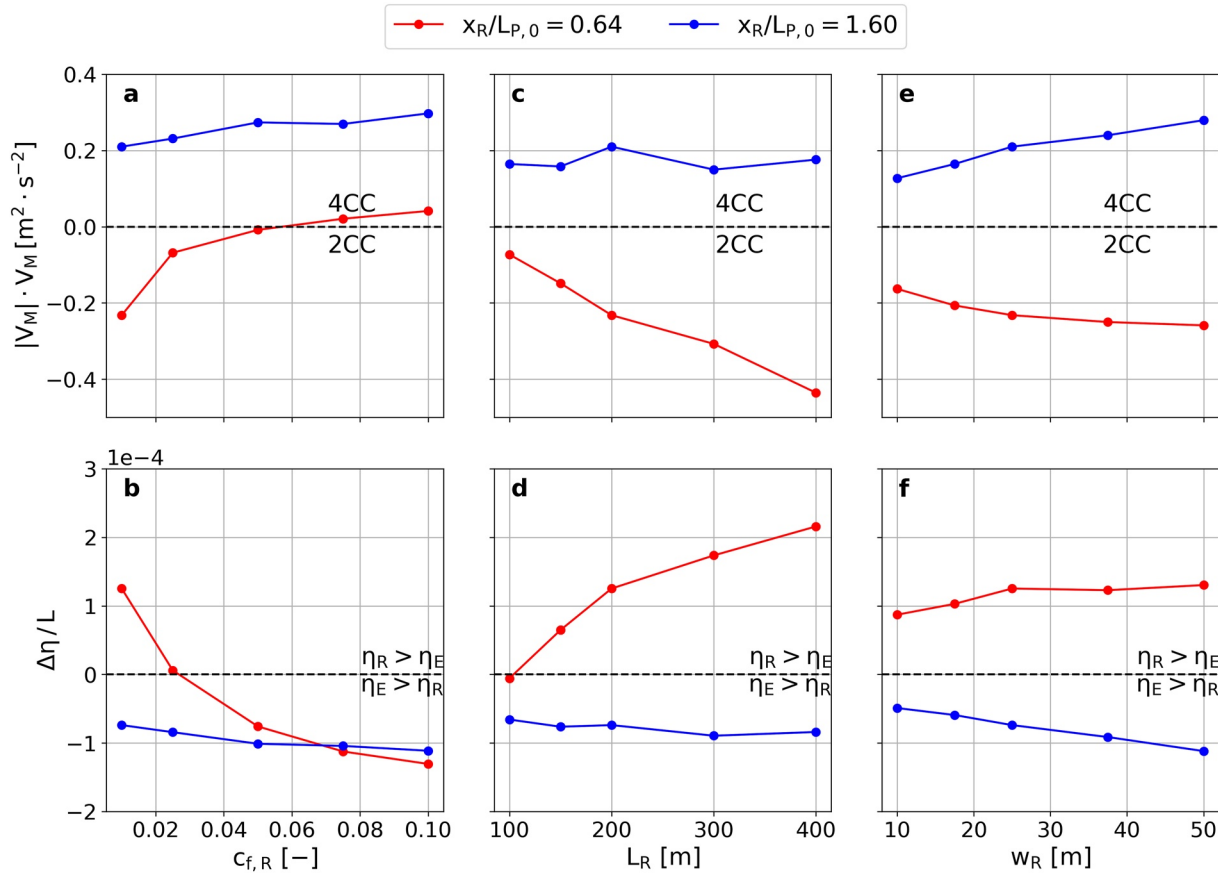
$TRSG_y$  and  $HRB_y$  had negligible contributions in both the 2CC and 4CC cases (Figures 7b and 7c). To conclude, despite the fundamental differences in their balances, the diverging and converging currents near the shoreline are ultimately primarily driven by the sign of  $PG_y$  near the shoreline. Accordingly, the differences between 2CC and 4CC cross-shore setup dynamics cause distinct alongshore flow patterns near the shoreline (see also Section 4.3).

## 4.2. Influence of Reef Properties and Beach Slope on Wave-Driven Flows

### 4.2.1. Reef Properties

Here we investigate how key reef properties, namely the reef friction coefficient  $c_{f,R}$ , reef distance to the shoreline  $x_R$ , reef base depth  $d_R$ , length  $L_R$ , and width  $w_R$ , influence the wave-driven flow patterns and relate these to the momentum dynamics. While a synthesis of how variations in these parameters influence the momentum dynamics and circulation patterns is presented here, a detailed set of figures showing how each parameter individually affects the flow dynamics can be found in the Supporting Information S1. The reef parameters  $c_{f,R}$  (0.01–0.1),  $L_R$  (100–400 m), and  $w_R$  (10–50 m) were varied one at a time while holding the other reef parameters constant at the default values for each parameter ( $c_{f,R} = 0.01$ ,  $L_R = 200$  m, and  $w_R = 25$  m). For each of these parameter variations, we ran two simulations with  $x_R = 100$  and 250 m because of anticipated major role of  $x_R$  in modifying flow patterns (da Silva et al., 2022; Ranasinghe et al., 2006, 2010). With the linear beach slopes assumed in this section,  $x_R$  and  $d_R$  are exactly related. For these runs, we used identical wave conditions and default reef geometries as the 2CC and 4CC representative cases (Section 4.1 and Table 2). We quantified the response of the alongshore flows near the shoreline to alongshore setup gradients as follows. To assess the strength of the alongshore currents, we computed the square of maximum velocities  $|V_M|V_M$  as an indicator for the circulation type and strength, based on the quadratic relationship that governs how bottom stresses  $\tau_{B,i}$  scale with the alongshore flow velocities (Equation 9). Given that in the lee of reefs the mean bottom shear stresses  $\langle \tau_{B,i} \rangle$  tend to be dominated by the contribution from mean currents (da Silva et al., 2022), using  $|V_M|V_M$  is a reasonable proxy for  $BS_y$ . The alongshore currents were first averaged from land to  $d = 1$  m ( $x < 50$  m), and then the maximum currents  $V_M$





**Figure 8.** Effect of varying (a, b) reef friction coefficient  $c_{f,R}$ , (c, d) reef length  $L_R$ , and (e, f) width  $w_R$  on (a, c, e) square of cross-shore averaged (near the shoreline) alongshore mass-flux velocity  $|V_M|V_M$  and (b, d, f) gradient between shoreline setup at the reef center and exposed beach  $\Delta\eta/L$ , where  $\Delta\eta = \eta_R - \eta_E$  and  $L = L_R/2 + x_R$ . The colors distinguish results for two different reef distances to the shoreline  $x_R$  normalized by the deep water peak wavelength  $L_{P,0}$ . The shoreline setup was calculated at the still water depth  $d = 0$  m (at  $x = 0$  m). The reef and exposed profile alongshore positions were taken at  $y = 0$  m and  $-L_R/2 - x_R$ , respectively. The alongshore mass-flux velocities  $V$  were first averaged from land until the still water depth  $d = 1$  m ( $x < 50$  m), then  $V_M$  was calculated where  $|V|$  is maximum over the lower ( $y < 0$  m) lee of the reef.

were calculated where their absolute values peaked. As we only included the lower part of the domain ( $y < 0$  m) because patterns are symmetric, negative and positive  $|V_M|V_M$  correspond to diverging (2CC) and converging (4CC) currents, respectively. Next, we calculated the gradient between the shoreline setup at the reef center and exposed beach  $\Delta\eta/L$  as a proxy for the overall alongshore pressure gradient  $PG_y$  driving the alongshore currents, where  $\Delta\eta = \eta_R - \eta_E$  and  $L = L_R/2 + x_R$ . The reference location for the exposed beach (given by the subscript  $E$ ) was taken at  $y = -L_R/2 - x_R$  (see Section 4.1.1). Note that changes in  $\Delta\eta/L$  are primarily driven by variations in  $\eta_R$  because, under constant wave forcing and with fixed beach slope,  $\eta_E$  is approximately a constant irrespective of the varied reef properties.

Increased reef roughness ( $c_{f,R}$ ) results in stronger converging flows  $|V_M|V_M$  (Figure 8a) and reduced setup in the lee of the reef ( $\eta_R$ ) (Figure 8b). Both the wave height and setup in the direct lee of the reef are reduced for larger  $c_{f,R}$  (Figures S1c and S1d in Supporting Information S1), which is explained by the increase in the magnitude of  $BS_x$  (Figure S1d in Supporting Information S1) that enhances the sink of momentum. As bottom stresses increase over the reef, the setup in the reef lee becomes increasingly lower than at the exposed beach and thus drives an increasingly converging  $PG_y$  (Figure S1d in Supporting Information S1), which ultimately leads to a switch from a 2CC to a 4CC for the  $x_R = 100$  m case (Figure 8a and Figure S1a in Supporting Information S1).

Changing the reef length  $L_R$  has two effects. For reefs close to the shoreline ( $x_R = 100$  m), increased  $\eta_R$  (Figure 8d) and stronger diverging flows (Figure 8c) occur for increased  $L_R$ . Despite the nearly similar wave dissipation over the reef (Figures S2c and S2d in Supporting Information S1), the setup in its lee is larger for longer reefs. The setup dynamics at the reef center for longer reefs approach the mean balance typically observed in alongshore

uniform beaches case (i.e., between  $RSG_x$  and  $PG_x$ ) due to the limited mass-flux atop the reef and decrease in magnitude of  $BS_x$  (Figure S2e in Supporting Information S1). Due to the increased path length for water behind a longer reef to flow back to the ocean, which results in increased integration of the bottom stress, the setup at the reef center becomes increasingly larger than at the exposed beach, which results in stronger diverging  $PG_y$ , that ultimately drive stronger diverging currents (Figures S2a and S2b in Supporting Information S1). For reefs situated in deeper waters ( $x_R = 250$  m),  $L_R$  had little effect on the alongshore circulation (Figure 8c, blue lines). Despite the increased setup immediately behind longer reefs (Figure S2d in Supporting Information S1), shorter reefs experience an increase in wave heights in the lee of the reef owing to alongshore fluxes of wave energy behind the reef (e.g., due to diffraction, Figure S2c in Supporting Information S1) that ultimately led to similar setup at the shoreline and no significant changes to the alongshore circulation.

Reefs with wider cross-shore widths  $w_R$  experience an increase in current magnitude, with stronger diverging and converging flows for reefs situated in shallower and deeper waters, respectively (Figures 8e and 8f, red lines). For reefs with  $x_R = 100$  m, wider reefs result in increased wave dissipation and increased setup in the lee (Figures S3c and S3d in Supporting Information S1). Despite the increase in  $BS_x$  (Figure S3e in Supporting Information S1), the setup is larger for wider shallow reefs because of greater dissipation by wave breaking. Consequently, larger diverging  $PG_y$  will drive stronger diverging currents near the shoreline (Figures S3a and S3b in Supporting Information S1). For reefs with  $x_R = 250$  m, wider reefs also experience increased wave dissipation and increased setup immediately behind the reef (Figures S3c and S3d in Supporting Information S1). Yet, larger setup occurs for narrower reefs because at the second break point close to the shoreline ( $x < 50$  m) wave heights are larger due to less dissipation occurring over the reef. Consequently, for  $x_R = 250$  m, an increase in the reef width  $w_R$  results in stronger converging  $PG_y$  that drive increased converging currents near the shoreline (Figures S3a and S3b in Supporting Information S1).

Overall, the four reef parameters  $x_R$ ,  $L_R$ ,  $w_R$ , and  $c_{f,R}$  influence the setup in the lee of the reef and are important for the alongshore flow dynamics. However, for the cases modeled,  $x_R$  and  $c_{f,R}$  were the only reef variables with the ability to modify the circulation pattern from a 2CC into a 4CC while keeping the remaining parameters constant, which suggests their key role in the flow dynamics.

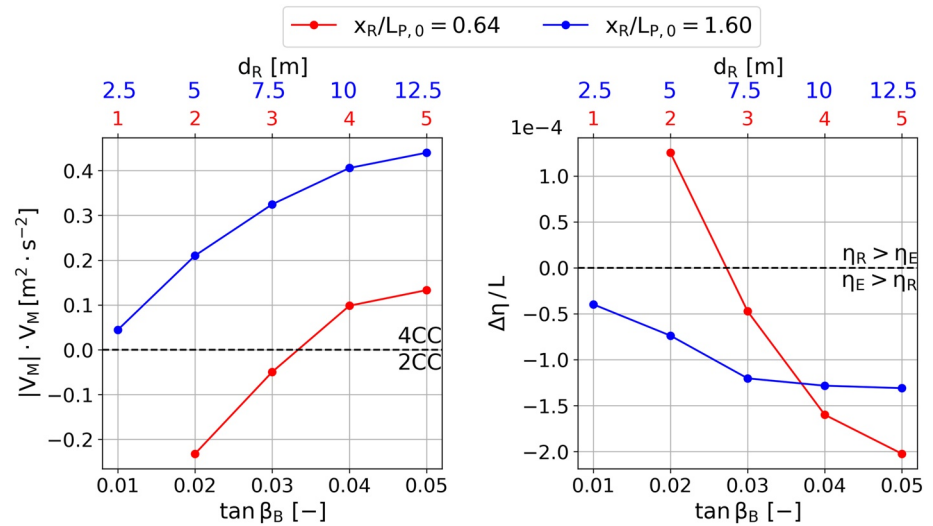
#### 4.2.2. Beach Slope

Here we evaluate the influence of the beach slope in influencing the flow dynamics. We analyzed how changing beach slopes influence  $|V_M|V_M$  and  $\Delta\eta/L$  (see Section 4.2.1). We varied the slope ( $\tan \beta_B = 0.01$ – $0.05$ ) while keeping both  $x_R$  and  $s_R$  constant, which resulted in varying  $d_R$  (2–12.5 m). For each slope variation, we ran two simulations with  $x_R = 100$  and 250 m. All other parameters were fixed and similar to the 2CC and 4CC representative cases (see Section 4.1). To calculate  $|V_M|V_M$ , the alongshore currents were first averaged from land to  $d = 1$  m (unlike in previous sections, a fixed depth and varying slopes result in  $x < 1/\tan \beta_B$ ), and then the maximum currents  $V_M$  are calculated where the absolute values peaked.

The results show that steeper slopes (or larger  $\tan \beta_B$ ) result in increased  $\eta_E$  (e.g., Raubenheimer et al., 2001) owing to larger  $RSG_x$ . The changes in  $\eta_E$  in response to varying slope generally influence  $\Delta\eta/L$  more than the changes in  $\eta_R$  (not shown). Steeper slopes yield increased  $\eta_E$  and reduced  $\Delta\eta/L$  (Figure 9b), which are consistent with stronger converging  $PG_y$  (Figure S4b in Supporting Information S1) that drive increased converging currents (Figure 9b and Figure S4a in Supporting Information S1). Increased  $x_R$  (or  $d_R$ , see top  $x$  axis of Figure 9) at a given slope results in stronger converging flows (Figure 8a and Figure S4a in Supporting Information S1). While for most cases this response is due to the reduction in  $\Delta\eta/L$ , for the steepest slopes ( $\tan \beta_B > 0.03$ ) both  $\Delta\eta/L$  and  $PG_y$  are lower for reefs situated with lower  $x_R$ . The fact that lower  $\Delta\eta/L$  yields lower converging currents can be explained by the larger area available for the development of alongshore currents for cases with larger  $x_R$  (i.e., with less influence of the diverging currents). Overall, these results indicate that the beach slope and the dependent parameters  $x_R$  and  $d_R$  have a major influence in the setup and alongshore circulation dynamics. For a given set of wave conditions and reef parameters, a change in slope can modify the circulation pattern from a 2CC into a 4CC, which makes it a key parameter in the alongshore flow dynamics.

#### 4.3. Synthesis of Drivers of Reef Circulation Patterns Subject to Variable Hydrodynamic Forcing

In this section, we collectively consider the results from the broad range of simulations together to identify the most significant features of the overall flow dynamics that differentiate the 2CC and 4CC patterns generally. Unlike in previous sections, where we studied how reef parameters and slopes individually affect the momentum dynamics, here we synthesize and analyze a comprehensive set of simulations including permutations of  $H_{S,0}$ ,



**Figure 9.** Effect of varying beach slope ( $\tan \beta_B$ ; where steep/mild slopes are indicated by large/small  $\tan \beta_B$  values, respectively) on (a) square of cross-shore averaged (near the shoreline) alongshore mass-flux velocity  $|V_M|V_M$  and (b) gradient between shoreline setup at the reef center and exposed beach  $\Delta\eta/L$ , where  $\Delta\eta = \eta_R - \eta_E$  and  $L = L_R/2 + x_R$ . The colors distinguish results for two different reef distances to the shoreline  $x_R$  normalized by the deep water peak wavelength  $L_{P,0}$ . The upper  $x$  axis indicates the reef base depth  $d_R$  for each  $x_R$ . The shoreline setup was calculated at the still water depth  $d = 0$  m (at  $x = 0$  m). The reef and exposed profile alongshore positions were taken at  $y = 0$  m and  $-L_R/2 - x_R$ , respectively. The alongshore mass-flux velocities  $V$  were first averaged from land until the still water depth  $d = 1$  m ( $x < 1/\tan \beta_B$ ), then  $V_M$  was calculated where  $|V|$  is maximum over the lower ( $y < 0$  m) lee of the reef.

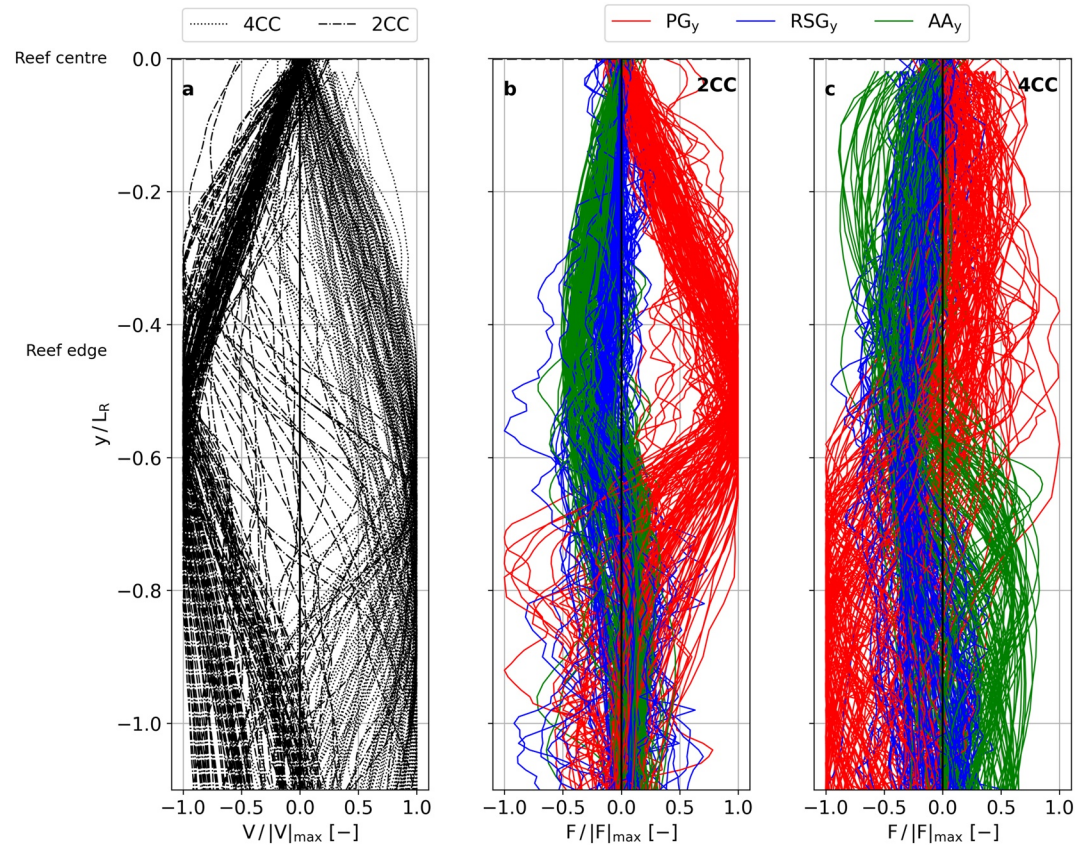
$T_P$ ,  $s_R$ ,  $x_R$ ,  $d_R$ ,  $L_R$  and  $w_R$  across our parameter space (Table 2) while keeping a fixed reef friction coefficient  $c_{f,R} = 0.01$  and beach slope  $\tan \beta_B = 1/50$  due to computational constraints.

### 4.3.1. Alongshore Drivers

Here we use the full database of simulations to assess common features of the alongshore variation of alongshore mass-flux velocities and momentum terms. First, we averaged  $V$ ,  $PG_y$ ,  $RSG_y$ , and  $AA_y$  close to the shoreline (same region as before, see Section 4.1); next, we normalized each by the maximum values of each simulation  $|V|_{max}$  and  $|F|_{max}$ , which were calculated where their absolute values peak. The momentum terms are normalized by  $|F|_{max}$  based on the maximum forcing term value among  $PG_y$ ,  $RSG_y$ , and  $AA_y$ . We grouped simulations into 2CC (Figure 10b) and 4CC (Figure 10c) classes based on the direction of the maximum absolute alongshore currents occurring in the lee of the reef (in the lower part of the domain 2CC and 4CC occur for negative and positive currents, respectively). The normalized alongshore currents and momentum terms patterns display similar alongshore variations as was observed for the representative 2CC and 4CC (Figure 10). Overall, this analysis indicates the magnitude and structure of the alongshore pressure gradients are the primary factors determining whether the flow is 2CC or 4CC. Next, we analyzed how the parameter space considered influences the setup profiles both over the reef center and at the exposed area by computing the correlation between  $\Delta\eta/L$  and  $|V_M|V_M$  (see Section 4.2 for details). Diverging (red in Figure 11) and converging (blue) currents generally develop for  $\eta_R > \eta_E$  and  $\eta_R < \eta_E$ , respectively. For diverging currents,  $|V_M|V_M$  highly correlates with  $\Delta\eta/L$  (red line,  $R^2 = 0.93$ ), whereas for converging currents a moderate correlation is observed (blue line,  $R^2 = 0.43$ ). The stronger correlation for diverging currents is consistent with the well-defined alongshore momentum balance patterns and stronger dominance of  $PG_y$  for the 2CC cases (Figure 10b) than for the 4CC cases (Figure 10c). Overall, these results indicate that knowledge of the shoreline setup onshore of the reef center and at the exposed profile can be used to reasonably determine whether a 2CC or 4CC will occur.

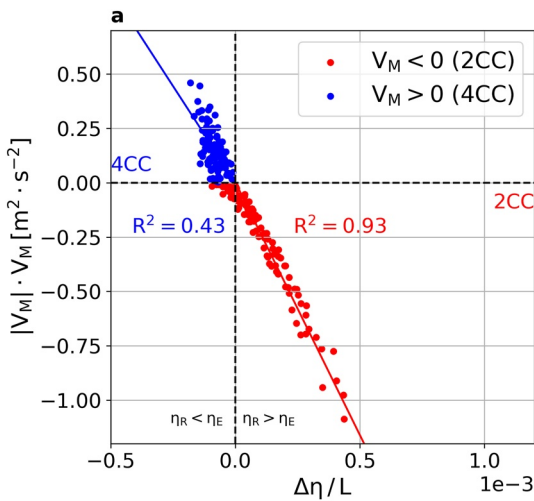
### 4.3.2. Setup Dynamics

Due to the importance of the magnitude of setup generation behind the reef to the alongshore flow dynamics, the study of the cross-shore setup balance allows us to identify the physical processes that create the 2CC and 4CC patterns. To understand the role of different cross-shore momentum terms in driving the shoreline setup at the reef center and exposed beach, we reconstructed the setup at these two locations first with  $RSG_x$  ( $\eta_{RSG_x}^{recon}$ ) and last with  $RSG_x + BS_x$  ( $\eta_{RSG_x+BS_x}^{recon}$ ; the same approach used in Section 4.1.1). The setup generation by wave breaking



**Figure 10.** (a) Mean (over the cross-shore) of alongshore mass-flux velocity  $V$  normalized by absolute value of maximum  $|V|_{max}$  as a function of alongshore location normalized by the reef length  $y/L_R$  for a range of modeling cases (see text for model input files). (b, c) Mean (over the cross-shore) of alongshore pressure gradient  $PG_y$ , radiation stress gradient  $RSG_y$ , and advective acceleration  $AA_y$ , each normalized by the maximum absolute forcing term  $|F|_{max}$ . Note that we only show the lower half ( $y < 0$  m) of the plot because results are symmetrical. The horizontal black line indicates the reef edge. In all panels velocities and momentum terms were averaged from land until the still water depth  $d = 1$  m ( $x < 50$  m). The classification into 2CC and 4CC in (a) was based on the direction of the maximum absolute alongshore currents occurring in the lee of the reef (i.e.,  $\sim -0.5 \leq y/L_R \leq 0$ ). The definition of each momentum term is given in Equation 1.

( $\eta_{R,RSG_x}^{recon}$ , i.e., predicted only by  $RSG_x$ ) is highly correlated with the actual setup behind the reef  $\eta_R$  ( $R^2 = 0.76$ ); however  $\eta_R$  is on average overestimated ( $RB = 36\%$ , where  $RB$  stands for relative bias, Figure 12a). The reconstructed setup with  $RSG_x + BS_x$  ( $\eta_{R,RSG_x+BF_x}^{recon}$ ) yield accurate setup estimates (Figures 12a and 12b), which indicates that including  $BS_x$  is essential for correctly calculating  $\eta_R$  (e.g., Figure 5b). The seaward  $BS_x$  associated with the onshore flows over the reef (e.g., Figures 5c and 5d) reduces the wave setup. At the exposed beach, the setup generation by wave breaking ( $\eta_{E,RSG_x}^{recon}$ ) accurately reproduces the setup ( $RB = -6\%$ , Figure 12c). The setup prediction is increased with  $RSG_x + BS_x$  ( $\eta_{E,RSG_x+BF_x}^{recon}$ ) and the negative bias is removed ( $RB = 1\%$ ), consistent with the shoreward  $BF_x$  associated with undertow near the shoreline enhancing wave setup (e.g., Figures 5c and 5d). Next, we calculated the reconstructed and actual difference between the setup at the reef and exposed beach  $\Delta\eta$  with the same forcing terms (Figures 12e and 12f). Despite the high correlation between the  $\eta_{RSG_x}^{recon}$  at the two locations, the reconstructed  $\Delta\eta$  with  $RSG_x$  ( $\Delta\eta_{RSG_x}^{recon}$ ) has poor correlation ( $R^2 = 0.18$ ) and a bias of  $\sim -200\%$  (Figure 12e). As  $\Delta\eta_{RSG_x}^{recon}$  results in nearly always positive values (i.e.,  $\eta_{R,RSG_x}^{recon} > \eta_{E,RSG_x}^{recon}$ ), the alongshore pressure gradients based on  $\eta_{RSG_x}^{recon}$  would generally result in diverging currents. The reconstructed  $\Delta\eta$  with  $RSG_x + BS_x$  ( $\Delta\eta_{RSG_x+BF_x}^{recon}$ ) provides increased correlation ( $R^2 = 0.80$ ) and much reduced bias ( $RB = -25\%$ , Figure 12f), which indicates that the alongshore pressure gradients predicted by  $\eta_{RSG_x+BF_x}^{recon}$  would provide reasonable estimates of the actual forcing that drives 2CC and 4CC systems. The perfect representation of  $\Delta\eta$  (i.e., with  $R^2 \sim 1$ ) requires reconstructing the setup by also including the advective acceleration  $AA_x$  and turbulent Reynolds stress gradients  $TRSG_x$  (not shown).



**Figure 11.** Square of cross-shore averaged (near the shoreline) alongshore mass-flux velocity  $|V_M|V_M$  versus gradient between shoreline setup at the reef center and exposed beach  $\Delta\eta/L$ , where  $\Delta\eta = \eta_R - \eta_E$  and  $L = L_R/2 + x_R$ , for a range of modeling cases (see text for model input files). The solid blue and red lines indicate the linear fit between  $|V_M|V_M$  and  $\Delta\eta/L$  for converging ( $V_M > 0 \text{ m s}^{-1}$ ) and diverging ( $V_M < 0 \text{ m s}^{-1}$ ) currents, respectively. The shoreline setup was calculated at the still water depth  $d = 0 \text{ m}$  (at  $x = 0 \text{ m}$ ). The reef and exposed profile alongshore positions were taken at  $y = 0 \text{ m}$  and  $-L_R/2 - x_R$ , respectively. The alongshore mass-flux velocities  $V$  are averaged from land until the still water depth  $d = 1 \text{ m}$  ( $x < 50 \text{ m}$ ), then  $V_M$  is calculated where  $|V|$  is maximum over the lower ( $y < 0 \text{ m}$ ) lee of the reef.

## 5. Discussion

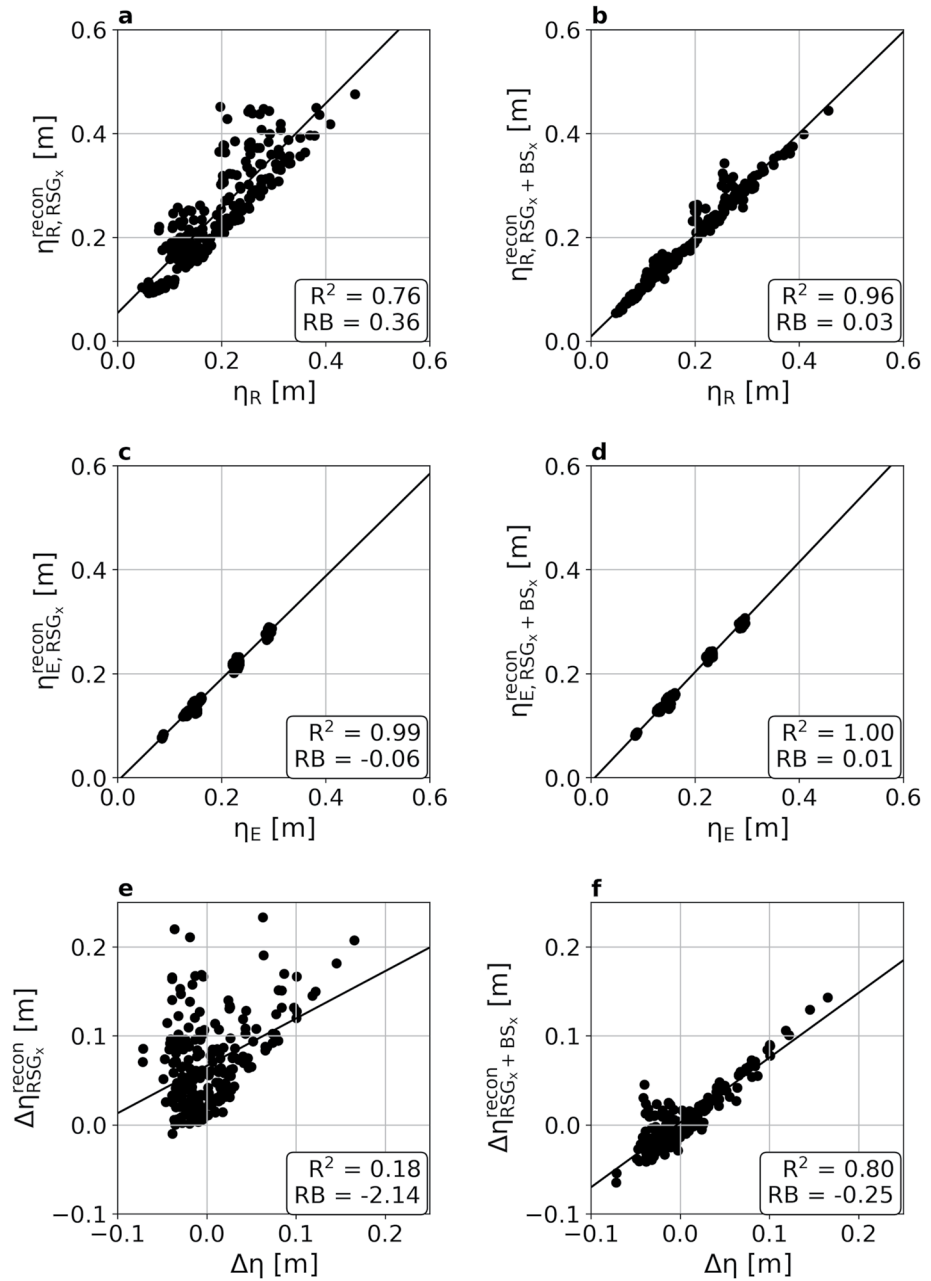
### 5.1. Circulation Dynamics

Through an analysis of momentum balances that govern the wave-driven circulation patterns in the lee of nearshore reef systems, our study demonstrated that the occurrence of 2CC and 4CC flow patterns are determined by distinct momentum balances that are established in different areas in the lee of the reef. The diverging and converging currents originate from wave breaking over the reef and at the adjacent exposed profile, respectively. The breaking over the reef results in diverging pressure gradients  $PG_y$  and converging radiation stress gradients  $RSg_y$ , and because  $|PG_y| > |RSg_y|$  diverging currents emerge directly in the lee of the reefs both for 2CC and 4CC. For the 2CC, this diverging current pattern extends to the shoreline. For the 4CC, although the area directly in the lee of the reef is also characterized by diverging currents, the wave breaking over the exposed profile at a distance from the shoreline results in converging  $PG_y$  and  $RSg_y$  that together drive converging currents onshore of the diverging currents up to the shoreline. Although the relative importance of each momentum term governing local balances varies and their accurate description requires most terms, the overall alongshore flow patterns (i.e., 2CC or 4CC) are largely driven by  $PG_y$ , which confirms the hypothesis made in previous studies (e.g., Ranasinghe et al., 2006; Villani et al., 2012). Given the critical role that the alongshore pressure gradient  $PG_y$  plays in describing the magnitude and direction of alongshore flows, the difference between the setup profiles over the reef center and at the adjacent exposed beach was found to correlate with alongshore currents near the shoreline. The strong influence of reef length on the shoreline setup demonstrates that alongshore wave propagation (e.g., due to diffraction) and alongshore currents need to be considered for an accurate description of the setup dynamics.

The key aspects of the overall flow dynamics in the lee of nearshore reef systems can be explained by the cross-shore setup dynamics over the reef-fronted and exposed beaches. In general, shoreline setup at the reef center that is lower or larger than at the exposed beach will result in converging and diverging currents, respectively. The cross-shore momentum balance analysis indicates that the shoreline setup mainly results from the forces associated with the wave breaking and onshore flows over the reef. Through the seaward bottom stresses (a response to the onshore flows over the reef), reef roughness can substantially reduce the setup generation by wave breaking. The setup that would be predicted by considering radiation stress gradients alone (i.e., neglecting bottom stresses) results in larger shoreline setup at the reef center than at the exposed beach, which would result in diverging pressure gradients that would drive diverging currents for nearly all cases. Consequently, including an accurate representation of the bottom stresses is fundamental for describing the dynamics of 2CC or 4CC patterns.

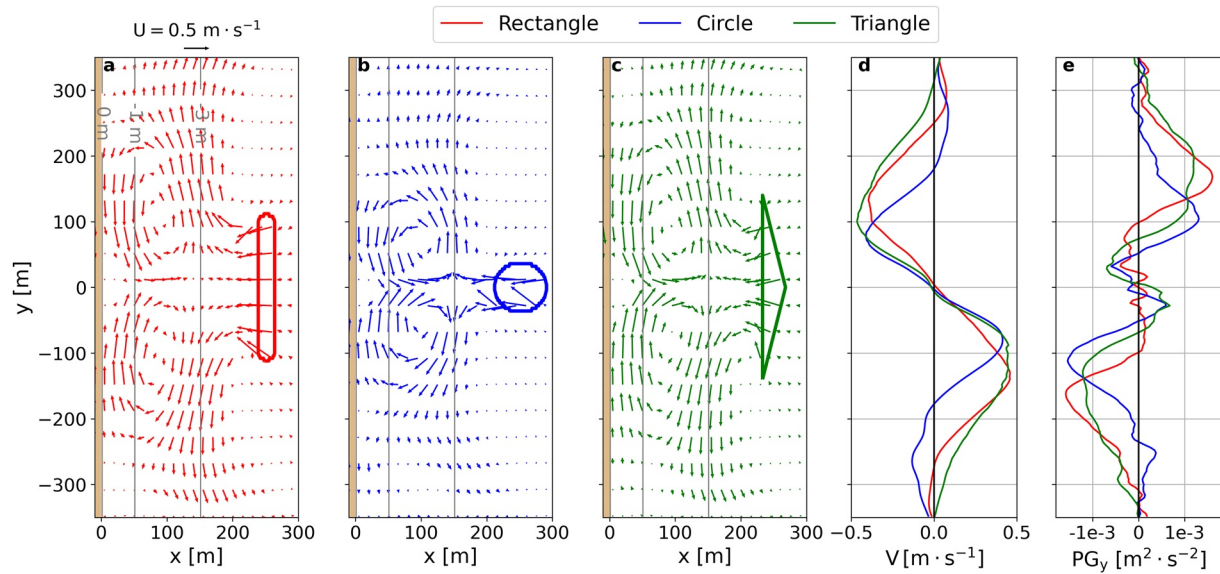
Reefs can be present in nature with a wide range of different roughness properties. Our study showed that variations of the reef friction coefficient substantially influence the alongshore flow dynamics. Rougher reefs are more prone to develop 4CC owing to decreased shoreline setup at the reef-fronted beach. We used a range of  $c_{f,R}$  based on mean currents (Rosman & Hench, 2011) to represent bottom shear stresses. However, in SWASH bottom stresses are calculated based on the instantaneous flows, independent of whether they are driven by mean currents or wave-driven oscillatory flows, which does account for how the relationship between bottom stresses and near-bed flows that depends on the frequency of the motion (Lowe et al., 2005). Therefore, an optimal  $c_{f,R}$  is likely to be different than that for mean flows alone. Limited studies to our knowledge have attempted to quantify reef friction coefficients  $c_{f,R}$  based on instantaneous velocities (e.g., Buckley et al., 2016), and thus this is suggested as a potential area of future research as to provide drag coefficients relevant to combined mean and oscillatory flows (at intrawave timescales) across a range of sea floor environments. This would provide greater confidence in the selection of drag coefficients, particularly given their importance in determining the flow dynamics demonstrated here.

Although an extensive parameter space of reef properties was considered in these simulations, the effect of variable frictional properties of the surrounding beach were not considered (the friction coefficient of beach,



**Figure 12.** Comparison between reconstructed  $\eta^{recon}$  and modeled shoreline setup  $\eta$  at the (a, b) reef center ( $\eta_R$ , calculated at  $y = 0$  m) and (c, d) exposed beach ( $\eta_E$ , calculated at  $y = -L_R/2 - x_R$ ), and (e, f) reconstructed  $\Delta\eta^{recon} = \eta_R^{recon} - \eta_E^{recon}$  and modeled  $\Delta\eta = \eta_R - \eta_E$  for a range of modeling cases (each dot corresponds to a single run; see text for model input files). In all panels  $RB$  indicates the relative bias. The shoreline setup was calculated at the still water depth  $d = 0$  m (at  $x = 0$  m). To reconstruct the shoreline setup, we assumed the balance between pressure gradients ( $g(d + \eta)\frac{\partial \eta}{\partial x}$ ) and each forcing term (indicated as subscripts; (a, c, e)  $RSG_x$ ; (b, d, f)  $RSG_x + BS_x$ , where  $RSG_x$  and  $BS_x$  indicate the cross-shore radiation stress gradients and mean bottom stresses, respectively; see Section 4.1.1).

$c_{f,B} = 0.005$ , consistent with sand, was held constant across all simulations). Accordingly, the changes to the alongshore pressure gradients near the shoreline were mainly driven by the variations of the shoreline setup at the reef-fronted beach, rather than the setup at the exposed beach. The beaches surrounding reefs can vary in nature, which can influence the flow dynamics. In case the surrounding beaches have rougher beds (e.g., rocky beds or with bed forms), increased  $c_{f,B}$  would likely increase the shoreline setup at the adjacent beach through the increased shoreward bottom stresses reacting to the undertow near the shoreline. As a result, rougher surrounding



**Figure 13.** Map views of (a–c) mass-flux velocities  $U_i$ , mean (over the cross-shore) of (d) alongshore currents  $V$  and (e) alongshore pressure gradients  $PG_y$ , resulting from waves interacting with rectangular (red), circular (blue), and triangular (green) shaped reefs with similar areas. The gray and red/blue/green lines give the depth and reef contours, respectively. Alongshore velocities and pressure gradients terms were averaged from land until the still water depth  $d = 1 \text{ m}$  ( $x < 50 \text{ m}$ ). The input conditions were similar to the representative four-cell circulation (4CC, Figure 3), except for the reef shape.

beaches would have further increased the likelihood of developing a 4CC pattern because of stronger converging alongshore pressure gradients near the shoreline.

## 5.2. Influence of Reef Shape

The geometry of natural reefs can vary substantially which makes their idealized representation challenging. For simplicity, we considered rectangular-shaped reefs in our study. To evaluate whether the wave-driven flows are sensitive to varying reef shapes, we conducted exploratory modeling with two alternative crest shapes, circular, and triangular (isosceles) and compared them with the rectangular reefs while keeping the location and crest area constant for every reef shape. We used the same wave conditions and remaining reef parameters as the representative 4CC case (see Section 4.1). Despite some local differences in the flow patterns, the general aspects of the wave-driven circulation are similar for rectangular, circular, and triangular-shaped reefs (Figures 13a–13c). Because the shapes had little influence on the alongshore pressure gradients (Figure 13e), which mainly drive the alongshore currents, the alongshore currents near the shoreline were similar (Figure 13d). Consequently, these results suggest that using different reef geometrical shapes would likely have limited influence on the overall alongshore flow dynamics.

## 5.3. Implications for Shoreline Processes

The interactions between waves and nearshore reefs result in 2CC and 4CC patterns. The alongshore gradients in the sediment transport associated with diverging (2CC) and converging (4CC) currents near the shoreline would likely drive shoreline erosion and accretion, respectively (da Silva et al., 2022; Ranasinghe et al., 2006). Among the variety of reef properties, the reef distance to shoreline  $x_R$ , reef friction coefficient  $c_{f,R}$ , and beach slope  $\tan \beta_B$  were found to have the most significant influence on the flow dynamics. Rougher reefs located farther away from the shoreline (or deeper) in steeper beaches are more prone to develop 4CC patterns generally because of reduced setup at the reef center that yields converging pressure gradients. Accordingly, these reef systems would more likely experience accreted shorelines behind a reef.

Reefs are present in a variety of coastal environments that experience a range of wave and water level conditions. As this forcing varies over time, it is possible for these circulation patterns behind natural reefs to substantially change during different periods (including alternating between 2CC and 4CC patterns) that may result in cycli-

cal patterns of shoreline erosion and accretion in the lee of reefs. With most studies of the shoreline responses to reefs having focused on the equilibrium shoreline response as a function of reef geometry (e.g., Black & Andrews, 2001), the dynamic nature of the shoreline position in the lee of small reefs remains largely unknown, with only a few exceptions (Duarte Nemes et al., 2019; Segura et al., 2018). For example, a study of a nearshore rocky reef system at Garden Island, Western Australia, found that the size of the salient (i.e., a seaward extension of the shoreline) behind reefs and at the adjacent embayment oscillated seasonally as a function of water levels and wave heights (Segura et al., 2018). While a detailed description of sediment transport patterns is required for better appraisal of the physical mechanisms driving the shoreline dynamics, this study may help to explain the cyclical behavior of the shoreline variability behind the reefs in response to seasonal variations in offshore sea level and wave conditions at that site. Results from the present study can explain some of the mechanisms by which temporal variations in hydrodynamic forcing conditions may influence the flow dynamics of nearshore reef systems and shoreline morphology. Larger oscillations of water levels, such as generated by large tidal ranges or seasonal sea level variations, would result in oscillating reef crest submergence. During periods with lower water levels, the wave breaking over reefs would yield 2CC or 4CC depending on the reef geometry. Reefs may become emergent and result in 4CC (e.g., da Silva et al., 2022; Suh & Dalrymple, 1987) and likely accretion in their lee. Increased water levels, which in the long-term may also be caused by sea level rise, could eventually inhibit or reduce depth-limited breaking over the reefs. In this case, the main hydraulic function of reefs would be to promote wave refraction, and the resulting alongshore-varying wavefield would yield alongshore-varying circulation forcing (e.g., Hansen et al., 2015). However, the decrease in the forcing may cause reduction of the strength of the alongshore currents (e.g., da Silva et al., 2022) and yield reduced sediment transport. The weakening of the mean flows that previously contributed to maintain erosion or accretion (e.g., salient) behind reefs would result in straightening of shorelines.

## 6. Conclusions

We conducted a detailed analysis of the momentum balances responsible for establishing 2CC and 4CC patterns in the lee of small nearshore reefs using a phase-resolved numerical model (SWASH) that incorporated a wide range of wave and water level conditions, reef properties, and beach slopes. The spatial variability of the pressure gradients and radiation stress gradients were responsible for driving the mean currents, which were countered by mean bottom stresses and advective accelerations. While the local balances significantly vary, the alongshore currents observed in 2CC and 4CC systems mainly resulted from diverging and converging alongshore pressure gradients that originate from the wave breaking over the reef and exposed profile, respectively. Rougher reefs situated in deeper waters (and farther away from the shoreline) were more prone to experience lower shoreline setup in their lees, which increases the likelihood of developing alongshore pressure gradients directed toward the reef center that drive 4CC systems. Through analysis of the cross-shore setup dynamics, we found that the setup on the reef profile developed in response to the net contribution of radiation stress gradients generated by wave breaking and mean bottom stresses associated with the strong onshore flows over the reefs. For 2CC cases, the reduction of setup by seaward bottom stresses was generally limited, which resulted in shoreline setup at the reef center that was larger than at the exposed beach. For the 4CC cases, the reduction of the setup by seaward bottom stresses resulted in shoreline setup at the exposed beach being larger than at the reef center.

## Data Availability Statement

The numerical model input files for the representative two-cell and four-cell circulation cases are publicly available at <https://doi.org/10.26182/1h84-7268>.

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