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# 1 Simulating waves and their interactions with a restrained ship using a 2 non-hydrostatic wave-flow model

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## 6 Abstract

7 This paper presents a numerical model to simulate the evolution of waves and their interactions with a  
8 restrained ship that is moored in coastal waters. The model aims to be applicable at the scale of a harbour  
9 or coastal region, while accounting for the key physical processes that determine the hydrodynamic loads  
10 on the ship. Its methodology is based on the non-hydrostatic wave-flow model SWASH, which provides  
11 an efficient tool to simulate the nonlinear dynamics that govern the nearshore wave field. In this work,  
12 we propose a new numerical algorithm that accounts for the presence of a non-moving floating body, to  
13 resolve the wave impact on a restrained ship. The model is validated through comparisons with an analytic  
14 solution, a numerical solution, and two laboratory campaigns. The results of the model-data comparison  
15 demonstrate that the model captures the scattering of waves by a restrained body. Furthermore, it gives a  
16 reasonable prediction of the hydrodynamic loads that act on a restrained container ship for a range of wave  
17 conditions. Importantly, the model captures these dynamics efficiently, which demonstrates that it retains  
18 this favourable property of the non-hydrostatic approach when a floating body is included. The findings of  
19 this study suggest that the model provides a promising new alternative to simulate the nonlinear evolution  
of waves and their impact on a restrained ship at the scale of a realistic harbour or coastal region.

20 *Keywords:* moored ship, wave-ship interactions, wave scattering, hydrodynamic loads, non-hydrostatic,  
21 SWASH

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## 22 1. Introduction

23 A ship that is moored in a harbour or coastal region is subject to the local wave field, which may cause  
24 the moored ship to move. When the motions of the ship become too large, ship operations may need to be  
25 terminated, resulting in undesired economic losses. Therefore, an accurate prediction of the local wave field,  
26 the hydrodynamic loads acting on the ship (the forces and moments), and the resulting ship motions are of  
27 vital importance to ensure safe and continuous operations of a moored ship.

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28 Numerical models provide a valuable tool to predict the wave-induced response of a moored ship. Such  
29 a model should account for the interactions between the local wave field and the ship, such as the scattering  
30 of the waves by the ship, and the radiation of waves due to the ship motions (e.g., Newman, 1977). Further-  
31 more, the model should account for the complex nearshore evolution of the waves as they propagate from  
32 relatively deep water to shallower water depths. This includes processes like shoaling, refraction, diffraction,  
33 wave breaking, and nonlinear interactions. The latter is especially relevant in the nearshore, as nonlinear  
34 wave effects like infragravity waves can cause significant ship motions (e.g., González-Marco et al., 2008;  
35 Sakakibara and Kubo, 2008; López and Iglesias, 2014). This highlights that an accurate description of the  
36 local nonlinear wave field is required when predicting the wave-induced response of a ship that is moored in  
37 coastal waters.

38 A variety of model techniques have been developed to simulate the interactions between waves and ships  
39 (see Bertram, 2012, for a concise overview). The first efforts to solve these interactions were based on  
40 potential flow theory (e.g., Korvin-Kroukovsky and Jacobs, 1957; Hess and Smith, 1962), in which the flow  
41 is assumed to be irrotational and inviscid. In this context, the Boundary Element Method (BEM) has been a  
42 popular method to solve the wave-ship interactions. Such models, which are also known as panel models, are  
43 applied in both offshore (e.g., Huijsmans et al., 2001; Newman, 2005; Zhao et al., 2011) and coastal waters  
44 (e.g., Van Oortmerssen, 1976; You and Faltinsen, 2015; Xiong et al., 2015) to predict the wave impact on  
45 floating bodies. More recently, potential flow models based on the Finite Element Method (FEM) have  
46 been developed to simulate similar interactions (e.g., Yan and Ma, 2007; Ma and Yan, 2009). Potential flow  
47 models based on the BEM and FEM share that they are not designed to simulate the evolution of waves at  
48 the scales of a coastal or harbour region. Consequently, they require information concerning the local wave  
49 field to predict the ship response based on an offshore wave climate

50 Furthermore, the assumption of potential flow is violated in the case of large wave impacts and signif-  
51 icant ship motions (e.g., ship capsizing). In such extreme conditions, an alternative approach is desired  
52 to adequately simulate the ship response. With the increase of computational powers, various detailed  
53 Computational Fluid Dynamics (CFD) models have been developed that can resolve the turbulent flow  
54 field in the vicinity of a floating body. Examples include models that are based on the Reynolds-averaged  
55 Navier-Stokes (RANS) equations (e.g., Hadžić et al., 2005; Lin, 2007; Stern et al., 2013), and models based  
56 on the Smoothed Particle Hydrodynamics (SPH) method (e.g., Bouscasse et al., 2013; Ren et al., 2015).  
57 For instance, RANS models have been used to simulate the seakeeping of ships, including the turbulent  
58 wake of the ship and rotating propellers (e.g., Wilson et al., 2006; Mofidi and Carrica, 2014). However,  
59 computational limitations restrict the application of such highly detailed models to relatively small scales,  
60 spanning only a few wave lengths and wave periods.

61 To simulate both the evolution of waves and their interactions with ships, several authors combined a  
62 wave model with a model that accounts for the wave-ship interactions (e.g., Bingham, 2000; Jiang et al., 2002;

63 Van der Molen et al., 2006; Van der Molen and Wenneker, 2008; Dobrochinski, 2014). To our knowledge,  
64 the most advanced methodology that can solve this complex problem combined a phase resolving wave  
65 model (i.e., a Boussinesq or a non-hydrostatic wave model) with a panel model (Bingham, 2000; Van der  
66 Molen and Wenneker, 2008; Dobrochinski, 2014). In this approach, the wave model is first used to simulate  
67 the evolution of the waves as they propagate in coastal waters. The wave model does not account for  
68 the presence of the ship, and the computed wave field represents the waves that are not disturbed by the  
69 ship. Next, a panel model based on linear potential theory is used to compute the interactions between  
70 this undisturbed wave field and the ship. The advantage of such a coupled wave-panel model is that it  
71 combines a wave model that can resolve the nonlinear wave evolution from deep to shallow water at the  
72 scale of a harbour or coastal region, with a panel model that includes a detailed schematisation of the ship's  
73 hull to determine the wave-induced response. However, the assumption of linear potential flow restricts this  
74 approach to relatively mild wave conditions, when the wave non-linearity is small (i.e.,  $a/d \ll 1$  in shallow  
75 water, where  $a$  is the wave amplitude and  $d$  is the still water depth, Bingham, 2000). Moreover, the coupling  
76 of two models complicates the usage and maintenance of this methodology.

77 In this work, we pursue an alternative approach to simulate the evolution of waves and their impact  
78 on a ship that is moored in coastal waters. Our ultimate goal is to develop a single model to simulate  
79 the wave-induced response of a moored ship based on an offshore wave climate. The model aims to be  
80 applicable at the scales of a harbour or coastal region, while accounting for the relevant processes on both  
81 relatively large scale (the nonlinear wave transformation over a complex bathymetry) and on small scale (the  
82 wave-ship interactions). Our approach is based on the non-hydrostatic wave-flow model SWASH<sup>1</sup>. Recent  
83 studies have shown that non-hydrostatic wave-flow models like SWASH are capable of resolving the complex  
84 evolution of waves over sloping bottoms (e.g., Yamazaki et al., 2009; Ma et al., 2012; Cui et al., 2012). This  
85 includes the nonlinear wave dynamics in the surf zone (Smit et al., 2013, 2014), and the nearshore evolution  
86 of infragravity waves (e.g., Ma et al., 2014b; Rijnsdorp et al., 2014, 2015; De Bakker et al., 2016), which  
87 play a key role in the wave-induced response of a ship that is moored in shallow water. This paper presents  
88 the first crucial step towards the development of such a single model tool. To predict the wave-induced  
89 response of a moored ship, an accurate description of the local wave field and the hydrodynamic loads are of  
90 vital importance. In this work, we advance the capabilities of the SWASH model to resolve the interactions  
91 between the waves and a non-moving floating body. This allows the model to resolve the wave impact on  
92 a restrained ship, providing the basis for future developments to simulate the wave-induced motions of a  
93 moored ship.

94 In non-hydrostatic models like SWASH, a fractional step method is used to solve the RANS equations.  
95 In this approach, the pressure is decomposed into a hydrostatic and a non-hydrostatic part. First, a discrete

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<sup>1</sup>Simulating WAves till SHore, available under the GNU GPL license at <http://swash.sourceforge.net/>.

96 free-surface equation is solved for the hydrostatic pressure (which determines the position of the free surface)  
97 to compute a provisional velocity field. In the subsequent step, the velocities are corrected after solving a  
98 Poisson equation for the non-hydrostatic pressure. One of the key properties of such models is their efficiency  
99 in simulating the nearshore wave dynamics due to the use of the Keller-Box scheme to discretise the non-  
100 hydrostatic pressure (e.g., Stelling and Zijlema, 2003).

101 In this work, we present a new numerical algorithm to account for the presence of a non-moving floating  
102 body in such a model (see §2). The inclusion of a floating body complicates the problem as the model has to  
103 account for the simultaneous occurrence of free-surface flow and the pressurised flow underneath the body.  
104 Following the approach of Casulli and Stelling (2013), we derived a free-surface equation that correctly  
105 describes the global continuity equation in both the free surface and the pressurised region. To ensure that  
106 the method is unconditionally stable with respect to the wave celerity (which is infinite in the pressurised  
107 region), our algorithm is based on the semi-implicit version of the SWASH model (e.g., Zijlema and Stelling,  
108 2005). Furthermore, we used the first-order pressure projection method (e.g., Chorin, 1968), instead of  
109 the second-order pressure correction method (e.g., Van Kan, 1986) that is used in SWASH, to deal with  
110 the pressurised flow underneath the ship. However, to retain the second-order accuracy when simulating  
111 free-surface flows, the second-order projection method is used in regions where the flow is bounded by a free  
112 surface (e.g., Vitousek and Fringer, 2013).

113 To assess the capabilities of this approach, we validated the model for the interactions between waves  
114 and a restrained ship using a total of four test cases. The first two tests consider the scattering of waves by  
115 a rectangular pontoon in a two-dimensional vertical (2DV) domain. First, we validate the model using an  
116 analytic solution for the scattering of linear monochromatic waves (§3). The second test case is based on  
117 a numerical solution of the scattering of a solitary wave (§4). Following these 2DV tests, we consider two  
118 laboratory experiments that were conducted in a wave basin, to assess the model capabilities in a three-  
119 dimensional (3D) physical domain. The third test case focusses on the scattering of regular waves by a  
120 rectangular pontoon (§5). To gain insight in the model capabilities for a more realistic environment, the  
121 final test considers an experimental campaign in which a realistic ship model (a Panamax container ship)  
122 was subject to a range of wave conditions, including short-crested sea states (§6). Finally, we summarise  
123 and discuss our findings in §7.

## 124 2. Numerical Methodology

125 The numerical methodology of the model that was developed in this work is based on the non-hydrostatic  
126 wave-flow model SWASH (Zijlema et al., 2011). The governing equations of the model are the RANS  
127 equations for an incompressible fluid with a constant density. The model solves the layer-averaged RANS  
128 equations using a curvilinear coordinate framework for the two horizontal dimensions, and a terrain following

129 coordinate framework for the vertical dimension.

130 In the following, we present the numerical methodology that was adopted to account for the presence of  
 131 a non-moving floating body. For the sake of clarity, we present our approach in its simplest form, without  
 132 loss of generality. We present the numerical approach in a Cartesian framework and for one horizontal  
 133 dimension. This relatively simple presentation of the modelling framework includes the numerical details  
 134 that are relevant for including a floating body in the numerical domain. Although porous structures are  
 135 included in the simulations of one of the test cases, we do not discuss their numerical discretisation as this  
 136 is not the focus of this study (see Appendix A for a brief description of its implementation).

### 137 2.1. Governing equations

138 We consider a two-dimensional domain that is bounded in the vertical by an interface at the top and at  
 139 the bottom (see Fig. 1). At the top interface, the domain is bounded by either a free surface  $z = \zeta(x, t)$ , or  
 140 a rigid non-moving floating body  $z = -S(x)$ , where  $t$  is time,  $x$  and  $z$  are the Cartesian coordinates, and  
 141  $z = 0$  is the still water level. At the bottom, the domain is bounded by a fixed bed,  $z = -d(x)$ . In this  
 142 domain, we can distinguish between two subdomains: an outer domain where the flow is bounded by a free  
 143 surface, and an inner domain where the flow is pressurised.

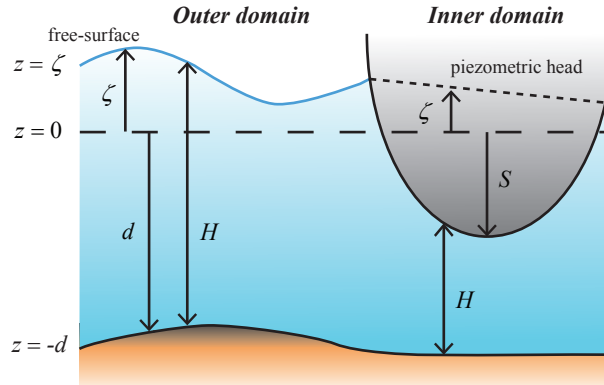


Figure 1: Sketch of the two-dimensional domain, including a free surface, a floating body, and a fixed bed.

144 In this framework, the governing equations read,

$$145 \quad \frac{\partial u}{\partial x} + \frac{\partial w}{\partial z} = 0, \quad (1)$$

$$146 \quad \frac{\partial u}{\partial t} + \frac{\partial uu}{\partial x} + \frac{\partial wu}{\partial z} = -g \frac{\partial \zeta}{\partial x} - \frac{\partial p}{\partial x} + \frac{\partial \tau_{xx}}{\partial x} + \frac{\partial \tau_{xz}}{\partial z}, \quad (2)$$

$$147 \quad \frac{\partial w}{\partial t} + \frac{\partial uw}{\partial x} + \frac{\partial ww}{\partial z} = -\frac{\partial p}{\partial z} + \frac{\partial \tau_{zx}}{\partial x} + \frac{\partial \tau_{zz}}{\partial z}, \quad (3)$$

148 where  $u(x, z, t)$  is the velocity in  $x$  direction,  $w(x, z, t)$  is the velocity in  $z$  direction,  $g$  is the gravitational  
 149 acceleration,  $\tau(x, z, t)$  represents the turbulent stresses,  $p(x, z, t)$  is the non-hydrostatic pressure (normalised

150 by a reference density), and  $\zeta(x, t)$  is the piezometric head (which is equivalent to the free surface in the  
 151 outer domain, see Fig. 1). At the top and bottom interfaces, the following kinematic boundary conditions  
 152 apply,

$$153 \quad w|_{z=\zeta} = \frac{\partial \zeta}{\partial t} + u \frac{\partial \zeta}{\partial x}, \quad (4)$$

$$154 \quad w|_{z=-S} = -u \frac{\partial S}{\partial x}, \quad (5)$$

$$155 \quad w|_{z=-d} = -u \frac{\partial d}{\partial x}. \quad (6)$$

156 At the bottom, we approximate the effect of bottom friction using a quadratic friction law,

$$157 \quad \tau_{xz}|_{z=-d} = c_f \frac{U|U|}{H}, \quad (7)$$

158 where  $c_f$  is a dimensionless friction coefficient,  $H$  is the total water depth, and  $U (= \frac{1}{H} \int u dz)$  is the depth-  
 159 averaged velocity. In this study, we computed  $c_f$  using the Manning-Strickler formulation ( $c_f = gn^2/H^{1/3}$ ,  
 160 where  $n$  is the Manning roughness coefficient). The turbulent stresses are evaluated using a turbulent  
 161 viscosity approximation (e.g.,  $\tau_{xx} = \nu_h \frac{\partial u}{\partial x}$  in which  $\nu_h$  is the horizontal eddy viscosity, and  $\tau_{xz} = \nu_v \frac{\partial u}{\partial z}$  in  
 162 which  $\nu_v$  is the vertical eddy viscosity). In a 3D framework, the horizontal viscosities are estimated using a  
 163 Smagorinsky-type formulation (Smagorinsky, 1963). In this work, the model is applied with a coarse vertical  
 164 resolution (2 layers) which implies that it does not fully resolve the vertical flow profile. To account for  
 165 some vertical mixing nonetheless, and to spread the effect of bottom friction over the vertical, the vertical  
 166 viscosity  $\nu_v$  was set at a constant value of  $10^{-4} \text{ m}^2\text{s}^{-1}$ .

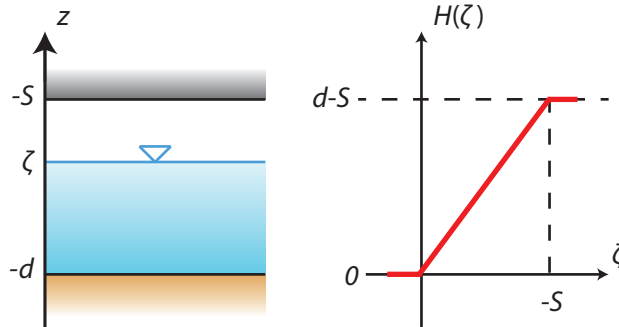


Figure 2: Piecewise linear function of the total water depth  $H$ , that is bounded by a fixed bottom ( $z = -d$ ) and a floating body ( $z = -S$ ).

167 To close the set of equations, we derive an extra equation to determine the piezometric head. Integrating  
 168 the continuity equation (1) from the bottom to the free surface and applying the relevant kinematic boundary  
 169 conditions (4 and 6) yields the following global-continuity equation in the outer domain,

$$170 \quad \frac{\partial \zeta}{\partial t} + \frac{\partial}{\partial x} \int_{-d}^{\zeta} u dz = \frac{\partial \zeta}{\partial t} + \frac{\partial HU}{\partial x} = 0,$$

171 where  $H = d + \zeta$  is the water depth in the outer domain. This equation governs the position of the free  
 172 surface in the outer domain, where the waves are dispersive. However, when a floating body is included in  
 173 the domain, a different equation applies in the pressurised region. Integrating Eq. (1) with the relevant  
 174 kinematic boundary conditions (5,6) yields the following equation,

$$175 \quad \frac{\partial}{\partial x} \int_{-d}^{-S} u dz = \frac{\partial HU}{\partial x} = 0,$$

176 where  $H = d - S$  is the water depth in the inner domain. This steady-state equation determines the  
 177 piezometric head in the pressured region. With the present assumptions of an incompressible fluid and a  
 178 rigid floating body, this equation implies that the celerity is infinite underneath the ship. Consequently,  
 179 perturbations in the flow and pressure field are spread instantly over the entire inner domain.

180 Following the approach of Casulli and Stelling (2013), these two global continuity equations are recast  
 181 into a single equation by defining the total water depth as a piecewise linear function of the piezometric head,  
 182  $H(\zeta) = \max(0, d + \min(-S, \zeta))$ . With this formulation, the water depth has a minimal value of zero, and  
 183 increases linearly as a function of  $\zeta$ , with an upper bound equal to the level of the floating body (illustrated  
 184 in Fig. 2). With this definition of the water depth, the two global continuity equations are combined into,

$$185 \quad \frac{\partial \max(-d, \min(-S, \zeta))}{\partial t} + \frac{\partial HU}{\partial x} = 0. \quad (8)$$

186 This single equation captures the nature of the flow in the outer and inner domain. This implies that the  
 187 resulting model accounts for the finite celerity in the outer domain (where waves are dispersive), and the  
 188 infinite celerity in the inner domain where the flow is pressurised. Furthermore, a pressurised cell can become  
 189 a free surface cell, and vice versa. This allows the model to account for the wetting and drying of the ship  
 190 as the water moves up and down the hull.

## 191 2.2. Spatial and temporal discretisation

192 The governing equations are discretised on a structured grid with a fixed number of layers  $K$  between  
 193 the top and bottom interface, where  $k = 1$  is the bottom layer, and  $k = K$  is the top layer. The resulting  
 194 grid has a spatially varying layer thickness of  $h_k = H/K$ , and a constant width  $\Delta x$ . A staggered grid is used  
 195 to arrange the variables: the piezometric head is located at a cell centre, the  $u$  velocities are located at the  
 196 centre the horizontal cell faces and the  $w$  velocities are located at the centre of the vertical cell faces (see Fig.  
 197 3). In the outer domain, the non-hydrostatic pressure variables are located at a vertical cell face following  
 198 the Keller-Box scheme (Lam and Simpson, 1976). Compared to the traditional cell centred arrangement  
 199 (e.g., Stansby and Zhou, 1998; Casulli and Stelling, 1998), this cell face arrangement significantly improves  
 200 the dispersive properties of the model (e.g., Stelling and Zijlema, 2003; Smit et al., 2014). For typical coastal  
 201 and harbour applications, two layers are generally sufficient to resolve the dispersion of the wave field. In  
 202 the simulations of this paper, two vertical layers were used as well.



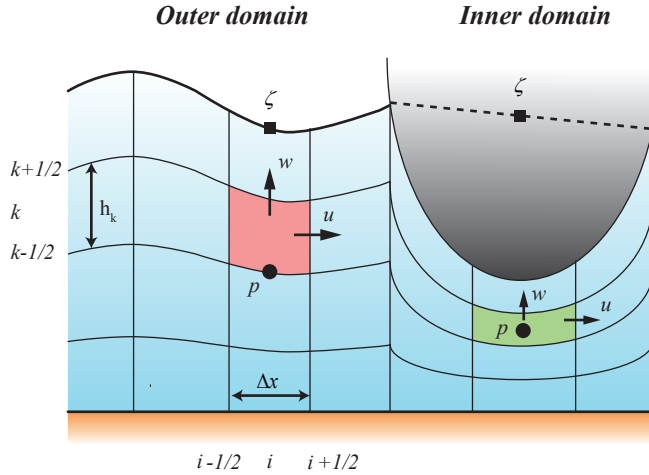


Figure 3: Horizontal and vertical grid definition, and the staggered variable arrangement on grid. A cell with its centre at  $i, k$  is bounded by a top ( $k + 1/2$ ) and bottom interface ( $k - 1/2$ ), and the left ( $i - 1/2$ ) and right ( $i + 1/2$ ) grid interfaces. The variable arrangement is depicted for the outer domain (illustrated in the red control volume) and the inner domain (illustrated in the green control volume).

203 In the inner domain, the piezometric head and velocity variables are arranged in a similar fashion.  
 204 However, the non-hydrostatic pressure variables are arranged using the cell centred arrangement instead  
 205 of the Keller-Box scheme. We adopt this arrangement as the application of the Keller-Box scheme is not  
 206 advantageous in the inner domain where the celerity is infinite. In addition, the centred arrangement allows  
 207 for an easier implementation, and results in a smaller stencil of the Poisson equation, which will become  
 208 apparent in the following (e.g., Eq. (14)).

209 A variable which is required at a location where it is not known is interpolated or extrapolated from  
 210 its surrounding variables. In both domains, these techniques follow the methodology of SWASH. Details  
 211 regarding the various types of interpolation used in SWASH (e.g., linear interpolation, upwind approxima-  
 212 tions, and flux limiters) can be found in Zijlema and Stelling (2005, 2008), and Zijlema et al. (2011). In  
 213 the following, variables that are computed using (bi)linear interpolation or extrapolation are denoted with  
 214 an overline, including the direction in which it takes place. For example, a layer thickness at the cell face  
 215  $i + 1/2$  that is computed using linear interpolation in  $x$  direction is written as  $\overline{h_{i+1/2,k}}^x$ . Variables that are  
 216 interpolated using upwind approximations, or flux limiters are denoted with a hat (e.g.,  $\hat{H}_{i+1/2}$ ). To achieve  
 217 second-order accuracy in space, and to avoid undesired oscillations near sharp gradients, we use the MUSCL  
 218 limiter (Van Leer, 1979) to determine the water depth and layer thickness at a horizontal cell face (e.g.,  
 219 Zijlema et al., 2011). Note that the water depth follows from  $H = d - S$  if a cell is located in the inner  
 220 domain. Here, the water depth and the layer thickness at a cell face can be directly computed from the  
 221 position of the bottom and the ship, and do not require interpolation.

222 To simulate the simultaneous occurrence of free surface and pressurised flows, the numerical method  
 223 must be unconditionally stable with respect to the celerity, which is infinite in the pressurised region (e.g.,  
 224 Casulli and Stelling, 2013). For this purpose, we use an (semi) implicit method to discretise the velocities  
 225 in the global continuity equation (8) and the piezometric head and the non-hydrostatic pressure in the  
 226 momentum equations (2-3). The advective and turbulent stress terms in the momentum equations (2-3) are  
 227 discretised using the same methods as in SWASH. As such, the vertical advective and turbulent stress terms  
 228 are discretised using the semi-implicit  $\theta$ -scheme (with  $\theta = 1/2$ ), to prevent a time step restriction when the  
 229 water depth becomes small (e.g., in the case of flooding and drying at a beach). Explicit schemes are used to  
 230 discretise the horizontal advective (the second-order accurate MacCormack scheme) and the turbulent stress  
 231 terms (the first-order accurate explicit Euler scheme). In space, the turbulent terms are discretised using  
 232 (second-order) central differences. For the spatial discretisation of the advective terms, various numerical  
 233 techniques can be used in SWASH (e.g., first-order upwind, flux limiters, and central differences). In this  
 234 work, the advective terms in the  $u$ -momentum equation are discretised using the MUSCL limiter. In the  
 235  $w$ -momentum equation, the horizontal advective terms are discretised using the second-order BDF scheme,  
 236 and the vertical term is discretised using the first-order upwind scheme.

237 In the following, we present the discretised versions of the layer-averaged equations, and the solution  
 238 algorithm that we adopted to include a floating body. To improve the readability of the paper, we focus on  
 239 the aspects that are affected by including a floating body in the domain. As the inclusion of the body does  
 240 not affect the integration of the equations over a layer, we omit their details as they have been extensively  
 241 treated before (Stelling and Zijlema, 2003; Zijlema and Stelling, 2005). For the same reason, we do not  
 242 present the discretisation of the advective and turbulent stress terms. Details regarding their discretisation  
 243 can be found in Zijlema and Stelling (2005, 2008) and Zijlema et al. (2011).

### 244 2.2.1. Continuity equations

245 The global continuity equation (8) is discretised in time using the  $\theta$ -method. For brevity, we will write  
 246 the semi-implicit terms that arise due to this method for some variable  $\phi$  as  $\phi^{n+\theta} = \theta\phi^{n+1} + (1-\theta)\phi^n$ , in  
 247 which  $n$  indicates the time level ( $t^n = n\Delta t$ , where  $\Delta t$  is a fixed time step) and  $\theta$  is an implicitness factor  
 248 (with an allowable range of  $1/2 \leq \theta \leq 1$ ). With  $\theta = 1$  the  $\theta$ -method is equivalent to the first-order accurate  
 249 implicit Euler method, and with  $\theta = 1/2$  it is equivalent to the second-order Crank Nicholson method. A  
 250 global mass conserving discretisation of Eq. (8) is given by,

$$251 \frac{\max(-d_i, \min(-S_i, \zeta_i^{n+1})) - \max(-d_i, \min(-S_i, \zeta_i^n))}{\Delta t} + \frac{\hat{H}_{i+1/2}^n U_{i+1/2}^{n+\theta_{i+1/2}} - \hat{H}_{i-1/2}^n U_{i-1/2}^{n+\theta_{i-1/2}}}{\Delta x} = 0, \quad (9)$$

252 in which  $U$  is the approximated depth-averaged velocity ( $U = 1/H \sum_{k=1}^K h_k u_k$ , where  $u_k$  is the layer-averaged  
 253  $u$ -velocity). In this work, a spatially varying  $\theta_{i\pm 1/2}$  parameter is adopted to account for the different flow  
 254 regimes in the outer and inner domain. To compute the steady-state solution of Eq. (9) when the flow

255 is pressurised, the value of  $\theta_{i\pm 1/2}$  is set at 1 when a horizontal grid interface  $i \pm 1/2$  is located in the inner  
 256 domain. If an interface is located in the outer domain,  $\theta_{i\pm 1/2} = 1/2$  to prevent numerical wave damping.

257 A local mass conserving discretisation of the local continuity equation (1) is given by,

$$258 \frac{\overline{h_{i+1/2,k}^n}^x u_{i+1/2,k}^{n+1} - \overline{h_{i-1/2,k}^n}^x u_{i-1/2,k}^{n+1}}{\Delta x} + w_{i,k+1/2}^{n+1} - w_{i,k-1/2}^{n+1} \quad (10)$$

$$- \overline{u_{i,k+1/2}^{n+1}}^x z \frac{z_{i+1/2,k+1/2}^n - z_{i-1/2,k+1/2}^n}{\Delta x} + \overline{u_{i,k-1/2}^{n+1}}^x z \frac{z_{i+1/2,k-1/2}^n - z_{i-1/2,k-1/2}^n}{\Delta x} = 0,$$

259 in which  $z_{k\pm 1/2}$  represent the vertical position of the interfaces at the top ( $z_{k+1/2}$ ) and bottom ( $z_{k-1/2}$ ) of a  
 260 layer.

### 261 2.2.2. Momentum equations

262 The layer-averaged version of the  $u$ -momentum equation (2) is discretised as,

$$263 \frac{u_{i+1/2,k}^{n+1} - u_{i+1/2,k}^n}{\Delta t} = -g \frac{\zeta_{i+1}^{n+\theta_{i+1/2}} - \zeta_i^{n+\theta_{i+1/2}}}{\Delta x} - Pu_{i+1/2,k}^{n+1}, \quad (11)$$

264 where  $Pu_{i+1/2,k}^{n+1}$  represents the discretisation of the non-hydrostatic pressure term. For brevity, we omit  
 265 details regarding the discretisation of the advective and turbulent terms in this momentum equation. For  
 266 the time integration of the piezometric head gradient, the  $\theta$ -method is used with a spatially varying  $\theta_{i\pm 1/2}$   
 267 parameter. Similar to the global continuity equation, the value of this parameter is set depending on the  
 268 location of the grid interface  $i \pm 1/2$ , that is,  $\theta_{i\pm 1/2} = 1/2$  in the outer domain and  $\theta_{\pm 1/2} = 1$  in the inner  
 269 domain.

270 The layer-averaged non-hydrostatic pressure term is evaluated as,

$$271 Pu_k = \frac{1}{h_k} \int_{z_{k-1/2}}^{z_{k+1/2}} \frac{\partial p}{\partial x} dz = \frac{1}{h_k} \left( \frac{\partial p_k h_k}{\partial x} - p_{k+1/2} \frac{\partial z_{k+1/2}}{\partial x} + p_{k-1/2} \frac{\partial z_{k-1/2}}{\partial x} \right).$$

272 Discretising this term yields different expressions in the outer and inner domain due to the differences in  
 273 the arrangement of the non-hydrostatic pressure variable (Fig. 3). In discretised form,  $Pu_{i+1/2,k}^{n+1}$  reads,

$$274 Pu_{i+1/2,k}^{n+1} = \begin{cases} \frac{1}{\overline{h_{i+1/2,k}^n}^x} \left[ \frac{\overline{p_{i+1,k}^{n+1}}^z h_{i+1,k}^n - \overline{p_{i,k}^{n+1}}^z h_{i,k}^n}{\Delta x} \right. \\ \quad - \overline{p_{i+1/2,k+1/2}^{n+1}}^x \frac{z_{i+1,k+1/2}^n - z_{i,k+1/2}^n}{\Delta x} \\ \quad \left. + \overline{p_{i+1/2,k-1/2}^{n+1}}^x \frac{z_{i+1,k-1/2}^n - z_{i,k-1/2}^n}{\Delta x} \right] & \text{(Outer domain),} \\ \frac{1}{\overline{h_{i+1/2,k}^n}^x} \left[ \frac{\overline{p_{i+1,k}^{n+1}}^z h_{i+1,k}^n - \overline{p_{i,k}^{n+1}}^z h_{i,k}^n}{\Delta x} \right. \\ \quad - \overline{p_{i+1/2,k+1/2}^{n+1}}^x z \frac{z_{i+1,k+1/2}^n - z_{i,k+1/2}^n}{\Delta x} \\ \quad \left. + \overline{p_{i+1/2,k-1/2}^{n+1}}^x z \frac{z_{i+1,k-1/2}^n - z_{i,k-1/2}^n}{\Delta x} \right] & \text{(Inner domain).} \end{cases} \quad (12)$$

275 This discretisation introduces virtual points in both the outer and inner domain. For example, virtual points  
 276 are located at the vertical cell faces in the inner domain, which are interpolated or extrapolated from the  
 277 surrounding pressure variables (e.g.,  $\overline{p_{i+1/2, k+1/2}^{n+1}}^{xz}$ ). Note that we take advantage of the pressure boundary  
 278 condition at the free surface in the outer domain (i.e.,  $p|_{z=\zeta} = 0$ ), to prescribe the pressure variables at the  
 279 free surface.

280 The layer-averaged version of the  $w$ -momentum equation (3) is discretised as,

$$281 \quad \frac{w_{i, k+1/2}^{n+1} - w_{i, k+1/2}^n}{\Delta t} = -Pw_{i, k+1/2}^{n+1}, \quad (13)$$

282 where  $Pw_{i, k+1/2}^{n+1}$  represents the discretisation of the non-hydrostatic pressure term. In this equation, we omit  
 283 details regarding the advective and turbulent terms for brevity. In the outer domain, Eq. (13) applies at all  
 284 interfaces except for the bottom, where the kinematic boundary condition (6) applies. In the inner domain,  
 285 Eq. (13) only applies at the internal interfaces, and the kinematic boundary conditions apply at the top (5)  
 286 and bottom interface (6).

287 Similar to the  $u$ -momentum equation, the discretised form of the non-hydrostatic pressure term is dif-  
 288 ferent in the outer and inner domain. In the outer domain, the non-hydrostatic pressure term,  $Pw_{k+1/2} =$   
 289  $\int_{z_k}^{z_{k+1}} \frac{\partial p}{\partial z} dz$ , is evaluated using the Keller-Box scheme (Lam and Simpson, 1976). In this method, the non-  
 290 hydrostatic pressure gradient is evaluated as the arithmetic average of the gradients at the vertical cell  
 291 faces,

$$292 \quad \frac{\partial p_k}{\partial z} = \frac{1}{2} \frac{\partial p_{k+1/2}}{\partial z} + \frac{1}{2} \frac{\partial p_{k-1/2}}{\partial z}.$$

293 With this expression, and following a straightforward evaluation of the  $\frac{\partial p_k}{\partial z}$  term, we derive an expression  
 294 for the gradient at the top cell interface  $\frac{\partial p_{k+1/2}}{\partial z}$ ,

$$295 \quad \frac{1}{2} \frac{\partial p_{k+1/2}}{\partial z} + \frac{1}{2} \frac{\partial p_{k-1/2}}{\partial z} = \frac{\partial p_k}{\partial z} \approx \frac{p_{k+1/2} - p_{k-1/2}}{h_k} \rightarrow \frac{\partial p_{k+1/2}}{\partial z} = 2 \frac{p_{k+1/2} - p_{k-1/2}}{h_k} - \frac{\partial p_{k-1/2}}{\partial z}.$$

296 The gradient at one interface lower,  $\frac{\partial p_{k-1/2}}{\partial z}$ , is evaluated similarly. A subsequent substitution of these  
 297 gradient terms into  $Pw_{k+1/2}$  results in the following expression,

$$298 \quad Pw_{k+1/2} = \sum_{m=0}^{k-1} \left[ (-1)^m 2 \frac{p_{k+1/2-m} - p_{k-1/2-m}}{h_{k-m}} \right] + (-1)^k \frac{\partial p_{1/2}}{\partial z}.$$

299 To close this expression, the vertical gradient of the non-hydrostatic pressure needs to be evaluated at the  
 300 bottom (i.e.,  $\frac{\partial p_{1/2}}{\partial z}$ ). This term is neglected in this work as its contribution is zero when the bottom is flat,  
 301 which is the case in the simulations of this study.

302 In the inner domain, we approximate the non-hydrostatic pressure term in a different manner,

$$303 \quad Pw_{k+1/2} = \int_{z_k}^{z_{k+1}} \frac{\partial p}{\partial z} dz = \frac{p_{k+1} - p_k}{h_{k+1/2}}.$$

304 In conclusion, the discretised form of  $Pw_{i,k+1/2}^{n+1}$  reads,

$$305 \quad Pw_{i,k+1/2}^{n+1} = \begin{cases} \sum_{m=0}^{k-1} \left[ (-1)^m 2 \frac{p_{i,k+1/2-m}^{n+1} - p_{i,k-1/2-m}^{n+1}}{h_{i,k-m}^n} \right] & \text{(Outer domain),} \\ \frac{p_{i,k+1}^{n+1} - p_{i,k}^{n+1}}{\bar{h}_{i,k+1/2}^z} & \text{(Inner domain).} \end{cases} \quad (14)$$

306 In the outer domain, this equation implies that Eq. (13) depends on all pressure variables that are located  
 307 at, and below the interface of interest. In contrast, this equation only depends on the two surrounding  
 308 pressure variables when a face is located in the inner domain.

### 309 2.3. Solution procedure

310 We employ a fractional step method that is known as the pressure projection method (e.g., Chorin,  
 311 1968) to solve the system of discretised equations. With this method, the time integration from  $n$  to  $n + 1$   
 312 is split into two steps. In the first step (or hydrostatic step), a provisional velocity field ( $u^*$ ) and the  
 313 piezometric head  $\zeta^{n+1}$  are computed using a reduced number of terms in the momentum equations (11,13).  
 314 In the second step (or non-hydrostatic step), the non-hydrostatic pressure  $p^{n+1}$  and the velocity field  $u^{n+1}$   
 315 and  $w^{n+1}$  are computed. Within the present framework, this fractional step procedure implies that the  
 316 horizontal momentum equation (11) is solved in two steps. First, a provisional  $u$ -velocity is computed in  
 317 the hydrostatic step,

$$318 \quad u_{i+1/2,k}^* = u_{i+1/2,k}^n - g \frac{\Delta t}{\Delta x} \left( \zeta_{i+1}^{n+\theta_{i+1/2}} - \zeta_i^{n+\theta_{i+1/2}} \right). \quad (15)$$

319 Subsequently, the  $u$  velocity at  $n + 1$  is computed in the non-hydrostatic step,

$$320 \quad u_{i+1/2,k}^{n+1} = u_{i+1/2,k}^* - \Delta t P u_{i+1/2,k}^{n+1}. \quad (16)$$

#### 321 2.3.1. Hydrostatic step

322 In the hydrostatic step, the global continuity equation (9) is solved to compute  $\zeta^{n+1}$ . For this purpose,  
 323 the horizontal momentum equation (16) is substituted into Eq. (9), which yields an implicit equation for the  
 324 unknown  $\zeta^{n+1}$ . In this work, we use a predictor-corrector technique to solve this implicit equation. With  
 325 this technique, the computation of the provisional horizontal velocity field  $u^*$  (15) is divided into two steps.  
 326 First, we predict an estimate of  $u^*$  based on the piezometric head at the previous time step,

$$327 \quad u_{i+1/2,k}^{**} = u_{i+1/2,k}^n - g \frac{\Delta t}{\Delta x} (\zeta_{i+1}^n - \zeta_i^n). \quad (17)$$

328 Subsequently, the provisional velocity field can be computed based on the piezometric head correction  
 329  $\Delta \zeta (= \zeta^{n+1} - \zeta^n)$ ,

$$330 \quad u_{i+1/2,k}^* = u_{i+1/2,k}^{**} - \theta_{i+1/2} g \frac{\Delta t}{\Delta x} (\Delta \zeta_{i+1} - \Delta \zeta_i). \quad (18)$$

331 To solve this equation, the piezometric head correction needs to be computed first. Substituting the equations  
 332 for  $u^{n+1}$  (16) and  $u^*$  (18) in the global continuity equation (9) yields an implicit equation for  $\Delta\zeta$ ,

$$\begin{aligned}
 & \max(-d_i - \zeta_i^n, \min(-S_i - \zeta_i^n, \Delta\zeta_i)) - g \frac{\Delta t^2}{\Delta x^2} \left[ \theta_{i+1/2}^2 \hat{H}_{i+1/2}^n (\Delta\zeta_{i+1} - \Delta\zeta_i) - \theta_{i-1/2}^2 \hat{H}_{i-1/2}^n (\Delta\zeta_i - \Delta\zeta_{i-1}) \right] \\
 & = \max(-d_i - \zeta_i^n, \min(-S_i - \zeta_i^n, 0)) \\
 & - \frac{\Delta t}{\Delta x} \left[ \hat{H}_{i+1/2}^n \left( \theta_{i+1/2} U_{i+1/2}^{**} + (1 - \theta_{i+1/2}) U_{i+1/2}^n \right) - \hat{H}_{i-1/2}^n \left( \theta_{i-1/2} U_{i-1/2}^{**} + (1 - \theta_{i-1/2}) U_{i-1/2}^n \right) \right] \\
 & + \sum_{k=1}^K \frac{\Delta t^2}{\Delta x} \left( \beta_{i+1/2} \theta_{i+1/2} \overline{h_{i+1/2,k}^n}^x P u_{i+1/2,k}^{n+1} - \beta_{i-1/2} \theta_{i-1/2} \overline{h_{i-1/2,k}^n}^x P u_{i-1/2,k}^{n+1} \right).
 \end{aligned} \tag{19}$$

333  
 334 This implicit equation represents a (positive definite and symmetric) tridiagonal piecewise-linear system of  
 335 equations for  $\Delta\zeta$ , which is solved using the Newton-type iterative method of Brugnano and Casulli (2009)  
 336 in combination with a tridiagonal matrix algorithm<sup>2</sup>. The parameter  $\beta$  indicates if the contribution of  $p^{n+1}$   
 337 is included ( $\beta = 1$ ) or excluded ( $\beta = 0$ ) in the global continuity equation. If  $\beta = 1$  in Eq. (19), the temporal  
 338 accuracy of the pressure projection method is second-order in simulating free-surface flows, whereas the  
 339 method is first-order accurate if  $\beta = 0$  (e.g., Vitousek and Fringer, 2013). Similar to  $\theta_{i\pm 1/2}$ , the parameter  
 340  $\beta_{i\pm 1/2}$  can be varied in the domain, which will be discussed in §2.3.3. If  $\beta_{i\pm 1/2} = 1$  in any of the cells,  
 341 Eq. (19) cannot be directly solved as the contribution of  $p^{n+1}$  in  $Pu^{n+1}$  is not yet known. To include this  
 342 contribution, several iterations over the hydrostatic and non-hydrostatic steps are required.

### 343 2.3.2. Non-hydrostatic step

344 In the non-hydrostatic step, the velocity field at  $n+1$  is computed based on the non-hydrostatic pressure  
 345 at  $n+1$ . The  $u^{n+1}$  velocity is computed following Eq. (16), and  $w^{n+1}$  is computed as,

$$346 \quad w_{i,k+1/2}^{n+1} = w_{i,k+1/2}^n - \Delta t P w_{i,k+1/2}^{n+1}. \tag{20}$$

347 To solve these equations,  $p^{n+1}$  is first computed based on the local continuity equation (10). Substituting  
 348 the momentum equations and the relevant kinematic boundary conditions in Eq. (10) yields a Poisson  
 349 equation for  $p^{n+1}$ . Fig. 4 illustrates the locations of the unknowns and the stencil of the non-hydrostatic  
 350 pressure in the outer and inner domain for a model with two vertical layers. The Poisson equation (which  
 351 is asymmetric and not positive definite) is solved using a preconditioned BiCGSTAB solver (e.g., Barrett  
 352 et al., 1994; Zijlema and Stelling, 2005).

### 353 2.3.3. Solution algorithm

354 The solution algorithm can be summarised as follows,

---

<sup>2</sup>In the case of two horizontal dimensions, the system is pentadiagonal and solved using a preconditioned conjugate gradient method (e.g., Barrett et al., 1994).

- 355 1. Start the computation with  $\zeta^n$ ,  $u^n$ ,  $w^n$ ,  $p^n$ , from the initial conditions or from the previous time step.
- 356 **2. Hydrostatic step**
- 357 (a) Solve Eq. (17) to compute the estimate of the provisional horizontal velocity ( $u^{**}$ ).
- 358 (b) Solve the global continuity equation (19) to compute the piezometric head correction ( $\Delta\zeta$ ).
- 359 (c) Solve Eq. (18) to compute the provisional horizontal velocity field ( $u^*$ ), which satisfies the global
- 360 continuity equation.
- 361 **3. Non hydrostatic step**
- 362 (a) Solve the Poisson equation resulting from the local continuity equation (10) to compute the
- 363 non-hydrostatic pressure at the next time step ( $p^{n+1}$ ).
- 364 (b) If the non-hydrostatic pressure is included in the hydrostatic step ( $\beta = 1$ ), return to step 2b and
- 365 repeat until convergence is reached.
- 366 4. Solve Eq. (16) and Eq. (20) to compute the divergence-free velocity field ( $u^{n+1}$ , and  $w^{n+1}$ ), and
- 367 advance the computation to the next time step.

368 This algorithm differs from the conventional SWASH model, which uses the explicit leapfrog scheme or

369 the semi-implicit  $\theta$ -method in combination with the pressure correction method of Van Kan (1986) to solve

370 the layer-averaged RANS equations. However, to simulate the simultaneous occurrence of free surface and

371 pressurised flows, the algorithm presented in this work is based on the semi-implicit version of the SWASH

372 model as explicit schemes are not suited to simulate pressurised flows (e.g., Casulli and Stelling, 2013).

373 Furthermore, we implemented a spatially varying implicitness parameter of the  $\theta$  scheme, with  $\theta = 1$  in the

374 inner domain and  $\theta = 1/2$  in the outer domain. This allows the model to compute the steady-state solution

375 of the global continuity equation in the inner domain, and at the same time it prevents undesired numerical

376 wave damping in the outer domain.

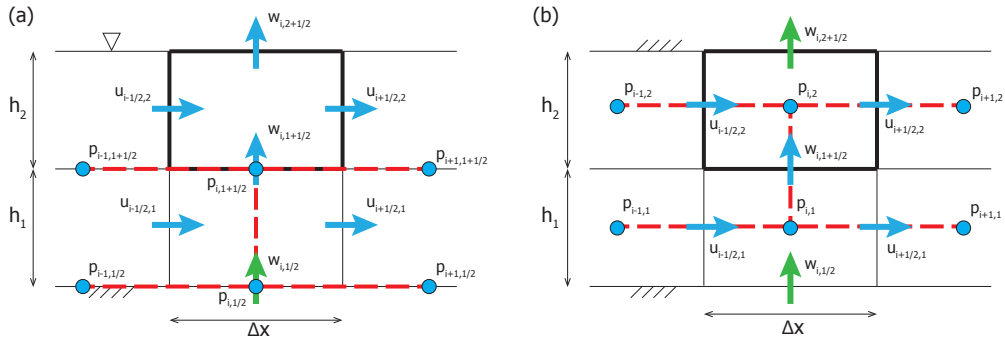


Figure 4: The locations of the unknowns, and the stencil of the non-hydrostatic pressure in the outer domain (a) and in the inner domain (b) for a two layer model. The thick black lines indicate the control volume of the local continuity equation. Green velocities are computed using the kinematic boundary condition, and blue velocities are computed using the momentum equations. The dashed red line indicates the stencil of the non-hydrostatic pressure.

377 The nature of the flow regime in the pressurised region also implies the use of the first-order accurate  
378 pressure projection method ( $\beta = 0$  in Eq. (19)), instead of the second-order accurate pressure correction  
379 method. Note that the main difference between the pressure projection and pressure correction method is  
380 the inclusion of an explicit non-hydrostatic pressure contribution in the hydrostatic step (see Stelling and  
381 Zijlema, 2003, for more details). The disadvantage of the first-order scheme is that it introduces a significant  
382 amount of wave damping in the outer domain. To retain the second-order accuracy in the outer domain and  
383 to prevent this damping (e.g., Vitousek and Fringer, 2013), the non-hydrostatic pressure contribution was  
384 included in the global continuity equation when a cell face is located in the outer domain (i.e.,  $\beta_{i\pm 1/2} = 1$  in  
385 Eq. (19)).

#### 386 2.4. Computation of hydrodynamic forces and moments

387 The resulting numerical model provides the flow and pressure field in the numerical domain, while  
388 accounting for the presence of the floating body. The resulting hydrodynamic forces that act on the body  
389 are found by integrating the total pressure over the wet surface of the body,

$$390 \quad \mathbf{F} = \iint_{\mathcal{H}} P \mathbf{n} \, d\mathcal{H},$$

391 where  $\mathbf{F} = (F_x, F_y, F_z)$ ,  $P$  is the total pressure (i.e., the combined hydrostatic and non-hydrostatic pressure),  
392  $\mathcal{H}$  represents the wet surface of the body, and  $\mathbf{n}$  is the unit vector normal to the body surface. The individual  
393 components of  $\mathbf{F}$  are known as the surge force ( $F_x$ ), the sway force ( $F_y$ ), and the heave force ( $F_z$ ). The  
394 moments around the centre of gravity of the body are computed as,

$$395 \quad \mathbf{M} = \iint_{\mathcal{H}} (\mathbf{r} - \mathbf{r}_c) P \mathbf{n} \, d\mathcal{H},$$

396 where  $\mathbf{M} = (M_x, M_y, M_z)$ ,  $\mathbf{r}$  is the position vector of the pressure acting on the body surface, and  $\mathbf{r}_c$  is the  
397 position vector of the centre of gravity of the body. The individual components of  $\mathbf{M}$  are known as the roll  
398 moment ( $M_x$ ), the pitch moment ( $M_y$ ), and the yaw moment ( $M_z$ ).

### 399 3. Scattering of linear monochromatic waves by a pontoon

400 We consider the interaction between linear monochromatic waves and a non-moving pontoon that is  
401 located in water of constant depth (see Fig. 5 for the geometry and the dimensions of the pontoon). For  
402 such a 2DV set-up, Cointe et al. (1991) presented an analytic solution of the linearised potential flow problem.  
403 To assess the model capabilities for this problem, model results are compared with the analytic solution for  
404 the (partial) reflection and transmission of the waves, and for the hydrodynamic loads that act on the body.  
405 A comparison is made for a series of monochromatic waves, with periods varying between 1 to 5 s and a  
406 constant small wave steepness ( $a/L = 1 \times 10^{-5}$ , where  $a$  is the wave amplitude and  $L$  is the wave length).



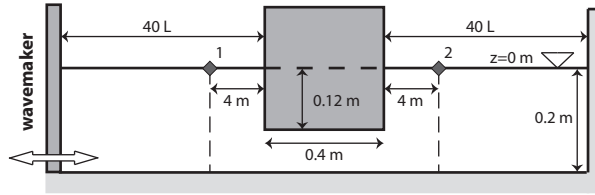


Figure 5: Sketch of the numerical set-up, including the geometry and dimensions of the pontoon. Note that the sketch is not at scale. The diamonds markers at the still water level indicate the output locations of the numerical model. These locations were positioned at a distance of 20 water depths away from the body ( $= 4$  m), to minimise the effect of evanescent modes (which decay exponentially away from the pontoon).

407 In the analytic solution of Cointe et al. (1991), the domain is divided in three sub-domains (up wave, down  
 408 wave and below the pontoon), in which the velocity potential is expressed by the appropriate eigenfunction  
 409 expansions. These eigenfunction expansions consist of a single propagating wave mode and an infinite  
 410 series of evanescent modes. In contrast with a propagating wave, evanescent modes exhibit an exponential  
 411 behaviour in the horizontal plane, and a sinusoidal variation in the vertical. They are primarily important  
 412 near sudden changes in the water depth, like the interfaces between the sub-domains. At these interfaces,  
 413 they are necessary to match the different solutions in the sub-domains. Matching the eigenfunctions and  
 414 their horizontal derivatives at the two interfaces between the three sub-domains, and truncating them at a  
 415 certain number of terms, yields an algebraic system of equations for the unknown velocity potential. This  
 416 system was solved using the Symbolic Toolbox of Matlab. For the wave conditions considered in this work,  
 417 we found that the analytic solution converged when 21 terms were included in the eigenfunction expansions  
 418 (not shown).

419 Fig. 5 illustrates the numerical set-up that was used in SWASH to reproduce this test case. A relatively  
 420 large numerical domain (spanning more than 80 wave lengths) was used to prevent adverse effects on the  
 421 analysis of wave reflections at the wavemaker and the vertical wall at the end of the domain. In the absence  
 422 of such reflections, the predicted wave signal at sensor 2 represents a transmitted wave. Furthermore, as  
 423 the wave conditions are linear, the signal at sensor 1 can be decomposed in an incident and reflected wave  
 424 component. At this sensor, the incident signal was computed based on a simulation that excluded the  
 425 floating body. Subsequently, the reflected signal was computed by taking the difference between the total  
 426 signal and the incident signal at sensor 1. With this model set-up, the reflection and transmission coefficients  
 427 were computed based on stationary reflected, transmitted, and reflected wave signals with a duration of at  
 428 least 25 wave periods.

429 The temporal and grid resolution that was used in the SWASH simulations is based on the wave charac-  
 430 teristics. The number of vertical layers was chosen based on the normalised water depth  $kd$  (in which  $k$  is  
 431 the wave number), which determines the dispersive properties of the waves. In this test case, the  $kd$  values

432 ranged between 0.15 – 1. For this range, two vertical layers are sufficient to resolve the wave dispersion  
 433 (e.g., Zijlema et al., 2011; Smit et al., 2014). The horizontal grid resolution was set at 100 points per wave  
 434 length (resulting in  $\Delta x \sim 0.008 - 0.04$  m), which provides sufficient grid points to capture the wave shape.  
 435 Finally, the time step was set at 300 points per wave period (resulting in  $\Delta t \sim 0.003 - 0.02$  s) to minimise  
 436 the numerical dissipation of the waves as they propagated through the relatively large domain.

### 437 3.1. Results

438 Fig. 6 shows the comparison between the model and the analytic solution for this test case. For increasing  
 439 wave periods, wave reflections reduce as the transmission increases (Fig. 6a-b). The model captures this  
 440 trend, and the magnitude of the coefficients for the considered range of wave periods (Fig. 6a-c). Similarly,  
 441 the predicted amplitudes of the two force components agree well with the analytic solution. Furthermore,  
 442 the model captures the phase difference between  $F_x$  and  $F_z$  (illustrated by the red line and markers in Fig.  
 443 6e).

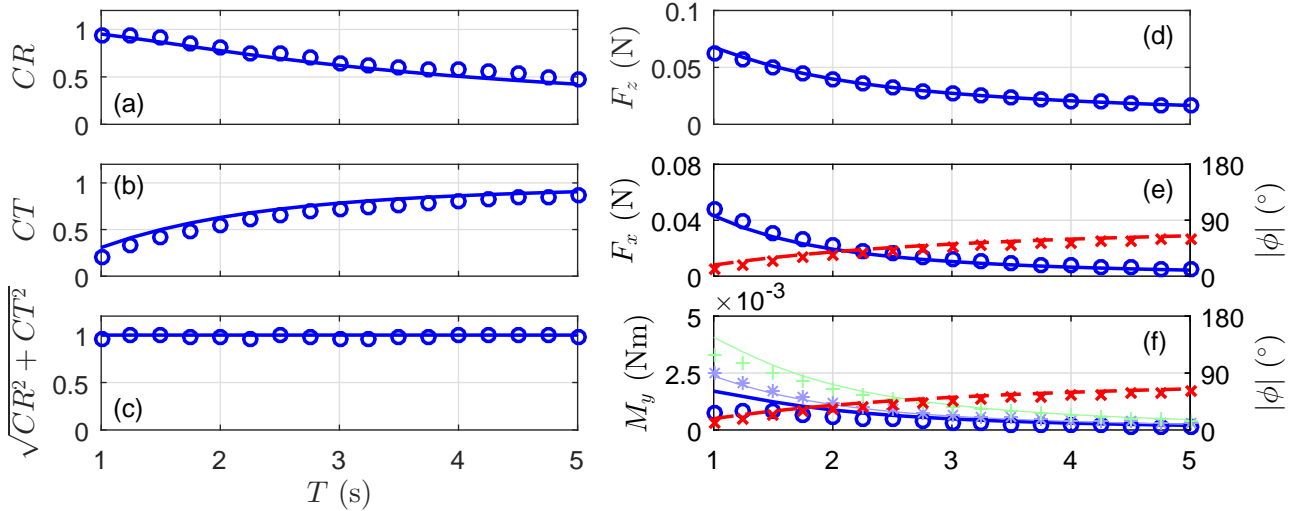


Figure 6: Comparison between the predicted (markers) and analytic results (lines) for the scattering of linear waves by a fixed pontoon. The left panels show the results for the reflection  $CR$  (a), transmission  $CT$  (b), and combined reflection and transmission coefficients  $\sqrt{CR^2 + CT^2}$  (c). The right panels show the results for the amplitudes of the heave force  $F_z$  (d), surge force  $F_x$  (e), and pitch moment  $M_y$  (f). The full line and the circles indicate the amplitude of the hydrodynamic loads. The dashed lines and the crosses in panel (e) and (f) depict the absolute phase difference ( $|\phi|$ ) between the respective load component ( $F_x$  or  $M_y$ ) and  $F_z$ . In panel (f), the individual contributions of  $F_z$  and  $F_x$  to  $M_y$  are depicted by the light green and light blue results, respectively.

444 Compared to the force components, discrepancies are larger for  $M_y$  (which is typically under predicted),  
 445 although its trend and especially its phase difference with  $F_z$  are reproduced well (Fig. 6f). The moment is  
 446 a linear combination of the moment contributions by  $F_z$  and  $F_x$ . These two contributions are nearly out of

447 phase with each other, and the amplitude of  $M_y$  is therefore approximately given by the difference between  
 448 the amplitude of  $F_z$  and  $F_x$ . Compared to the amplitude of  $M_y$ , the predicted amplitudes of these two  
 449 contributions agree better with the analytic solution (illustrated by the light blue and light green results in  
 450 Fig. 6f), although the  $F_z$  contribution is under predicted for shorter wave periods. This illustrates that  $M_z$   
 451 is sensitive to relatively small discrepancies in the force components.

452 The results of this test case show that the model predictions are in general agreement with the analytic  
 453 solution for the transmission and reflection coefficients, and the hydrodynamic loads. This demonstrates that  
 454 two layers are sufficient to capture the scattering of the waves by the pontoon, and the overall magnitude  
 455 of the hydrodynamic loads that act on the pontoon.

456 To gain insight in the temporal accuracy of the model when solving a combination of free surface and  
 457 pressurised flows, a numerical convergence test was conducted for one wave condition of this analytic test  
 458 case (i.e., the wave with a period of 1 s). For this condition, we conducted a series of simulations with a  
 459 gradually decreasing time step (starting at 80 points per wave period), for which the numerical solution is  
 460 expected to converge to a final solution. By taking the root-mean-square-error between the results of the  
 461 finest and a coarser temporal resolution, we can gain insight in the convergence behaviour and the temporal  
 462 accuracy of the model. The results of this convergence test confirm that the overall temporal accuracy of  
 463 the model is first order when predicting the hydrodynamic loads on a floating body (Fig. 7).

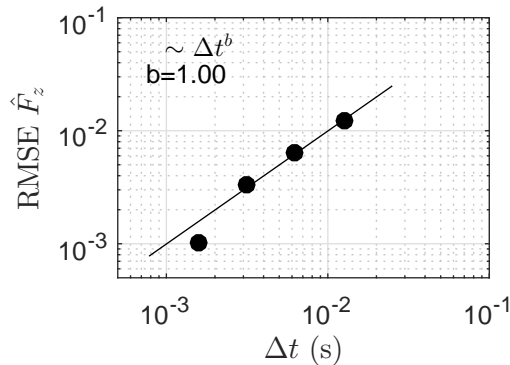


Figure 7: Root-mean-square-error of the heave force amplitude  $\hat{F}_z$  for a varying temporal resolution. The markers indicate the computed error, and the line indicates the best fit for the  $\Delta t^b$  power function (in which  $b$  is a real number). In the top left corner, the  $b$  coefficient of the power function is listed.

#### 464 4. Scattering of solitary wave by a pontoon

465 In a similar 2DV set-up as §3, Lin (2006) considered the interactions between a fixed pontoon and a  
 466 solitary wave. In this test, the still water depth was 1 m, and the pontoon had a width of 5 m and a draft of  
 467 0.4 m. The domain had a total length of 100 m, and the centre of the pontoon was positioned at  $x = 32.5$  m

468 (see Fig. 8a). In this set-up, Lin (2006) solved the scattering of a solitary wave with a height of 0.1 m using  
 469 a non-hydrostatic  $\sigma$ -coordinate model and a volume of fluid model. Both models yielded similar results  
 470 with the same horizontal resolution, but with different vertical resolutions (i.e., 20 layers in the  $\sigma$ -model,  
 471 and 130 meshes in the VOF model). In this work, we compare our model results with the results of Lin  
 472 (2006), to demonstrate the capabilities of the present approach. To allow for a fair comparison, the spatial  
 473 resolution was set in accordance with the study of Lin (2006), except for the vertical resolution. In this  
 474 work, only 2 layers were employed to discretise the vertical domain. The horizontal grid resolution was set  
 475 at  $\Delta x = 0.05$  m, and the time step at  $\Delta t = 0.01$  s.

#### 476 4.1. Results

477 After generation at the wavemaker, the solitary wave propagated towards the pontoon, where it partially  
 478 reflected and transmitted. After interacting with the pontoon, the reflected part of the wave propagated  
 479 back towards the wavemaker, where it was absorbed. This wave arrived after about 20 s at sensor 1, which  
 480 is characterised by an initially positive elevation that is followed by a depression and some small oscillations  
 481 (Fig. 8b). At roughly the same time, the transmitted wave arrived at sensor 2 (Fig. 8c). At both wave  
 482 sensors, the results of the 2 layer SWASH model and the 20 layer  $\sigma$ -model are in excellent agreement.  
 483 Naturally, the coarse vertical resolution that was used in this work implies that the model did not capture  
 484 the vertical structure of the flow field in the vicinity of the structure. Nonetheless, the model captured the  
 485 partial reflection and transmission of the solitary wave, which demonstrates that the present approach can  
 486 efficiently resolve its interactions with the pontoon.

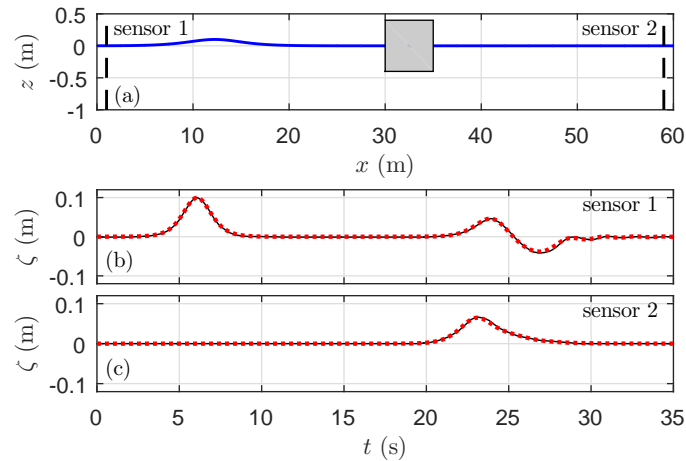


Figure 8: Set-up of the solitary wave test case and snapshot of the free surface at  $t = 10$  s (a), and the time series of the free-surface elevation at the two wave sensors (b and c). The black line indicates the solution of the 20 layer model of Lin (2006), and the dotted red line indicates the solution of the 2 layer SWASH model.

487 **5. Scattering of regular waves by a pontoon**

488 The third test case considers the scattering of regular waves by a rectangular pontoon that was located  
 489 inside a wave basin (Wang et al., 2011), see Fig. 9 for an overview of the laboratory set-up. The basin had  
 490 a constant depth of 0.3 m, except for a deep water region near the wavemaker. The pontoon was restrained  
 491 by four tripods; and had a width of 0.6 m, a length of 2 m, and a draft of 0.24 m. A total of 14 wave  
 492 sensors were positioned in the vicinity of the pontoon to measure the surface elevation. A wave absorber  
 493 was positioned along the right boundary of the wave basin, to minimise wave reflections. In this experiment,  
 494 a total of six wave conditions were forced at the wavemaker, which varied in wave period ( $T = 1.5, 2,$  and  
 495  $3$  s) and wave height ( $H = 3,$  and  $6$  cm). Here, we consider the steepest wave condition and the weakest  
 496 nonlinear wave condition of this experiment (i.e., a wave with  $H = 6$  cm and  $T = 1.5$  s, and a wave with  
 497  $H = 3$  cm and  $T = 3$  s, respectively).

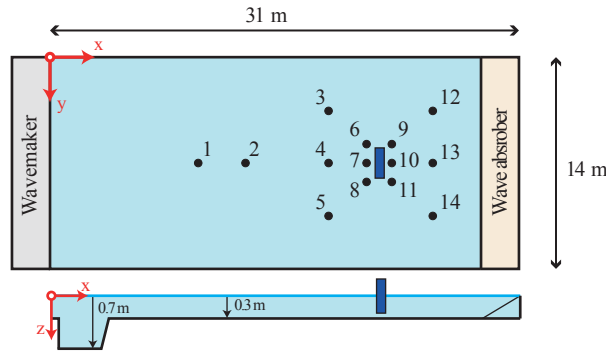


Figure 9: Overview of the experimental set-up. The numbered blue markers indicate the location of the wave sensors, and the blue rectangle indicates the position of the pontoon.

498 The spatial and temporal resolution of the SWASH model were chosen based on the wave characteristics.  
 499 The grid resolution was set at  $\Delta x = \Delta y = 0.05$  m, corresponding to at least 50 points per wave length.  
 500 The temporal resolution was set at 100 points per wave period, which resulted in  $\Delta t = 0.015 - 0.03$  s. Two  
 501 vertical layers were used, which is sufficient to capture the wave dispersion for the range of normalised water  
 502 depths encountered in the deep water region (which varied between  $0.6 - 1.4$ ). A sponge layer of 5 m width  
 503 was positioned along the right boundary of the basin to dissipate incoming waves.

504 *5.1. Results*

505 Fig. 10 shows the time series of the measured and predicted (normalised) surface elevation for the two  
 506 wave conditions of this test case. They depict the surface elevation for 6 wave periods, after the initial waves  
 507 have reached sensors 12-14. In this test case, waves are reflected and transmitted by the pontoon, and wave  
 508 diffraction occurs in the lee of this body. For the steepest wave case, the first waves reached sensors 12-14

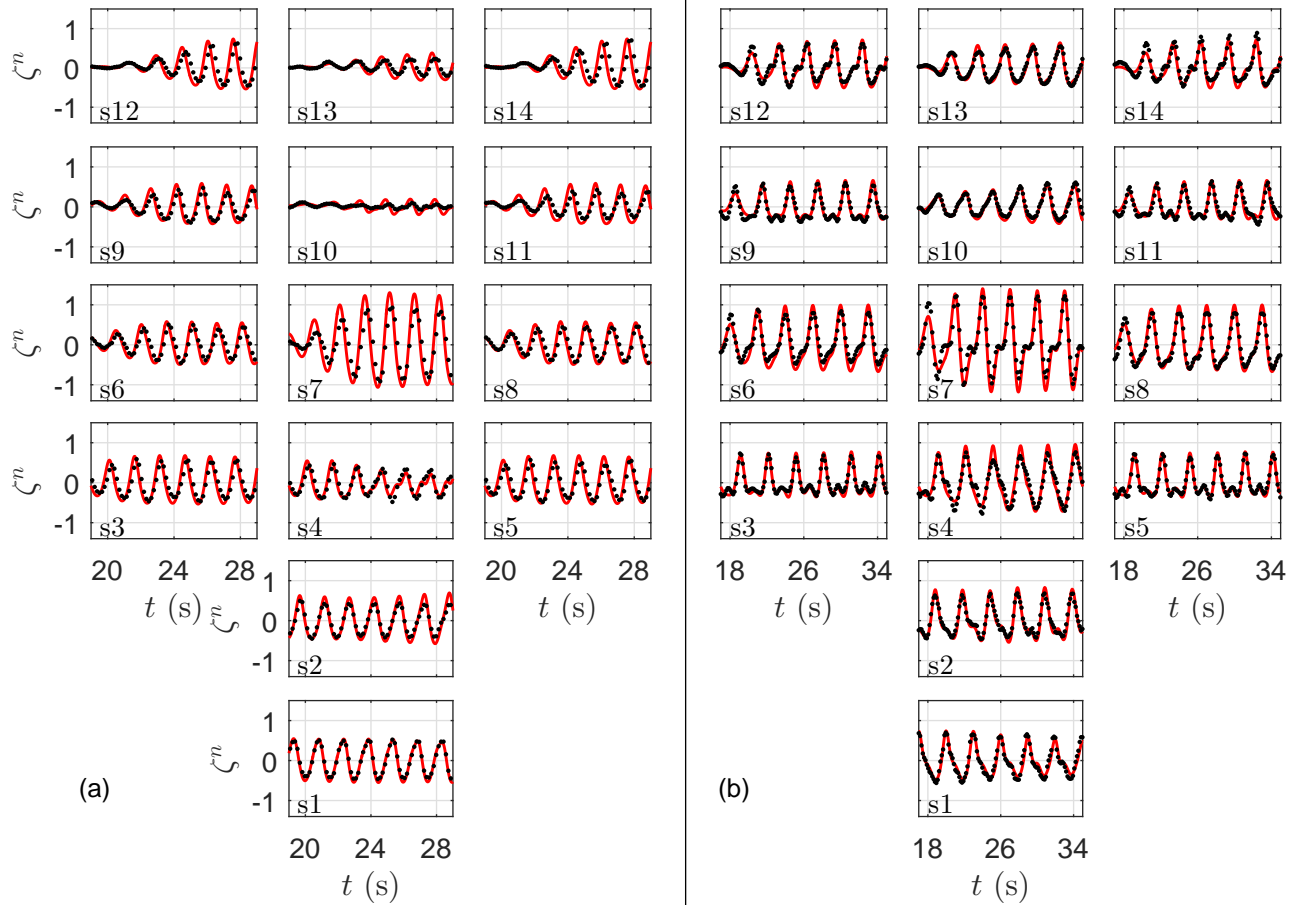


Figure 10: Time series of the surface elevation normalised by the incident wave height ( $\zeta^n$ ) at the 14 wave sensors for the steepest wave condition (a), with  $H = 6$  cm and  $T = 1.5$  s, and for the weakest nonlinear wave condition (b), with  $H = 3$  cm and  $T = 3$  s. The black dots indicate the measurements, and the red and blue line indicates the model predictions for the steep and weakly nonlinear condition, respectively. In each subplot, the number indicates the position of the respective wave sensor. Please note that the subplots are arranged according to the position of the respective wave sensor in the wave basin.

509 after approximately 20 s (Fig. 10a). For this relatively short-wave period, the waves reflected significantly  
510 at the pontoon and the wave transmission was very small, which is illustrated by the high wave elevation  
511 at sensor 7 and the low elevation at sensor 10. Due to the diffraction of waves in the lee of the pontoon,  
512 the wave elevation at sensor 13 is larger compared to the signal at sensor 10. At all sensors, the predicted  
513 wave signals agree well with the measurements. A small phase difference between the measurements and  
514 the predictions can be observed at sensors 12-14 (where the wave field is progressive). This is attributed  
515 to a small difference between the analytical and numerical wave celerity ( $\sim 0.5\%$ ). For the simulation that  
516 considers a longer wave period, the waves experienced a stronger transmission and diffraction (Fig. 10b).  
517 The model reproduced the (irregular) wave elevation that was measured at all sensors, which illustrates that  
518 it captured this pattern. Overall, the model predictions agree well with the measurements of this laboratory

519 experiment. These results demonstrate that the model captures the scattering of regular waves, and the  
 520 diffraction in the lee of a rectangular pontoon.

## 521 6. Wave impact on a container ship

522 The last test case considers the wave impact on a restrained container ship for a range of wave conditions  
 523 (Bijleveld, 2004; Van der Molen, 2006). This experimental campaign was conducted in a wave basin that  
 524 measured approximately  $40 \times 40 \text{ m}^2$ . In the campaign, a restrained ship, located either in open water or  
 525 in a harbour basin, was subject to a range of wave conditions, including realistic short-crested sea states  
 526 (see Fig. 11 for a sketch of the experimental set-up). The still water depth in the basin was 0.2 m. To  
 527 prevent reflections at the side walls of the basin, gravel beaches were constructed along parts of the basin  
 528 boundaries. When the harbour basin was present, a gravel slope was positioned at the harbour wall that  
 529 faced the wavemaker to reduce reflections.

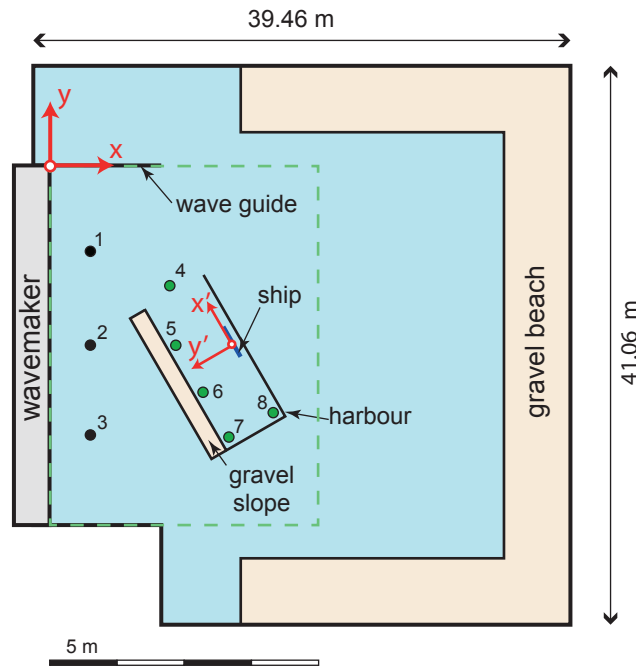


Figure 11: Overview of the laboratory set-up, including the harbour and the location of the ship. The numbered circles indicate the location of the wave sensors. Sensors 1-3 were present during all experiments, and sensors 4-8 were only available for the experiments which included the harbour basin. The thin dashed green line illustrates the region of interest.

530 The ship, a 1 : 100 scale model of a Panamax container ship, was restrained by six force transducers  
 531 that fixed the ship to a steel frame. Based on these transducers, the forces and moments were measured  
 532 relative to a ship coordinate system ( $x' - y'$ , illustrated in Fig. 11), in which the horizontal coordinates  
 533 are rotated with  $120^\circ$  relative to the global coordinate system ( $x - y$  in Fig. 11). With this set-up, small

Table 1: Wave parameters at the wavemaker for the irregular wave conditions of the experimental program. Listed are the wave height  $H_{m0}$ , the peak wave period  $T_p$ , the directional distribution of the wave spectrum  $D(\theta)$  (which was constant over the frequencies), and the duration of the experiment  $T_{exp}$ . The directional distribution is defined as  $D(\theta; f) = \frac{S_\zeta(f, \theta)}{S_\zeta(f)}$  (e.g., Holthuijsen, 2007), where  $S_\zeta(f, \theta)$  is the frequency-direction spectrum and  $S_\zeta(f)$  is the frequency spectrum of the surface elevation (see also Appendix B.1).  $D(\theta) = \delta$  corresponds to long-crested waves, in which  $\delta$  is the Dirac delta function. The mean wave angle of all wave conditions is perpendicular to the wavemaker.

	$H_{m0}$ (cm)	$T_p$ (s)	$D(\theta)$	$T_{exp}$ (min)
OWi1	1.5	1.0	$\delta$	30
OWi2	1.5	1.5	$\delta$	30
OWi3	1.5	1.0	$\cos^2(\theta)$	30
OWi4	1.5	1.5	$\cos^4(\theta)$	30
HBi1	3.0	1.0	$\delta$	45
HBi2	3.0	1.5	$\delta$	45
HBi3	3.0	1.0	$\cos^2(\theta)$	45
HBi4	3.0	1.5	$\cos^2(\theta)$	45

534 measurement errors in the forces can induce significant errors in the moments, and the roll moment in  
535 particular (e.g., Van der Molen, 2006). Nonetheless, we compare the model results and the measurements  
536 for all load components, but we anticipate that discrepancies are typically larger for the moments than for  
537 the forces. Several wave sensors were positioned inside the basin to measure the surface elevation. Near the  
538 wavemaker, three sensors were present for all simulations. For the simulations in which the harbour basin  
539 was present, five additional wave sensors were positioned in the vicinity of the ship (see Fig. 11).

540 Waves were forced using a piston-type wavemaker, including second-order wave control and reflection  
541 compensation. The wave conditions varied from monochromatic to short-crested waves. In this paper, we  
542 distinguish between the conditions in which the ship was moored in open water (labelled as OW) or inside  
543 the harbour basin (labelled HB). We consider a total of ten wave conditions: two regular wave conditions  
544 (labelled as OWr and HBr) and eight irregular wave conditions (with the label OWi and HBi). In the regular  
545 wave experiments, which had a duration of 10 min, a monochromatic wave was forced with an amplitude  
546 of 1 cm, a period of 1 s, and a direction perpendicular to the wavemaker. In the irregular experiments,  
547 both long-crested and short-crested wave fields were generated, of which the bulk wave parameters are listed  
548 in Table 1. In these test cases, the wave conditions differed mainly in the wave period, and in directional  
549 spreading. They varied from long-crested waves with a relatively long peak period (e.g., OWi2 and HBi2),  
550 to short-crested sea states with relatively short peak periods (e.g., OWi3 and HBi3).

551 Similar to the previous test cases, the temporal and spatial grid resolution of the model were chosen based  
552 on the characteristics of the wave conditions. Two vertical layers were sufficient to capture the dispersion of



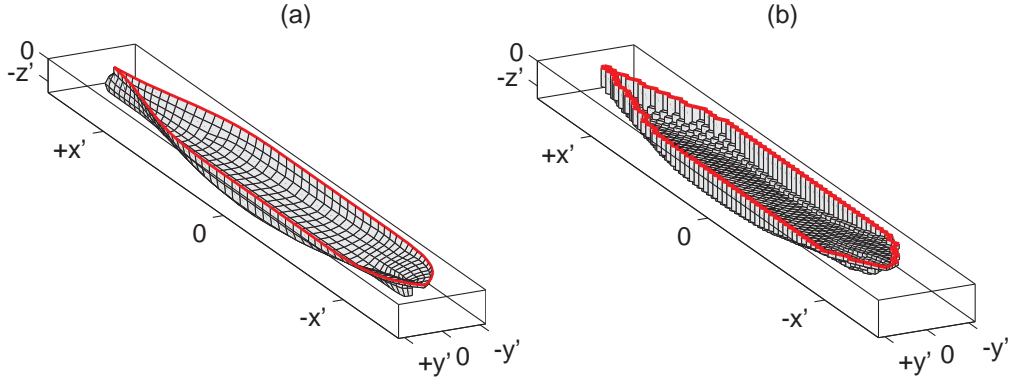


Figure 12: Sketch of the ship hull in the ship coordinate system. (a) Panel model of the Panamax ship. (b) Single valued ship function  $S(x', y')$  used in the SWASH computations. The thick red line in (a) and (b) indicates the waterline contour.

553 the dominant waves (for which the  $kd$  values ranged  $0.6 - 3.2$ ). The grid resolution was set at  $\Delta x = 0.02$  m  
554 and  $\Delta y = 0.035$  m, which corresponds to at least 20 points per wave length for frequencies up to  $2f_p$ , where  
555  $f_p (= 1/T_p)$  is the peak frequency. The time step was set at 0.01 s, which corresponds to at least 50 points  
556 per wave period for frequencies up to  $2f_p$ . To reduce the computational effort, we reduced the domain size in  
557 both horizontal directions. The resulting numerical domain spans approximately  $30 \times 36$  m<sup>2</sup>. Furthermore,  
558 the grid resolution was set to increase linearly away from the region of interest (illustrated by the dashed  
559 green line in Fig. 11), with a maximum grid resolution of 0.25m. The Manning roughness coefficient was set  
560 at the default value used in SWASH,  $n = 0.019$  s/m<sup>1/3</sup>. Waves were generated at the numerical wavemaker  
561 using weakly nonlinear wave theory to include the bound infragravity waves (Rijnsdorp et al., 2015), based  
562 on the wave parameters of the laboratory experiment (e.g., Table 1). The model simulations were run with  
563 the same duration as the laboratory experiment, except for the regular wave conditions which were run for  
564 5 min (corresponding to  $\sim 300$  waves). The wave guides, harbour walls, and gravel slopes were schematised  
565 as a porous structure (see Appendix A for a brief description). The impermeable wave guides and harbour  
566 walls were schematised with a porosity equal to zero, and the gravel slopes were schematised with a porosity  
567 of 0.45, and a characteristic stone size of 2 cm.

568 In the numerical model, the hull of the ship is represented as a single valued function in  $x - y$  space.  
569 A panel model of the Panamax ship (Fig. 12a) was converted into a single valued function (Fig. 12b) by  
570 interpolating the panel elements that were located within the waterline contour to the computational grid  
571 used in SWASH. Because the ship is represented as a single valued function in  $x - y$  space, the bulbous bow  
572 of the ship is not included in this schematisation. This model limitation will likely affect the predictions of  
573 the hydrodynamic loads that act on the body, as the bulbous bow alters the flow field in the vicinity of the  
574 ship (e.g., Bertram, 2012).

575 Animations of the simulated wave field for OWi1 and HBi4 are included in the supplementary material.

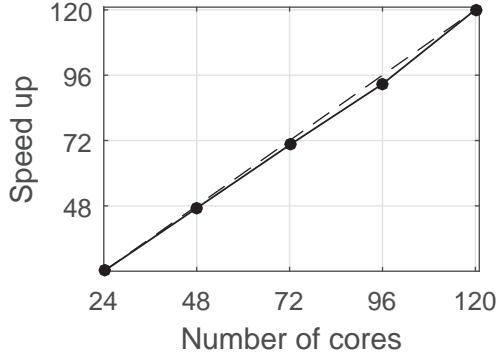


Figure 13: Scaling of the Cartesius supercomputer (40960 Intel Xeon cores, 2.4 – 2.6GHz with 64GB internal memory). The line with the markers represents the model speed up. The dashed line illustrates a linear speed up (i.e., if the number of cores is doubled the computational time is halved).

576 Although the set-up of this experiment is relatively simple, it provides a demanding test case for the numerical  
577 model as it includes many features that are representative for a real harbour. For example, it includes the  
578 reflection and diffraction of waves by the presence of quay walls, and a realistic ship model. Furthermore,  
579 the size of the domain and the duration of the simulation are representative for a realistic harbour or coastal  
580 region. At prototype scale, this experimental set-up corresponds to a domain that spans approximately  $4 \times 4$   
581 km (20 – 30 dominant wave lengths), and a duration of 5 – 7.5 hr (1200 – 2700 dominant wave periods).  
582 Given these scales, all simulations of this laboratory experiment were ran with 120 cores on Cartesius, the  
583 Dutch national supercomputer. The model showed an excellent parallel scaling on Cartesius (Fig. 13). The  
584 regular wave simulations took on average 4 hr to run, and the irregular wave simulations took on average  
585 32 hr to run. This makes the computational effort significant, but viable on present day multi-processor  
586 machines.

### 587 6.1. Results

588 The model results and measurements are compared based on time series for the regular wave conditions,  
589 and based on spectral results for the irregular wave conditions. We compared spectral results for the irregular  
590 wave conditions instead of time series as they allow us to gain more insight in the frequency dependence of  
591 the wave field and the hydrodynamic loads. In the following, we will focus on the results of the irregular sea  
592 states. The results of the two regular wave conditions can be found in Appendix C.

593 To assess the model performance quantitatively, several bulk parameters were computed: the root-mean-  
594 square wave height ( $H_{rms}$ ) and the mean wave period ( $T_{m02}$ ) for the wave field, and the bulk load (e.g.,  
595  $F_{x',rms}$ ) and mean load period (e.g.,  $F_{x',m02}$ ) for the hydrodynamic loads (see Appendix B.1). Based on these  
596 bulk parameters, two statistical measures were computed to quantify the model performance: the relative  
597 bias RB and the scatter index SI (see Appendix B.2). In this work, we qualify the model-data agreement

598 as follows: measures  $< 15\%$  are considered good, measures between  $15\%$  and  $30\%$  indicate reasonable  
 599 agreement, and measures  $> 30\%$  indicate significant discrepancies.

600 First, we discuss detailed spectral results of the surface elevation and hydrodynamic loads for two rep-  
 601 resentative simulations. These two simulations represent the results with the best and the worst overall  
 602 scatter index (SI). This overall SI was computed by averaging the SI over all bulk parameters. The first  
 603 simulation (case OWi4) corresponds to the lowest SI value (best comparison), and the second (case HBi3)  
 604 corresponds to the highest SI value (worst comparison).

605 For the simulation with the lowest scatter index (OWi4), the ship was moored in open water and subject  
 606 to a short-crested wave field (Table 1). The model reproduced the typical shape and the energy levels of  
 607 the surface elevation spectra  $S_\zeta$  near the wavemaker (Fig. 14a), except for an over prediction near  $f_p$ . This  
 608 is confirmed by the bulk wave parameters ( $|RB| < 0.08$ ). The predicted and observed wave spectra are  
 609 comparable to the target wave spectrum (depicted by the dash-dot gray line in Fig. 14a). This indicates  
 610 that the wave field was dominated by the waves generated at the wavemaker, and that the influence of waves  
 611 reflected at the ship was relatively small. Therefore, these results illustrate that the wavemaker in the model

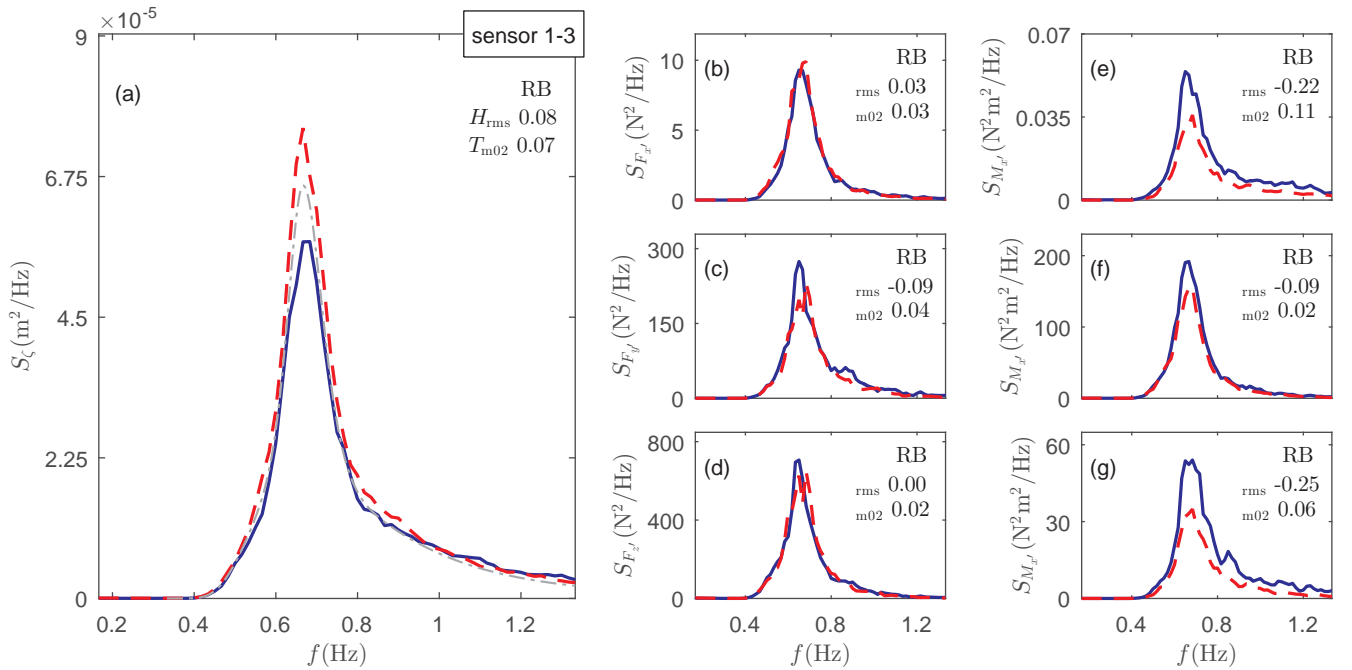


Figure 14: Predicted (red line) and observed (blue line) spectra of the surface elevation  $S_\zeta$  (a), and the forces  $S_F$  (b-d) and moments  $S_M$  acting on the ship (e-g) for OWi4. The surface elevation spectra plotted in panel (a) is the average of the spectra at sensor 1-3. In panel (a), the thin dash-dot gray line indicates the target JONSWAP spectrum with which the physical and numerical wavemakers were forced. In each panel, the relative bias (RB) of the two bulk parameters are depicted in the top right corner. For brevity, the bulk loads are denoted with  $\text{rms}$ , and the mean load periods are denoted with  $\text{m02}$ .

612 reproduced the wave field that was generated in the laboratory experiment.

613 The spectral shape of the observed force and moment spectra is similar to  $S_\zeta$  (Fig. 14b-g versus Fig.  
 614 14a). The predicted force and moment spectra generally agree well with the measurements, especially for  
 615 the three force components and the pitch moment ( $M_{y'}$ ). This is confirmed by the low RB values of their  
 616 bulk parameters ( $|\text{RB}| < 0.09$ ), which indicate that they were reproduced with a similar accuracy as that  
 617 of the wave field. In contrast, the predicted  $M_{x'}$  and  $M_{z'}$  show bigger discrepancies as their spectral levels  
 618 are under predicted. Nonetheless, their spectral shape was reproduced well and their bulk parameters were  
 619 predicted with reasonable accuracy ( $|\text{RB}| < 0.25$ ).

620 In HBI3, the ship was moored inside the harbour and subject to a short-crested wave field (Table 1). The  
 621 predicted spectra and bulk wave parameters agree with the measurements near the wavemaker (Fig. 15a).  
 622 Here, the wave field is dominated by the waves generated at the wavemaker as the spectra compare well with  
 623 the target wave spectrum. In the harbour basin, the predicted and observed wave spectra and bulk wave  
 624 parameters are in good agreement ( $\text{RB} \leq 0.11$ ), although discrepancies were generally larger compared to

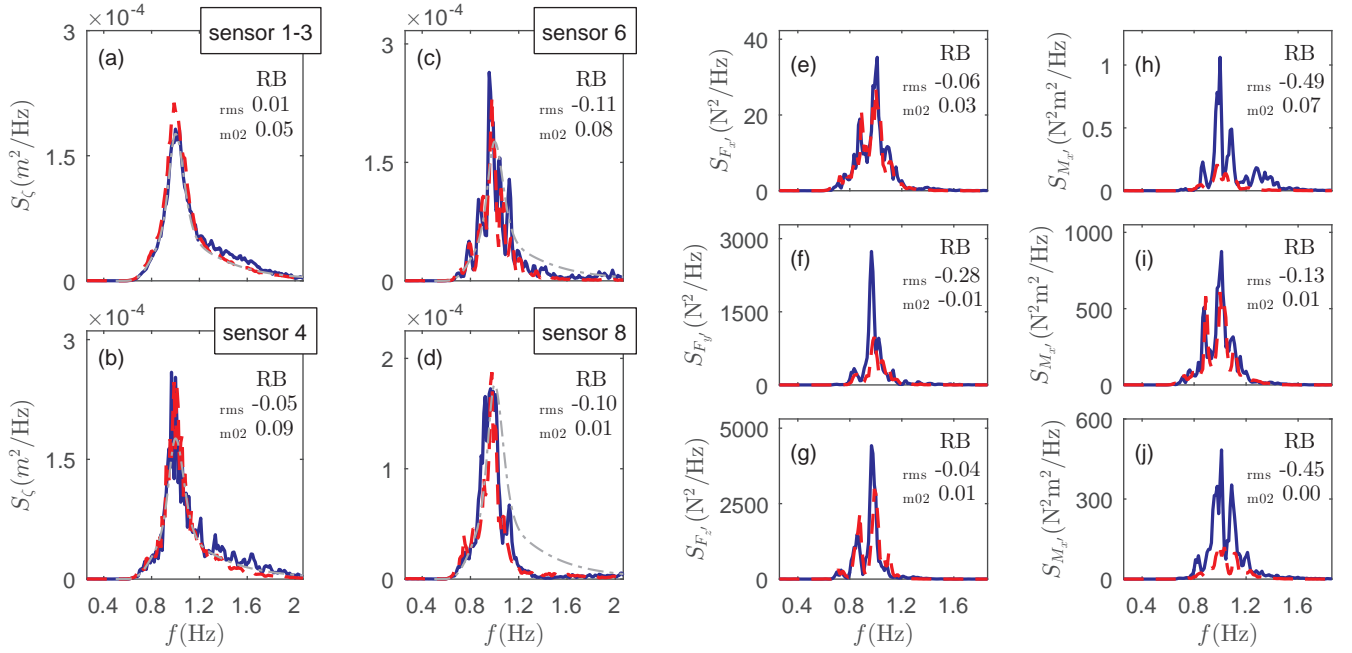


Figure 15: Predicted (red line) and observed (blue line) spectra of the surface elevation  $S_\zeta$  (a-d), and the forces  $S_F$  (e-g) and moments  $S_M$  acting on the ship (h-j) for HBI3. The plotted surface elevation spectra in panel (a) is the average of the spectra at sensor 1-3. The surface elevation spectra in panel (b-d) are the results at sensors 4, 6, and 8, respectively (see Fig. 11 for the sensor positions). In panel (a-d), the thin dash-dot gray line indicates the target JONSWAP spectrum with which the physical and numerical wavemakers were forced. In each panel, the relative bias (RB) of the two bulk parameters are depicted in the top right corner. For brevity, the bulk wave heights and loads are denoted with  $\text{rms}$ , and the mean wave and load periods are denoted with  $\text{m02}$ .

625 the results at the sensors near the wavemaker. Furthermore, the model captured the irregularity of the wave  
 626 spectra, which is indicative for the occurrence of a (partially) standing wave field. These results show that  
 627 the model captures the overall wave field in the harbour.

628 Overall, the spectral shape and the spectral levels were reproduced well for the three force components  
 629 (Fig. 15e-g), including most of the distinct spectral features (e.g., the additional peaks in  $F'_z$ , see Fig.  
 630 15g). The forces on the moored ship were reproduced with larger discrepancies compared to the wave field,  
 631 although the errors in the bulk parameters were of similar order ( $|RB| \leq 0.28$  versus  $RB \leq 0.11$ ). In contrast  
 632 with the forces, the moments were predicted with significant errors (Fig. 15h-j). Only  $M'_y$  was reproduced  
 633 well (Fig. 15i), both in terms of the irregular spectral shape and the bulk moment parameters (for which  
 634  $|RB| \leq 0.13$ ).

635 To present the main findings of this test case, Fig. 16 and Table 2 show a comparison between the  
 636 predicted and measured bulk parameters for all conditions that were considered. Near the wavemaker, the  
 637 predicted  $H_{\text{rms}}$  agree well with the measurements (blue dots in Fig. 16a). Inside the harbour basin, the

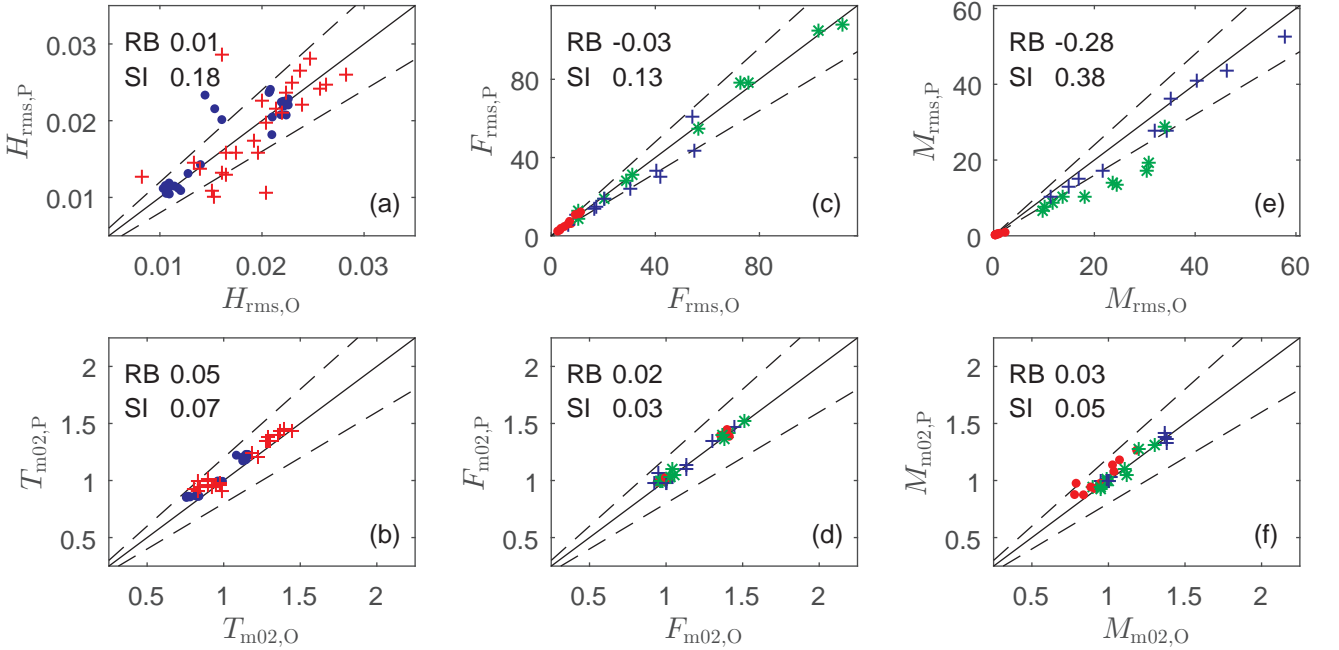


Figure 16: Predicted (subscript P) versus observed (subscript O) wave height  $H_{\text{rms}}$  (a), mean wave period  $T_{\text{m02}}$  (b), bulk force  $F_{\text{rms}}$  (c), mean force period  $F_{\text{m02}}$  (d), bulk moment  $M_{\text{rms}}$  (e), and mean moment period  $M_{\text{m02}}$  (f). The solid black line indicates perfect agreement, and the dashed black lines indicate the 20% error bands. In each panel, the overall relative bias (RB) and scatter index (SI) are printed in the top left side. In panel (a) and (b), results of a sensor located outside the harbour are indicated by a blue dot, and results of a sensor located inside the harbour are indicated by a red plus. In panel (c-f), the color and type of the marker indicates the direction of the parameter. That is, a red dot indicates the  $x'$  component, a blue plus the  $y'$  component, and a green asterisk the  $z'$  component.

638 scatter is typically larger (red pluses in Fig. 16a). Overall, the model reproduced the wave height with a  
639 scatter of 18%. Note that the average RB is smaller than SI, because  $H_{\text{rms}}$  is both over and under predicted.  
640 The outliers in Fig. 16a correspond to case HBr (see Fig. C.2). The model systematically over predicted  
641  $T_{\text{m02}}$  with a relatively small bias of 5% (Fig. 16b), and there is no clear difference between predictions outside  
642 or inside the harbour. Overall, the discrepancies between the predictions and measurements are larger in  
643 subset HB than in OW (Table 2). This is likely related to the increased complexity of the conditions in  
644 subset HB, as a standing wave pattern occurred inside the harbour basin.

645 The bulk forces and the mean force periods were predicted with an accuracy that is comparable to the  
646 wave field (Fig. 16c-d). The  $F'_z$  and  $F'_y$  force components were typically an order of magnitude larger than  
647  $F'_x$ , whereas their mean periods were similar. These trends were reproduced well by the model. Overall,  $F'_z$   
648 was reproduced with good statistical agreement ( $SI \leq 0.05$ , see Table 2). Discrepancies were larger for the  
649 horizontal force components  $F'_x$  and  $F'_y$ , which were in reasonable agreement with the measurements ( $SI \leq$   
650  $0.12$  and  $SI \leq 0.22$ , respectively, see Table 2). In contrast to the forces, the bulk moments were predicted  
651 with significant deviations (Fig. 16e), although their mean periods agreed well (Fig. 16f). Discrepancies

Table 2: Statistical measures (relative bias RB, and scatter index SI) of the wave parameters (significant wave height and mean wave period), and the hydrodynamic loads (forces and moments) for the simulations with a ship moored in open water (OW), a ship moored inside a harbour basin (HB), and for all simulations combined (Overall).

	OW		HB		Overall	
	RB	SI	RB	SI	RB	SI
$H_{\text{rms}}$	0.02	0.12	0.01	0.19	0.01	0.18
$T_{\text{m02}}$	0.06	0.07	0.05	0.07	0.05	0.07
$F'_{x,\text{rms}}$	-0.09	0.14	0.07	0.10	0.02	0.12
$F'_{y,\text{rms}}$	-0.10	0.14	-0.13	0.20	-0.12	0.22
$F'_{z,\text{rms}}$	-0.01	0.07	0.01	0.04	0.00	0.05
$M'_{x,\text{rms}}$	0.22	0.24	-0.48	0.59	-0.42	0.63
$M'_{y,\text{rms}}$	-0.16	0.19	-0.05	0.08	-0.09	0.11
$M'_{z,\text{rms}}$	-0.34	0.44	-0.34	0.36	-0.34	0.39
$F'_{x,\text{m02}}$	0.02	0.02	0.01	0.02	0.01	0.02
$F'_{y,\text{m02}}$	0.04	0.05	-0.01	0.02	0.02	0.04
$F'_{z,\text{m02}}$	0.03	0.03	0.01	0.01	0.02	0.02
$M'_{x,\text{m02}}$	0.11	0.12	0.06	0.06	0.08	0.10
$M'_{y,\text{m02}}$	0.01	0.02	0.00	0.03	0.01	0.02
$M'_{z,\text{m02}}$	0.03	0.04	-0.02	0.04	0.00	0.04

652 were typically largest for the  $M'_x$  and  $M'_z$  moment ( $SI \leq 0.63$  and  $SI \leq 0.39$ , respectively), whereas  $M'_y$   
653 was reproduced with an SI that is comparable to the forces (see Table 2). These findings mirror the results  
654 of the individual force components. For example, the error in  $M'_x$  (which depends on  $F'_y$  and  $F'_z$ ) is larger  
655 than the error in  $M'_y$  (which depends on  $F'_x$  and  $F'_z$ ) as the error in  $F'_y$  is larger than the error in  $F'_x$  (see  
656 Table 2). These results highlight the sensitivity of the moments to relatively small discrepancies in the  
657 force predictions. Although the errors in the predicted moments were significant, the model captured the  
658 variation of the bulk moments for the variety of wave conditions that were considered in this work (Fig.  
659 16e).

660 To summarise, these findings show that the wave-induced forces were predicted with an accuracy that  
661 is comparable to the wave field, whereas the moments were predicted with more significant discrepancies.  
662 This is not surprising given the relatively coarse schematisation of the ship's hull (e.g., the bulbous bow was  
663 not included in the simulations), and to difficulties in measuring the moments that act on a restrained ship  
664 (e.g., Van der Molen, 2006). Overall, the results of this test case demonstrate the potential of the model  
665 in seamlessly simulating the wave field in the basin, their interactions with the restrained ship, and the  
666 resulting hydrodynamic loads that act on the body.

## 667 7. Discussion

668 This paper presents a new numerical approach to simulate the nonlinear evolution of waves and their  
669 impact on a restrained ship at the scale of a realistic harbour or coastal region. This model is based on  
670 the non-hydrostatic approach, and the SWASH model in particular, which is in essence a direct numerical  
671 implementation of the RANS equations. The use of the Keller-Box scheme to discretise the non-hydrostatic  
672 pressure allows such models to efficiently resolve a range of nearshore wave and flow phenomena. To include  
673 the interactions between the waves and the ship, we developed a new method to account for the presence  
674 of a floating body in the non-hydrostatic approach. The findings of this work demonstrated that the  
675 model captures the scattering of regular waves and a solitary wave by a rectangular pontoon. Furthermore,  
676 the model gave a reasonable prediction of the magnitude and periodicity of the hydrodynamic loads on a  
677 restrained container ship for a range of realistic wave conditions. Most importantly, this work demonstrated  
678 that a coarse vertical resolution sufficed to capture these interactions, which highlights that the model retains  
679 this favourable property of the non-hydrostatic approach when a floating body is included.

680 Compared to the variety of models that have been developed to solve the wave-ship interactions (e.g.,  
681 Newman, 2005; Hadžić et al., 2005; Yan and Ma, 2007; Bouscasse et al., 2013), the primary advantage of the  
682 present approach is that it does not rely on predictions of the wave field in the vicinity of the moored ship.  
683 To date, the most advanced methodology that was developed to solve both the evolution of waves and their  
684 impact on a moored ship coupled a wave model based on the Boussinesq or non-hydrostatic approach with

685 a panel model (Bingham, 2000; Van der Molen and Wenneker, 2008; Dobrochinski, 2014). This coupled  
686 approach includes a detailed schematisation of the ship’s hull, but is restricted to relatively mild wave  
687 conditions, whereas the present approach makes no a-priori assumptions concerning the nonlinearity of the  
688 wave field, but is limited to a relatively coarse ship schematisation. Although a direct comparison between  
689 these two methods was not the subject of this work, we can make an indirect comparison based on the  
690 work of Dobrochinski (2014). In this study, a coupled model (combining SWASH and a panel model) was  
691 validated for several wave conditions belonging to the same laboratory experiment that was considered in  
692 the present work (§6). Overall, the discrepancies in the hydrodynamic load predictions of this coupled model  
693 are comparable to the results presented here (§6.1). This suggests that the accuracy of these two methods  
694 is similar for these experimental conditions.

695 The key features of the present approach are thus that (i) it can relatively efficiently resolve the evolution  
696 of waves in coastal waters (Zijlema et al., 2011; Smit et al., 2013, 2014), including the infragravity waves  
697 which are known to disrupt harbour operations (Rijnsdorp et al., 2014, 2015; De Bakker et al., 2016),  
698 and (ii) that it can seamlessly account for the interactions between the waves and a restrained ship. This  
699 demonstrates that the model provides a promising new alternative to simulate the nonlinear evolution of  
700 waves and their impact on a restrained ship at the scale of a harbour or coastal region. Based on these  
701 considerations, we believe that this work provides a crucial first step towards the development of a new  
702 approach to simulate the wave-induced response of a ship that is moored in coastal waters.

703 So far, the model was used to simulate the wave impact on a restrained ship under idealised conditions  
704 (e.g., relatively mild waves, and a relatively simple harbour layout). Further research is therefore required  
705 to push the capabilities of the approach towards more realistic conditions. This includes an assessment of  
706 the model capabilities for more challenging environments, for example, in a complex coastal region or in  
707 the case of significant nonlinear wave effects. Furthermore, future work can be undertaken to resolve the  
708 actual wave-induced motions of a moored ship, and to improve the accuracy of the model in resolving the  
709 wave-ship interactions. In this study, the model was applied with a relatively coarse vertical resolution,  
710 which permits applications at relatively large scale. On the other hand, this implies that the model does  
711 not resolve the details of the vertical flow structure in the vicinity of the ship, which are likely important  
712 in the case of energetic wave conditions (or significant ship motions) when turbulent effects are significant.  
713 Given the flexibility of the non-hydrostatic approach (in contrast to the coupled wave-panel methodology),  
714 resolving such features merely requires an increase of the vertical resolution near the ship combined with  
715 the use of a proper turbulence model. For example, by implementing a domain decomposition technique,  
716 the model can retain its favourable features in simulating nonlinear waves at large scales, while it at the  
717 same time can resolve the vertical flow structure in the vicinity of the moored ship.



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724 **Appendix A. Porous flow**

725 To account for the flow through a porous structure, the governing equations are adapted in accordance  
 726 with Madsen (1983). In SWASH, only the global continuity and the horizontal momentum equation are  
 727 adapted to include the effect of the flow through a porous structure, whereas the vertical momentum equation  
 728 is not adapted. Although an inclusion of the porous influence in the vertical momentum equation is likely  
 729 more accurate (e.g., Higuera et al., 2014; Ma et al., 2014a; Jacobsen et al., 2015), we are not primarily  
 730 interested in the flow through a porous medium. We merely mimic the dissipation induced by a gravel  
 731 beach, and the reflections induced by impermeable walls, for which this approach is expected to be sufficiently  
 732 accurate.

733 The modified equations in the outer domain read,

$$\begin{aligned}
 734 \quad n \frac{\partial \zeta}{\partial t} + \frac{\partial HU}{\partial x} &= 0, \\
 735 \quad \frac{\partial u_n}{\partial t} + \frac{\partial u_n u_n}{\partial x} + \frac{\partial wu}{\partial z} &= -g \frac{\partial \zeta}{\partial x} - \frac{\partial p}{\partial x} + \frac{\partial \tau_{xx}}{\partial x} + \frac{\partial \tau_{xz}}{\partial z} - f_l u - f_t u |u|,
 \end{aligned}$$

736 where  $n$  is the porosity,  $u_n (= \frac{u}{n})$  is the seepage velocity inside a porous medium,  $f_l$  is a laminar friction  
 737 factor, and  $f_t$  is a turbulent friction factor. The friction factors are given by (e.g., Madsen, 1983),

$$\begin{aligned}
 738 \quad f_l &= \alpha_e \frac{(1-n)^3}{n^2} \frac{\nu}{D}, \\
 739 \quad f_t &= \beta_e \frac{1-n}{n^3} \frac{1}{D},
 \end{aligned}$$

740 where  $\nu$  is the kinematic viscosity of water,  $D$  is a characteristic stone size, and  $\alpha_e$  and  $\beta_e$  are empirical  
 741 coefficients. In this study, the empirical coefficient were set at their default values ( $\alpha_e = 1000$ , and  $\beta_e = 2.8$ ).

742 **Appendix B. Quantitative model-data comparison**

743 *Appendix B.1. Bulk parameters*

744 To quantify the model performance for the laboratory experiment of §6, we computed several bulk  
 745 parameters that represent the wave conditions inside the laboratory basin, and the hydrodynamic loads that

746 act on the ship. We characterise the wave conditions using the root mean square wave height  $H_{\text{rms}} = \sqrt{8m_0}$   
747 and the mean wave period  $T_{m_{02}} = \sqrt{m_0/m_2}$ , in which  $m_n = \int f^n S_\zeta(f)df$ , and  $S_\zeta(f)$  is the surface elevation  
748 spectrum. The  $H_{\text{rms}}$  provides a measure of the total wave energy, and  $T_{m_{02}}$  provides a measure of the mean  
749 wave period. Furthermore,  $T_{m_{02}}$  gives some information on the frequency distribution of the wave energy.  
750 Similar to the bulk wave parameters, we computed bulk parameters for the hydrodynamic loads to gain  
751 insight in the overall forces and moments acting on the ship. The bulk parameters were computed for each  
752 individual component, following the same methodology as the wave height and the mean wave period. For  
753 example, the bulk force in  $x'$  direction is computed as  $F_{x',\text{rms}} = \sqrt{8m_0}$ , in which  $m_0 = \int S_{F_{x'}}(f)df$ , and  $S_{F_{x'}}$   
754 is the spectrum of  $F_{x'}$ . All spectra were computed with 60 degrees of freedom, based on ensemble averaged  
755 Fourier-transforms of detrended and windowed signals. To account for the spin-up time of the model and  
756 the measurements, the first 80 s of the signals was excluded in the case of a regular wave experiment, and  
757 the first 120 s were excluded in the case of an irregular wave experiment (see §6 for a description of the  
758 experiments).

## 759 *Appendix B.2. Statistical measures*

760 We quantified the model performance with two statistical measures: the relative bias, and the scatter  
761 index. The relative bias is computed as,

$$762 \quad \text{RB} = \frac{\sum_{i=1}^N (Q_p^i - Q_o^i)}{\sum_{i=1}^N Q_o^i}, \quad (\text{Appendix B.1})$$

763 and the scatter index is computed as,

$$764 \quad \text{SI} = \frac{\sqrt{\frac{1}{N} \sum_{i=1}^N (Q_p^i - Q_o^i)^2}}{\frac{1}{N} \sum_{i=1}^N Q_o^i}, \quad (\text{Appendix B.2})$$

765 where  $Q_p$  is a predicted parameter, and  $Q_o$  is an observed parameter in a sample of size  $N$ . We computed  
766 these statistical measures for the parameters of several groups of simulations. In total we considered three  
767 groups, of which one represents all simulations, and of which the two others represent the two simulation  
768 subsets (OW and HB). The measures were computed for each bulk parameter of the forces and moments  
769 (e.g.,  $F_{x',\text{rms}}$ ), by taking the summation over the simulations belonging to a group (i.e.,  $N = 5$  for group  
770 OW and HB, and  $N = 10$  for the group that contains all simulations). For the wave heights and mean  
771 periods, the measures were computed by taking the summation over all available wave measurements in the  
772 group.

773 **Appendix C. Regular wave impact on a container ship**

774 *Appendix C.1. Open water*

775 First, we compare predictions and measurements of the surface elevation and hydrodynamic loads for  
 776 OWr, in which the moored ship was subject to a monochromatic wave. In this experiment, the first waves  
 777 arrived at the wave sensors after approximately 10 s (Fig. C.1a-c), and about 10 s later they reached  
 778 the moored ship (Fig. C.1d-i). The signals are roughly sinusoidal for  $t > 60$  s, which indicates that the  
 779 conditions became approximately stationary. Due to the orientation of the ship with respect to the wave  
 780 direction, the sway force ( $F_{y'}$ ) is slightly larger compared to the surge force ( $F_{x'}$ ). Furthermore, the pitch  
 781 and yaw moment ( $M_{y'}$  and  $M_{z'}$ , respectively) are an order of magnitude larger compared to the roll moment

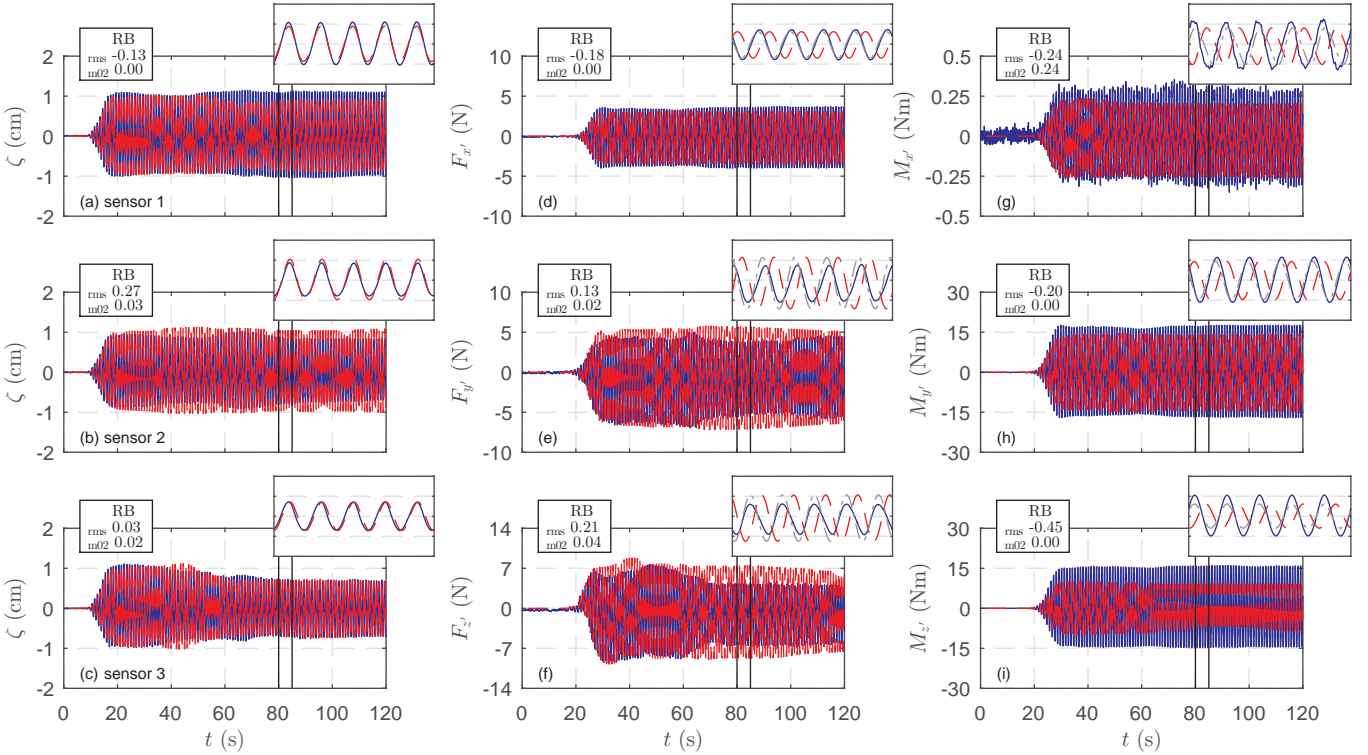


Figure C.1: Predicted (dashed red line) and observed (blue line) time series of the surface elevation  $\zeta$  (a-c), and the forces  $F$  (d-f) and moments  $M$  acting on the ship (g-i) for the first two minutes of simulation OWr. The insets adjacent to the main panels show a close up of the results for  $80 \leq t \leq 85$  s (illustrated by the two vertical black lines in the main panels). To facilitate a comparison between the predicted and observed hydrodynamic load signals, the dash-dot gray line in the insets of (d-i) shows the predicted hydrodynamic load signal including a time shift of  $-0.35$  s. In each panel, the relative bias (RB) of the two bulk parameters are depicted in the top left corner. In panel (a-c), the RB of the wave height  $H_{\text{rms}}$  and the mean wave period  $T_{\text{m02}}$  are shown. In panel (d-i), the RB of the bulk hydrodynamic loads (e.g.,  $F_{x',\text{rms}}$ ) and the mean period of the loads (e.g.,  $F_{x',\text{m02}}$ ) are shown. For brevity, the bulk loads are denoted with  $_{\text{rms}}$ , and the mean load periods are denoted with  $_{\text{m02}}$ . Note that in this case the scatter index is equal to the absolute value of RB.

782 ( $M_{x'}$ ). Note that the  $M_{x'}$  signal is relatively noisy, as its measurements suffer from significant inaccuracies  
783 (e.g., Van der Molen, 2006).

784 The model reproduced the typical surface elevation signal at the wave sensors (Fig C.1a-c), and the  
785 predicted wave height and wave period were in reasonable agreement with the measurements ( $|\text{RB}| \leq 0.27$ ).  
786 The agreement appears best at the start of the simulation ( $t < 30$  s), when the wave field at the sensors  
787 was progressive. This illustrates that the model reproduced the monochromatic wave that was generated at  
788 the numerical wavemaker. For  $t > 30$  s, discrepancies between the predicted and observed surface elevation  
789 signals can be observed at all wave sensors. At this time, the waves that were reflected at the ship and at  
790 the wave guides reached the wavemaker and were (partly) absorbed. These discrepancies are in part related  
791 to errors in the scattering of waves at the ship, and to differences between the absorption characteristics of  
792 the physical and numerical wavemaker.

793 The discrepancies between the predicted and measured load signals are typically larger compared to the  
794 surface elevation signals, especially for  $M_{z'}$  (which is under predicted with 44%, see Fig. C.1i). Furthermore,  
795 the predicted signals are shifted in time with respect to the measurements. Applying the same time shift  
796 of  $-0.35$  s to all load signals (illustrated by the dash-dot gray line in the insets of Fig. C.1d-i), the phases  
797 of the predicted loads are comparable to the measurements. This shows that the predicted hydrodynamic  
798 loads experience the same phase shift, indicating that the relative phasing of the individual load components  
799 is correct. The negative phase difference, which is only a small fraction of the time required for the waves to  
800 reach the moored ship ( $\sim 4\%$ ), cannot be explained by the error in the numerical wave celerity. Although the  
801 actual reason remains unclear, we hypothesise that this time shift (or spatial shift)<sup>3</sup> is related to a difference  
802 between the position of the ship in the laboratory and in the numerical model, and the relatively coarse  
803 schematisation of the hull (e.g., the bulbous bow is excluded in the model). However, the model reproduced  
804 the global arrival time of the waves at the ship as the load signals become non-zero at approximately the same  
805 moment in time (Fig C.1d-i). Furthermore, the model captured the order of magnitude and the periodicity  
806 of the individual load components, including their mutual dependence (e.g.,  $M'_x \ll M'_y$ , and  $M'_y \sim M'_z$ ).

### 807 *Appendix C.2. Harbour basin*

808 In HBr, the ship which is moored inside the rectangular harbour basin is subject to the same monochro-  
809 matic wave as in OWr. Near the wavemaker, the predicted surface elevation signal compares well with the  
810 measurements for  $t < 25$  s, when the (progressive) wave field at the sensors was not yet disturbed by the  
811 waves reflected at the gravel slopes in front of the harbour walls, the wave guides, and the wavemaker (Fig.  
812 C.2a). For  $t > 25$  s, the predicted and observed signal became relatively stationary and the wave height  
813 is consistently over predicted (likely due to differences in the wave damping that is induced by the gravel  
814 slopes located in front of the harbour walls).

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<sup>3</sup>A time shift of 0.35 s is equivalent to a wave propagation distance of  $\sim 0.4$  m

815 Near the harbour entrance and inside the harbour basin, a (partially) standing wave field occurred  
816 due to wave reflections at the harbour walls and wave guides. Here, the conditions became approximately  
817 stationary for  $t > 80$  s (see Fig. C.2b-i). Near the harbour entrance at sensor 4, the predicted wave field  
818 differs in magnitude and phase compared to the measurements (Fig. C.2b), whereas the predicted wave field  
819 agrees well at sensor 6 which is located inside the harbour (Fig. C.2c). On average, the discrepancies in the  
820 predicted wave field are larger compared to the results of OWr. This is likely due to the increased complexity  
821 of the conditions in subset HB due to the partial reflections at the gravel slopes and the occurrence of a  
822 standing wave field inside the harbour. Differences between the physical and numerical domain (e.g., due  
823 to the discretisation of the harbour) and small errors in the numerical phase velocity may not only result in  
824 phase differences, but also in amplitude differences between the predicted and observed wave field (possibly  
825 explaining the differences observed at sensor 4).

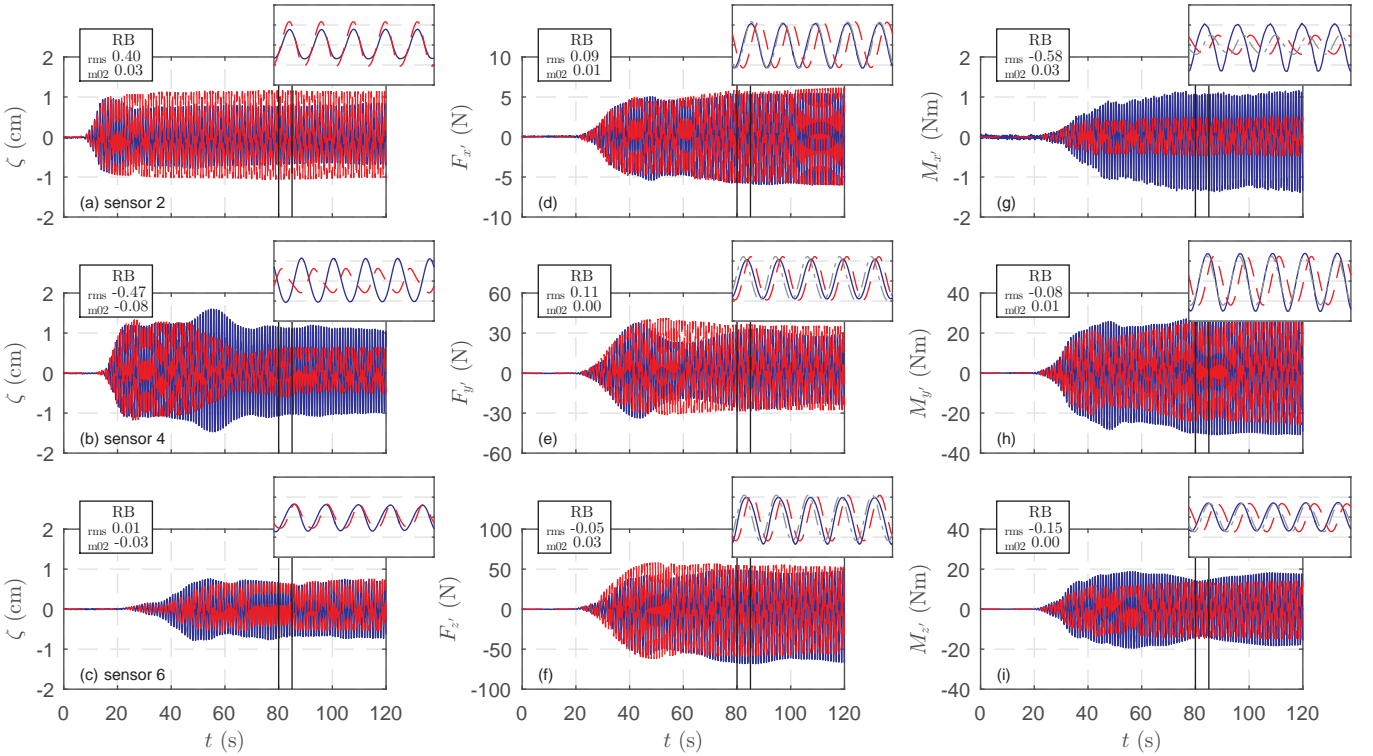


Figure C.2: Predicted (dashed red line) and observed (blue line) time series of the surface elevation  $\zeta$  (a-c), and the forces  $F$  (d-f) and moments  $M$  acting on the ship (g-i) for HBr. The insets adjacent to the main panels show a close up of the results for  $80 \leq t \leq 85$  s (illustrated by the two vertical black lines in the main panels). To facilitate a comparison between the predicted and observed hydrodynamic load signals, the dash-dot gray line in the insets of (d-i) shows the predicted hydrodynamic load signal including a time shift of  $-0.23$  s. In each panel, the relative bias (RB) of the two bulk parameters are depicted in the top left corner. For brevity, the bulk wave heights and loads are denoted with  $\text{rms}$ , and the mean wave and load periods are denoted with  $\text{m02}$ . Note that in this case the scatter index is equal to the absolute value of RB.

826 The wave field near the harbour entrance (sensor 4) and inside the harbour basin (sensor 6), and the  
827 wave-induced loads acting on the moored ship became approximately stationary after  $t > 60$  s (Fig. C.2b-i).

828 Despite the errors in the predicted wave field inside the harbour, the model reproduced the forces and  
829 moments that act on the ship (Fig. C.2d-i); except for  $M'_x$ , and a phase difference between the measured and  
830 predicted load signals. Similar to OWr, a constant time shift approximately corrects for the phase difference  
831 of all individual load components but  $M_{x'}$ . The errors in  $M_{x'}$  suggest that relatively small discrepancies in  
832 the force components (in this case,  $|RB| \leq 0.11$  for  $F'_y$  and  $F'_z$ ) can cause significant discrepancies in the  
833 moment ( $|RB| \leq 0.58$  for  $M'_x$ ).

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