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A novel metric for detecting quadrotor loss-of-control*

Jasper J. van Beers¹, Prashant Solanki², and Coen C. de Visser³

Abstract—Unmanned aerial vehicles (UAVs) are becoming an integral part of both industry and society. In particular, the quadrotor is now invaluable across a plethora of fields and recent developments, such as the inclusion of aerial manipulators, only extends their versatility. As UAVs become more widespread, preventing loss-of-control (LOC) is an ever growing concern. Unfortunately, LOC is not clearly defined for quadrotors, or indeed, many other autonomous systems. Moreover, any existing definitions are often incomplete and restrictive. A novel metric, based on actuator capabilities, is introduced to detect LOC in quadrotors. The potential of this metric for LOC detection is demonstrated through both simulated and real quadrotor flight data. It is able to detect LOC induced by actuator faults without explicit knowledge of the occurrence and nature of the failure. The proposed metric is also sensitive enough to detect LOC in more nuanced cases, where the quadrotor remains undamaged but nevertheless losses control through an aggressive yawing manoeuvre. As the metric depends only on system and actuator models, it is sufficiently general to be applied to other systems.

I. INTRODUCTION

A. Motivation

As the world becomes more automated, and various robots become more integrated with daily life, the ability of these systems to recognize and prevent accidents is essential to their widespread and accepted use. In fact, Carlson et al. [1] found that the main cause of failure in many robotic applications is the control system (henceforth referred to as loss-of-control, LOC), followed by mechanical failures (e.g. actuators). Moreover, studies which find that the increase in automation and application of robotics often lead to more accidents, such as for aircraft autopilots [2] and manufacturing robots [3], only underscore this need for better safety.

In recent years, unmanned aerial vehicles (UAVs) have enjoyed a surge of popularity and use in the field of robotics and beyond. UAVs have become indispensable in a plethora of applications, such as: agriculture [4], (potentially hazardous) maintenance & inspection [5], medical operations [6], and videography. Recent literature on UAVs extends their versatility by equipping them with manipulators [7]. These manipulators may facilitate repairs of infrastructure, such as

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off-shore wind turbines [5], or improve operational efficiency by enabling perching [8].

Given this explosion of research, and the perpetual concern of safety, it comes as no surprise that an extensive body of research focuses on improving UAV safety (e.g. [9], [10], [11], [12]). In particular, many of the advancements are centered around the under actuated - and thus vulnerable quadrotor, which is perhaps the most popular variant of the UAV. However, many of these works (e.g. [10], [13], [14], [15], [16]) are concerned with fault-tolerant control (FTC), and thus do not directly address cases where the undamaged quadrotor experiences loss-of-control (LOC). Furthermore, LOC itself is not clearly defined for the quadrotor; the few LOC definitions that exist are based on simple attitude constraints and are thus too restrictive [11], [12]. Therefore, to encourage the advancement of LOC-aware quadrotors (and by extension other autonomous systems), there is a need to properly detect and label moments of LOC.

B. Related Work

With regards to FTC, many derive unique controller architectures to accommodate hovering and high-speed flight of the quadrotor, despite single and double rotor loss by forfeiting yaw control [10], [17], [18]. Other FTC schemes include those based on sliding mode control [13], [19], machine learning [14], and model predictive control [16].

In aircraft literature, LOC is well-studied and is often defined as an excursion from the safe flight envelope (SFE) bounds [20], [21], [22], [23]. Due to the curse of dimensionality, obtaining estimates of the SFE is difficult and computationally intractable through standard Hamilton-Jacobi reachability analyses [24]. Therefore, Sun et al. [9] employ Monte Carlo simulations to approximate a 6-state SFE of a quadrotor through optimal (bang-bang) control. However, this approach does not accommodate the use of other controllers. Instead, other efficient SFE estimation techniques, such as [24], may be used. However, any estimated SFEs emerge from a given (nominal) model of the system and thus do not directly account for changing dynamics and/or faults. Deriving a family of, already computationally intensive, SFEs can be impractical.

Others instead define quadrotor LOC based on attitude constraints. For example, Schieni et al. [11] hedge the allowable attitude of the quadrotor to limit its aggressiveness, thereby avoiding dangerous manoeuvres. Altena et al. [12] train a recurrent neural network to predict quadrotor LOC using flight data of an undamaged quadrotor where LOC is defined as the moment when the roll or pitch angle exceed

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90 deg. This is tailored to the LOC scenario of the data set. These definitions are prohibitive and scenario specific.

C. Contributions

The main contribution of this paper is a novel indicator, termed the *feasibly controllable metric* (FCM), that defines LOC for quadrotors. By applying the proposed LOC detector to both simulated and real flight data, we demonstrate that the FCM is not only sensitive to LOC detection under actuator faults, but is also capable of detecting LOC when no faults are present (i.e. in the undamaged case).

Moreover, since the FCM derives from system and actuator models, it is sufficiently general to be compatible with other robotic or autonomous platforms where such state measurements and suitable actuator models are available.

D. Organization

The remainder of this paper is organized as follows: section II briefly describes the quadrotor equations of motion and aerodynamic models used in this study. The FCM metric itself is derived in section III and applied to simulation and flight data in section IV.

II. QUADROTOR MODEL

The equations of motion for the quadrotor, expressed in the body reference frame, may be described by

$$m\left(\dot{\mathbf{V}}_{B} + \Omega_{B} \times \mathbf{V}_{B}\right) = R_{BE}m\mathbf{g} + \mathbf{F}_{B} \tag{1}$$

$$\mathbf{I}_{\mathbf{v}}\dot{\Omega}_B + \Omega_B \times \mathbf{I}_{\mathbf{v}}\Omega_B = \mathbf{M}_B \tag{2}$$

where, the mass and moment of inertia of the quadrotor are denoted by m and I_v respectively. The gravity vector, defined in the inertial (North-East-Down, NED) reference frame is given by \mathbf{g} and the rotation matrix transforming a vector from the inertial frame to the body frame is represented by R_{EB} . The body translational and rotational velocities are described by $\mathbf{V}_B = [u, v, w]^T$ and $\Omega_B = [p, q, r]^T$ respectively. $\mathbf{F}_B = [F_x, F_y, F_z]^T$ and $\mathbf{M}_B = [M_x, M_y, M_z]^T$ represent the (aerodynamic) forces and moments acting on the quadrotor body.

The non-linear \mathbf{F}_B and \mathbf{M}_B can be identified from flight data through step-wise regression [25]. Indeed, step-wise regression has previously, and successfully, been applied and numerically validated for quadrotors (interested readers are directed to [26], [27], [28] for more details on the identification procedure and model structure selection). We here employ the models of [28], for which the underlying high-speed flight data is collected (at 500Hz) via free flights in a wind tunnel with wind speeds ranging from 0-14 m/s.

While the LOC detection method proposed in section III should be generalizable to other controlled systems where state and actuator models/measurements are available, we here apply the metric to the (inner-loop) rate control of a quadrotor. Rearranging eq. (2) and replacing M_B with the appropriate identified polynomial aerodynamic models of [28] yields eq. (3).

$$\dot{\Omega}_{B} = \mathbf{I_{v}}^{-1} \begin{bmatrix} M_{x}(p, u_{p}) \\ M_{y}(q, u_{q}) \\ M_{z}(r, u_{r}) \end{bmatrix} - \mathbf{I_{v}}^{-1} \Omega_{B} \times \mathbf{I_{v}} \Omega_{B}$$
(3)

In eq. (3), u_p , u_q , and u_r represent the difference in rotor speeds that enact rolling, pitching, and yawing moments respectively. This is used as the input vector in this paper since it results in a diagonal control effectiveness matrix, B, in section III. The control moments depend on the quadrotor configuration and, for the quadrotors used in this paper¹, may be constructed from the rotor speeds via

$$u_{p} = (\omega_{1} + \omega_{4}) - (\omega_{2} + \omega_{3})$$

$$u_{q} = (\omega_{1} + \omega_{2}) - (\omega_{3} + \omega_{4})$$

$$u_{r} = S_{r}[(\omega_{1} + \omega_{3}) - (\omega_{2} + \omega_{4})]$$
(4)

 $S_r = 1$ for clockwise rotation of ω_1 and $S_r = -1$ if counterclockwise. The aerodynamic moment models themselves are (up to) forth order polynomial functions of the associated body rotational rates Ω_B and control moments [27], [28].

III. DERIVATION OF FEASIBLY CONTROLLABLE METRIC

Consider a general non-linear system described by

$$\dot{\mathbf{x}} = f(\mathbf{x}, \mathbf{u}) \tag{5}$$

where $\mathbf{x} \in \mathbb{X} \subset \mathbb{R}^n$ denotes the system states and $\mathbf{u} \in \mathbb{U} \subset \mathbb{R}^m$ describes the inputs of the system.

The difference of eq. (5) between two consecutive samples, k and k+1, may be approximated (assuming, $f(\mathbf{x}, \mathbf{u})$ is smooth and differentiable) through

$$\dot{\mathbf{x}}_{k+1} - \dot{\mathbf{x}}_k = \frac{\delta f}{\delta \mathbf{x}} \cdot (\mathbf{x}_{k+1} - \mathbf{x}_k) + \frac{\delta f}{\delta \mathbf{u}} \cdot (\mathbf{u}_{k+1} - \mathbf{u}_k)
\rightarrow d\dot{\mathbf{x}} = \frac{\delta f}{\delta \mathbf{x}} d\mathbf{x} + \frac{\delta f}{\delta \mathbf{u}} d\mathbf{u}$$
(6)

Taking the time derivative of this difference yields

$$\frac{1}{dt} \cdot (d\dot{\mathbf{x}}) = \frac{1}{dt} \cdot \left(\frac{\delta f}{\delta \mathbf{x}} d\mathbf{x} + \frac{\delta f}{\delta \mathbf{u}} d\mathbf{u} \right)
\rightarrow \ddot{\mathbf{x}} = \frac{\delta f}{\delta \mathbf{x}} \dot{\mathbf{x}} + \frac{\delta f}{\delta \mathbf{u}} \dot{\mathbf{u}} \tag{7}$$

Equation (6) is only truly valid if $d\mathbf{x}$ and $d\mathbf{u}$ are small. For dynamic systems such as the quadrotor, this holds if the time increment, dt, is sufficiently small². Hence, taking the time derivative is an elegant way to linearize the system - with respect to its derivative - to arrive at the so-called differential form (or, alternatively, the velocity form [29]):

$$\ddot{\mathbf{x}} = A\dot{\mathbf{x}} + B\dot{\mathbf{u}} \tag{8}$$

Equation (8) gives an exact representation of the non-linear system at the point (\mathbf{x}, \mathbf{u}) . In other words, it may be considered a linear parameter varying (LPV) model, scheduled by the states and inputs. For the fortunate cases where $f(\mathbf{x}, \mathbf{u})$ is known (and differentiable), relations for A and B may be exactly derived. Even if $f(\mathbf{x}, \mathbf{u})$ is known, linearization is nonetheless useful as it facilitates the application of powerful and well-studied linear analysis tools. While not strictly

 $^{^{1}\}omega_{1}$ is located front left, ω_{2} front right, ω_{3} aft right and ω_{4} aft left.

²Many open-source flight controllers, such as BetaFlight, support sampling rates of up to 8kHz.

necessary for the method described here, the differential form offers a simple way to derive a valid linear formulation, in particular for the control effectiveness B, of the system.

Often, the standard definition for controllability (i.e. eq. (9)) is too lenient as it does not consider the limits of the actuator. Indeed, for a system to be *feasibly controllable*, the actuators should be capable of enacting the change necessary to maintain control. This may not always be the case, especially in the presence of partial actuator faults or saturation. However, purely looking at actuator saturation for LOC detection is too restrictive as it may be necessary to (at least temporarily) saturate the actuators to satisfy reference tracking. Consider, for example, a "punch out" manoeuvre for the quadrotor or other such aggressive maneuvering which often saturates the rotors, but are often not considered LOC events³. The well-known controllability matrix is:

$$C = [B \quad AB \quad A^2B \quad \cdots \quad A^{n-1}B] \tag{9}$$

In general, $f(\mathbf{x}, \mathbf{u})$ is mostly unknown and thus A and B need to be estimated. These may be estimated directly through eq. (8), or derived using the velocity form applied to a full non-linear model that approximates $f(\mathbf{x}, \mathbf{u})$ identified through other techniques, such as neural networks or stepwise regression [25], [27].

Note that, for fast systems such as the quadrotor, the time increment between samples is often small and thus $d\mathbf{x} \approx 0$. While not strictly necessary for the metric, we will make the approximation that $d\dot{\mathbf{x}} \approx B \cdot d\mathbf{u}$ when dealing with real flight data in section IV to address cases where reliable estimates of A may be unavailable. The $d\dot{\mathbf{x}} \approx B \cdot d\mathbf{u}$ approximation can be made for systems with similar (actuator) characteristics, but should not be made when $A \cdot d\mathbf{x}$ is not negligible across consecuetive time steps.

However, unless B (and equivalently, A if available) is estimated online, the identified models typically refer to the nominal system and thus may not account for time-varying dynamics or actuator faults. Indeed, the ability of a system to maintain control depends on its current dynamics and actuator capabilities. We therefore suggest that A and B be locally updated in some capacity. The cross-correlation⁴, $M \in (0,1]$, between $d\dot{\mathbf{x}}$ and $A \cdot d\mathbf{x} + B \cdot d\mathbf{u}$ may be used as an indicator of the discrepancy between the nominal and current systems: any changes in the state derivative should be explainable by a corresponding change in the (one-step behind) inputs. The nominal control effectiveness may then be modified through a product with M (i.e. $B_{k+1} = B_k M$) where M is estimated over a moving window. Other methods for obtaining M, such as Recursive Least Squares, may also be used for better estimates.

The core principle behind the proposed metric is that, under perfect conditions, changes in the state derivative are fully explainable by the model. Thus,

$$d\dot{\mathbf{x}} - A \cdot d\mathbf{x} - B \cdot (\mathbf{u}_{k+1} - \mathbf{u}_k) = 0 \tag{10}$$

However, errors - be these from model misspecification, a change in dynamics, or faults - will likely be observed. These should be accommodated by an additional control effort as shown in eq. (11). Note that **e** here refers to the error between measurements of the state derivative and predictions from the (difference) model (eq. (6)), and not the tracking error.

$$d\dot{\mathbf{x}} - A \cdot d\mathbf{x} - B \cdot (\mathbf{u}_{k+1} - \mathbf{u}_k + \Delta \mathbf{u}_c) = \mathbf{e}$$
 (11)

Substituting eq. (10) into eq. (11) and solving for the necessary corrective control action yields

$$\Delta \mathbf{u_c} = B^{-1} \mathbf{e} \tag{12}$$

The key, then, is to determine if such a corrective command is possible, and if not, we consider the system to be in a state of instantaneous LOC. Indeed, the allowable periods of LOC may differ between systems and operating conditions. Therefore, a majority voting window - tied to a specified tolerable duration of sustained LOC - may be employed to identify periods of LOC. These may be related to the time-to-recovery, or backward reachable set, of the system.

An actuator model may be used to probe the feasibility of a particular command. We here rely on a first order actuator model of the quadrotor, however, other (potentially nonlinear) actuator models are compatible with the proposed approach so long as the maximum actuator effort can be found at each time step. The maximum possible change in the control moments prescribed by the first order motor model is given by

$$\Delta \mathbf{u}_{\mathbf{MAX}} = dt \cdot \sum_{i=1}^{4} \frac{1}{\tau} \left(\omega_{MAX} - \omega_i \right)$$
 (13)

where dt denotes the time step, τ the actuator time constant (which can be estimated from flight data), and ω_{MAX} is the lower/upper saturation limits of the rotor. Whether the lower or upper limit should be used depends on the direction of necessary change in rotor speed in order to correct for \mathbf{e} .

The quadrotor is considered to be in a state of LOC if $\Delta \mathbf{u}_{MAX} < \Delta \mathbf{u}_{c}$, even when eq. (9) maintains full row rank. We define the *Feasibly Controllable Metric* (FCM), at an instant, k, to be

$$FCM[k] = \begin{cases} 0 & \text{if } \Delta \mathbf{u_{MAX}}[k] < \Delta \mathbf{u_{c}}[k] \text{ or } rank(\mathbf{C}[k]) < n \\ 1 & \text{otherwise} \end{cases}$$
(14)

This may be extended to a majority voting window by taking the average of FCM[k] across MVW samples to yield the windowed FCM:

$$FCMW = \begin{cases} 0 & \text{if } \frac{1}{MVW} \sum_{i=k-MVW}^{k} FCM[i] < 0.5\\ 1 & \text{otherwise} \end{cases}$$
 (15)

Note that, for many systems such as the quadrotor, direct measurements of \dot{x} (and \ddot{x}) are usually unavailable. These therefore need to be estimated (from the state), which often introduces a lag between knowledge of the current state

³Occasionally, however, these aggressive manoeuvres can lead to LOC, suggesting that saturation may play a crucial role in LOC detection.

⁴For the quadrotor, M < 0 should not occur as the control effectiveness associated with the control moments cannot switch. Moreover, M = 0 is avoided as this leads to a singular B.

and corresponding derivative. Thus, the state, its derivative, and input vectors should be properly synchronized when computing the FCM through eq. (8), eq. (11) and eq. (13). Subsequently, the FCM information is also delayed with respect to the current index by a few samples, which can easily be compensated for in (a-posteriori) analyses by shifting the time-series. In online applications, this delay in FCM delivery is negligible if LOC manifests on a relatively longer time-scale compared to the sampling rate (i.e. time-to-LOC \gg time step).

IV. RESULTS: SIMULATION AND FLIGHT DATA

We first apply the FCMW metric on a simulated quadrotor to demonstrate its use for cases with full model knowledge and actuator faults. Such faults are considered true LOC scenarios. As a more practical demonstration, the FCMW is also applied to real quadrotor flight data where LOC is suspected, but not guaranteed, to occur. For this case, a full model of the quadrotor is assumed to be unavailable, and thus the FCMW is derived only from estimates of B made on the flight data. Note, however, that the implicit assumption made here is that the quadrotor remains (theoretically) controllable by $rank(\mathbf{C}) = n$. This assumption is reasonable since no (partial) actuator faults occur in the flight data.

A. Simulation Overview

The identified high-speed aerodynamic models of [28] are deployed in a Python-based non-linear quadrotor simulation environment running at 250 Hz. Control of the quadrotor is facilitated through cascaded PID loops which map desired position and yaw commands to desired accelerations and rates. The inner-most rate and acceleration loop utilize the incremental non-linear dynamic inversion (INDI) controller developed by [30]. Briefly, the goal of the controller is to align the thrust-vector of the quadrotor with the desired acceleration vector in the NED frame. The simulated quadrotor's properties are summarized in table I.

Furthermore, zero-mean white noise is injected into the simulated measurements of the quadrotor's velocity, $\mathcal{N}(0, \sigma_V = 0.01)$ m/s, and rotational rates, $\mathcal{N}(0, \sigma_\Omega = 8.73 \cdot 10^{-5})$ rad/s. These values are derived from the inertial measurement unit (MPU6000) of the quadrotor used to generate the underlying aerodynamic models for the simulator.

B. Loss-of-control Detection in Simulation

Using the simulator, two experiments are conducted wherein the quadrotor is assigned a simple position tracking

TABLE I
PHYSICAL PROPERTIES OF THE SIMULATED QUADROTOR

Mass (incl. batteries), g				433
Diagonal hub-to-hub				217
diameter, mm				
Propeller diameter, mm				76.5
_	[0.865	0	0
Moment of inertia, $kg \cdot m^2$	10^{-3} ·	0	1.07	0
		0	0	1.71
Actuator time constant, Hz		-		60

task. In the first experiment, the quadrotor is in its nominal configuration and experiences no actuator faults. In this scenario, the proposed metrics are not expected to detect LOC. Conversely, in the second experiment, one of the rotors is capped at 0% thrust at t = 5.2s, representing the complete loss of a single rotor. Here, the proposed metrics are expected to be able to detect LOC. In this experiment, the metrics are not explicitly made aware of the fault (i.e. eq. (13) assumes that all rotors are still fully operational).

In both experiments, the current control effectiveness matrix is updated through $B_{k+1} = B_k M$ as described in section III. Here, a moving window of 0.2s is used to determine the values of M where, nominally, M = I. Recall that B (and thus M) are diagonal as the quadrotor control scheme employed here relies on the (orthogonal) control moments as the input vector. Furthermore, the majority voting window duration for the FCMW is also set to 0.2s to mirror M.

Figure 1 depicts the position tracking trajectory of the quadrotor in its nominal configuration (i.e. no actuator faults). As expected, rank(C) = 3 and both the FCM[k] = 1 and FCMW = 1 suggesting that the quadrotor remains in control for the duration of the flight.

Conversely, when an actuator fault occurs during flight, the FCM[k] and FCMW are able to detect LOC shortly after the

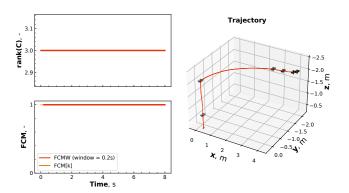


Fig. 1. Position tracking trajectory of the nominal quadrotor. Also shown are the standard controllability metric, rank(C) = n, and those proposed in this paper, FCM[k] and FCMW.

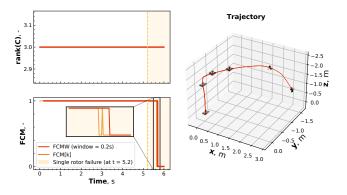


Fig. 2. Position tracking trajectory of the quadrotor with the complete failure of a single rotor at t = 5.2s. Also shown are the standard controllability metric, rank(C) = n, and those proposed in this paper, FCM[k] and FCMW.

onset of the fault as shown in fig. 2. Crucially, this LOC event is not observable through the controllability check alone (i.e. rank(C) = 3 persists), even with the updated $B_{k+1} = B_k M$. This is because the elements of C only approach zero, but do not reach it. This demonstrates the potential of the FCM[k] and/or FCMW for LOC detection. Furthermore, in fig. 2, the merits of using a voting window are highlighted by the more stable response of FCMW compared to FCM[k]. However, this comes at the cost of a delayed LOC detection. Future work should seek to combine various window durations of FCMW to refine estimates of LOC.

C. Quadrotor Loss-of-control Flight Data Overview

For a more practical demonstration, we here apply the FCMW to real LOC flight data. As a means of comparison, the LOC flight data collected in the LOC prediction study of Altena et al. [12] is used here. Flights are flown using a custom built quadrotor from commercial parts, the properties of which are summarized in table II. The flight data is collected in the CyberZoo - an open area of 7x7x10m in height, width, and length respectively - at the Delft University of Technology. LOC is induced by demanding an excessively high yaw rate (± 2000 deg/s) from the quadrotor. Some time after the start of this manoeuvre, the quadrotor begins to oscillate about its roll and pitch axes with increasing magnitude until it makes a sudden, aggressive, turn culminating in a crash. More details on the quadrotors used, the LOC manoeuvre, and the flight data itself can be found in [12]. Note that this LOC scenario is more nuanced than the clear-cut actuator fault case investigated in section IV-B.

Moreover, in [12], LOC is defined as the moment in time where the roll or pitch angle exceeds, and continues to exceed, 90 deg after the start of the yawing manoeuvre. As stated by the authors, this definition is rather rudimentary and is tailored to the yaw LOC scenario. Indeed, the true moment of LOC may occur before, or after, the labelled moment. Therefore, the yaw manoeuvre flights which did not meet the LOC definition criteria of [12] are also included in this study. Moreover, system identification flights for the CineGo quadrotor are also included in the data set as a ground truth for which LOC is not considered to occur. These include flights where a similar aggressive yaw manoeuvre is conducted, but stopped before any off-axis oscillations start. This culminates in a total of 121 flights: 12 are non-LOC flights and the remaining 109 harbor the dangerous potentially LOC inducing - yaw manoeuvre, of which only 34 meet the attitude criteria of [12].

TABLE II PROPERTIES OF THE GEPRO CINEGO QUADROTOR

Mass (incl. batteries), g	265
Diagonal hub-to-hub	361
diameter, mm	
Propeller diameter, mm	76.5
Motor, -	Emax Eco 1407 3300kv
Batteries, -	1x Tattu R-Line 14.8V 550mAh 4S
Flight Controller (FC), -	MATEKSYS F722-mini 2-8S
FC Software, -	Betaflight 4.2

D. Loss-of-control Detection on Real Flight Data

From preliminary results, it was observed that applying a low-pass filter to the raw flight data (i.e. quadrotor rates and rotor speed measurements) improves the ability of the *FCMW* to distinguish between the non-LOC and LOC flights. This is likely due to the noise present in the data, which results in false positives when the actuators are near, or at, saturation during an aggressive manoeuvre. Therefore, the *FCMW* appears to be sensitive to noise in the data and adequate measures should be taken to minimize this effect.

Indeed, it is unclear what combination of majority voting window, MVW, and low-pass cut-off frequency, CF, yield the best LOC detection performance and how sensitive the FCMW is to these hyper-parameters. Therefore, the FCMW is computed across the whole flight data set for various combinations of voting window duration $MVW \in [0.02, 0.05, 0.1, 0.2, 0.4, 0.6, 1, 1.2, 1.5]$ s and cut-off frequency $CF \in [1, 5, 10, 30, 50, 100]$ Hz. The duration of the LOC inducing yaw manoeuvre lasts, on average, 2.4s before a crash, with the fastest crash occurring after 1.3s. Subsequently, the MVW is capped at 1.5s to afford the FCMW enough time to detect potential features which may occur within the period of the manoeuvre, but also to verify that windows longer than the LOC manoeuvre likely fail at detection altogether. Similar motivations for the cut-off frequency follow from power spectral densities of the raw flight data where the majority of the aerodynamics are observed to occur at frequencies below 50 Hz.

The ground truth non-LOC flights are used to determine which hyper-parameter combinations promote the greatest *FCMW* sensitivity to LOC while limiting false positives of non-LOC. Figure 3 summarizes the performance of the *FCMW* across all the *MVW* and *CF* combinations. In general, the shorter the *MVW*, the more prone the *FCMW*

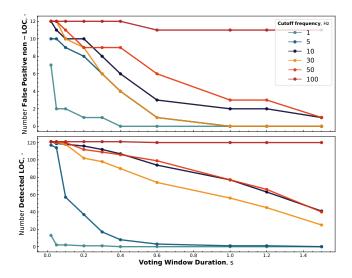


Fig. 3. Performance of the Windowed Feasibly Controllable Metric (FCMW), applied to the CineGo loss-of-control flight data set [12], for various combinations of majority voting window, MVW, duration (in seconds) and low-pass filter cut-off frequency, CF (in Hertz).

metric is to falsely label a non-LOC flight as a LOC flight. Longer MVWs reduce the sensitivity of the FCMW (see top subplot of fig. 3). Conversely, the lower the CF, the more capable the FCMW is at correctly identifying a non-LOC flight. However, if the CF is too low, then the FCMW becomes insensitive to LOC detection as the majority of the aerodynamics are filtered out (refer to bottom subplot of fig. 3). The optimum combination is found to be MVW = 1.0s and CF = 30Hz as this combination correctly identifies all non-LOC flights while being the most sensitive to LOC detection. As expected, this MVW is below the fastest observed crash of 1.3s.

Figure 4 illustrates the LOC detection capacity of the FCMW detector, using the optimal hyper-parameters, for all yaw-LOC inducing flights of the CineGo. Also shown are the detection distributions of the FCMW and attitude-based (Att) definition of [12], along with an example of these detectors applied to an arbitrary LOC flight plotted in black. It is clear that the FCMW tends to detect LOC much earlier than the attitude definition, suggesting that LOC potentially occurs much earlier than initially expected in [12]. Additionally, the FCMW distribution suggests that this indicator is more consistent than its attitude-based counterpart. Interestingly, the FCMW appears to detect LOC shortly after the unstable off-axis oscillations - which ultimately lead to the crash begin. It is hypothesized that the FCMW may be detecting the onset of a bifurcation, where the quadrotor transitions from a non-oscillatory equilibrium to an (unstable) oscillatory one. Indeed, the oscillatory response of the quadrotor may be reflective of the controller struggling to maintain control, or an increase in phase lag between the inputs and system response. These hypotheses should be verified in future experiments.

Another possibility is that the FCMW simply flags LOC once the yaw manoeuvre lasts for the duration of the chosen voting window since the rotor speed commands saturate during the manoeuvre (i.e. the moment of LOC detection may be equivalent to the duration of MVW). This would imply that the FCMW is not sensitive to LOC. To verify if this is the case, the time between the start of the vaw manoeuvre and LOC detection is evaluated for all MVW durations at the optimal cut-off frequency of CF = 30 Hz(illustrated in fig. 5). The majority of the LOC detections occur above the trivial case (i.e. time-to-LOC detection \neq MVW), indicating that the FCMW LOC detection is not only based on the duration of the MVW. While a larger MVW does increase the time-to-LOC detection, this can be explained by the fact that more FCM[k] need to be in the LOC state for the longer windows to trigger. In other words, the longer the MVW, the more severe the LOC event is. Moreover, recall that the non-LOC flights include the same aggressive yaw manoeuvres that induce LOC, only stopped before significant oscillations appear; none are detected as LOC by the FCMW with the optimal hyper-parameters. This further suggests that the FCMW is not simply flagging the yaw-manoeuvre itself, but rather other features indicative of LOC. As the FCMW detects LOC earlier than the attitude

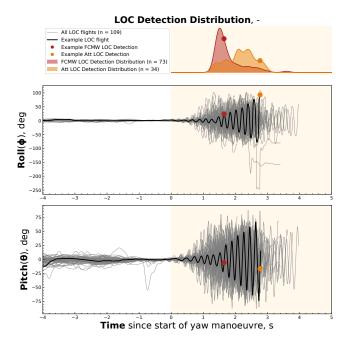


Fig. 4. Comparison of the quadrotor loss-of-control (LOC) detection capabilities of the Windowed Feasibly Controllable Metric (FCMW) versus the attitude-based definition (Att) of [12] for yaw-induced LOC flights of the CineGo quadrotor. Shown are the detection distributions of each definition Plotted in black is an example LOC detection of both definitions for one of the LOC flights. The hyper-parameters for the FCMW are: voting window MVW = 1.0s and cut-off frequency CF = 30Hz.

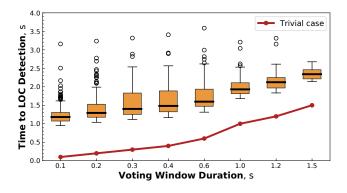


Fig. 5. Variation in the time to loss-of-control detection of the Windowed Feasibly Controllable Metric (FCMW) as a function of the majority voting window (MVW) duration, in seconds. Also shown, in red, is the trivial case where the time-to-LOC detection = MVW. The two lowest MVW (i.e. 0.02s and 0.05s) are not shown due to large variances and outliers.

definition of [12], it is perhaps unsurprising that it also labels more of the flights as LOC. Compare the 73 LOC detections of the *FCMW* to the 34 of the attitude-based definition.

These experimental results show that - with appropriate hyper-parameters - the *FCMW* is capable of more nuanced LOC detection for real, undamaged, quadrotor data. Moreover, the *FCMW* does not flag nominal flights as LOC, even when similar manouevres are present. Taken in tandem with the simulation experiment results, the proposed metric (*FCMW*) appears to be a promising, and potentially general, indicator of (un)damaged quadrotor LOC.

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