

## An experimental and numerical investigation of coarse aggregate settlement in fresh concrete under vibration

Cai, Yuxin; Liu, Qing feng; Yu, Linwen; Meng, Zhaozheng ; Hu, Zhe; Yuan, Qiang ; Šavija, Branko

**DOI**

[10.1016/j.cemconcomp.2021.104153](https://doi.org/10.1016/j.cemconcomp.2021.104153)

**Publication date**

2021

**Document Version**

Accepted author manuscript

**Published in**

Cement and Concrete Composites

**Citation (APA)**

Cai, Y., Liu, Q. F., Yu, L., Meng, Z., Hu, Z., Yuan, Q., & Šavija, B. (2021). An experimental and numerical investigation of coarse aggregate settlement in fresh concrete under vibration. *Cement and Concrete Composites*, 122, Article 104153. <https://doi.org/10.1016/j.cemconcomp.2021.104153>

**Important note**

To cite this publication, please use the final published version (if applicable).  
Please check the document version above.

**Copyright**

Other than for strictly personal use, it is not permitted to download, forward or distribute the text or part of it, without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license such as Creative Commons.

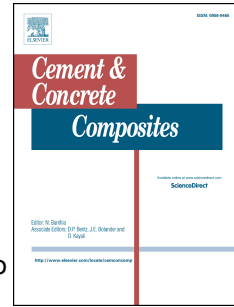
**Takedown policy**

Please contact us and provide details if you believe this document breaches copyrights.  
We will remove access to the work immediately and investigate your claim.

# Journal Pre-proof

An experimental and numerical investigation of coarse aggregate settlement in fresh concrete under vibration

Yuxin Cai, Qing-feng Liu, Linwen Yu, Zhaozheng Meng, Zhe Hu, Qiang Yuan, Branko Šavija



PII: S0958-9465(21)00221-3

DOI: <https://doi.org/10.1016/j.cemconcomp.2021.104153>

Reference: CECO 104153

To appear in: *Cement and Concrete Composites*

Received Date: 21 April 2021

Revised Date: 10 June 2021

Accepted Date: 21 June 2021

Please cite this article as: Y. Cai, Q.-f. Liu, L. Yu, Z. Meng, Z. Hu, Q. Yuan, B. Šavija, An experimental and numerical investigation of coarse aggregate settlement in fresh concrete under vibration, *Cement and Concrete Composites* (2021), doi: <https://doi.org/10.1016/j.cemconcomp.2021.104153>.

This is a PDF file of an article that has undergone enhancements after acceptance, such as the addition of a cover page and metadata, and formatting for readability, but it is not yet the definitive version of record. This version will undergo additional copyediting, typesetting and review before it is published in its final form, but we are providing this version to give early visibility of the article. Please note that, during the production process, errors may be discovered which could affect the content, and all legal disclaimers that apply to the journal pertain.

© 2021 Published by Elsevier Ltd.

# An experimental and numerical investigation of coarse aggregate settlement in fresh concrete under vibration

Yuxin Cai <sup>a,b</sup>, Qing-feng Liu <sup>a,b,\*</sup>, Linwen Yu <sup>c</sup>, Zhaozheng Meng <sup>a,b</sup>, Zhe Hu <sup>a,b</sup>,  
Qiang Yuan <sup>d</sup>, Branko Šavija <sup>e</sup>

<sup>a</sup> State Key Laboratory of Ocean Engineering, School of Naval Architecture, Ocean and Civil Engineering, Shanghai Jiao Tong University, Shanghai 200240, China

<sup>b</sup> Shanghai Key Laboratory for Digital Maintenance of Buildings and Infrastructure, Shanghai 200240, China

<sup>c</sup> College of Materials Science and Engineering, Chongqing University, Chongqing 400045, China

<sup>d</sup> School of Civil Engineering, Central South University, Changsha 410075, China

<sup>e</sup> Microlab, Faculty of Civil Engineering and Geosciences, Delft University of Technology, Delft 2628CN, the Netherlands

\* Corresponding author.

*E-mail address:* liuqf@sjtu.edu.cn (Q.-F. Liu).

## Abstract

Fresh concrete needs vibration to compact, fill the mould and reach a dense state. During the compaction process, coarse aggregates (CAs) tend to settle, affecting the homogeneity and eventually the long-term durability of hardened concrete. In this study, a 3-D, multi-phase numerical model for fresh concrete is developed for better understanding the CA settlement under vibration. The settlement rate of the CA in vibrated concrete is considered based on the Stokes law, and the calibrated rheological parameter of mixtures is determined by the segmented sieving method. The model prediction shows that the vibration time has the greatest effect on CA settlement, followed by the particle size of CAs, whereas the density of CAs and the plastic viscosity of mixtures contribute a little compared with the aforementioned factors. Through experimental tests, the validity of prediction results is well verified. The proposed model provides a new method to understand and estimate the settlement behaviour of CAs.

**Keywords:** CA settlement; Fresh concrete; Vibration; Rheology; Numerical model; Grey relational analysis

## 1. Introduction

In general, concrete comprises cement as a binder, natural sand and gravel as aggregates, and mixing water together with chemical admixtures. With the hydration reaction of cementitious materials, fresh concrete will gradually develop from a viscoplastic cohesive process to a viscoelastic hardening process [1]. The stability of fresh concrete refers to its ability to maintain the uniform distribution of constituents during transport, casting and compacting [2]. In the process of consolidation, vibration helps to remove entrapped air voids and improve the compactness of concrete, but also causes the relative movement and redistribution of various components of mixtures due to the insufficient cohesion and density difference [3,4]. Notably, high-frequency vibration-induced settlement of coarse aggregates (CAs) greatly increases the heterogeneity of fresh concrete [5–7]. At present, among various types of concretes, only self-compacting concrete with optimum flowability and viscosity does not need to be vibrated during placement [8]. It can be seen that the vibrating process still remains a necessary step in most cases.

The rheological behaviour of vibrated fresh concrete has been reported in some previous studies. Tattersall and Baker [9,10] held the view that fresh concrete no longer behaved as a Bingham model when exposed to vibration, but approximately followed a power-law pseudoplastic model with zero yield value. When the shear rate was rather low, it could be considered as a Newtonian fluid. Hu and de Larrard [11] pointed out that vibration greatly decreased the yield stress, and sometimes even made it practically disappear, which caused the CAs to settle. Nevertheless, the plastic

23 viscosity was reduced a little or seemed unaffected sometimes by external vibration.  
24 Esmailkhanian et al. [12] indicated that vibration would decrease the “internal  
25 friction” of concrete mixtures, which promoted sinking of CAs under the action of  
26 gravity. Pichler et al. [13] highlighted again that the apparent flowing behaviour of  
27 fresh cement-based materials under vibration could be described using a power-law  
28 model with shear-thinning nature.

29 The settlement of CAs has an adverse impact on the surface appearance, design  
30 strength and durability of hardened concrete. This may cause significant problems,  
31 such as the decline in mechanical strength, increased shrinkage and cracking, and the  
32 reduction of chemical erosion resistance, all of which are detrimental to the  
33 performance of reinforced concrete structures [14–21]. However, due to the opacity of  
34 concrete, the direct observation of CA settlement with naked eye is impossible.  
35 Therefore, some special experimental techniques have been proposed to characterize  
36 the settlement phenomenon. Petrou et al. [22] introduced a radioactive element  
37 labelling method that utilized nuclear medicine technology to monitor the deposition  
38 of CAs in vibrated concrete. Koch et al. [23] and Tian et al. [24] used carbomer gel to  
39 prepare a transparent paste, and visually observed the settlement and segregation of  
40 fresh concrete. After concrete hardening, Barbosa et al. [25], Navarrete and Lopez  
41 [26], and Nili et al. [27] cut the specimen and analysed the CA distribution through  
42 image processing. Benaicha et al. [28] proposed a method based on the ultrasonic  
43 velocity to estimate the homogeneity and quality of concrete at early age. Through the  
44 electrical conductivity method, Khayat et al. [29] inserted the electrode pairs at

45 different heights of concrete specimen to assess the uniformity of CA content.  
46 Furthermore, a technique of gamma-ray attenuation was adapted by Vanhove et al. [30]  
47 and Gokce et al. [31] to measure the distribution of CAs in concrete.

48 In summary, the instability caused by vibration is a critical issue in fresh concrete,  
49 and it is necessary to present a convenient and visual methodology to reveal the  
50 problem of CA settlement in vibrated concrete. In recent years, the theoretical models  
51 of rheological properties of cement-based materials have been extensively studied  
52 [32–37]. However, these developments have not been applied on the evaluation of CA  
53 settlement, and most knowledge is still based on experimental observations described  
54 above.

55 Therefore, the main objective of this study is to develop a rational and reliable  
56 numerical model to investigate the settlement of CAs. Experiments are also designed  
57 to verify the validity of the model prediction, based on the segmented sieving method.  
58 Parametric studies of influencing factors such as the vibration time, the properties of  
59 CAs and the plastic viscosity of mixtures on CA settlement are performed and  
60 discussed, and grey relational analysis is put forward to compare the influence level of  
61 these factors. The proposed model for CA settlement can not only save time, workload  
62 and raw materials, but also provide a potential approach to visualize the CA  
63 movement and a complementary tool to adequately understand and estimate the  
64 settlement behaviour of CAs in vibrated concrete.

65

## 66 2. Experimental details

### 67 2.1. Materials and mixtures

68 P.O 42.5R ordinary Portland cement (OPC) conforming to Chinese standard GB  
 69 175-2007 with a density of  $3020 \text{ kg/m}^3$  and a Blaine specific surface area of  $340$   
 70  $\text{m}^2/\text{kg}$  was used to prepare the concrete mixtures. Silica fume (SF), with a density of  
 71  $2200 \text{ kg/m}^3$  and a Blaine specific surface area of  $22205 \text{ m}^2/\text{kg}$ , was used to replace a  
 72 certain amount of OPC. The chemical compositions of OPC and SF determined by  
 73 X-ray fluorescence (XRF) are given in Table 1. River sand was used as the fine  
 74 aggregate, with the apparent density of  $2690 \text{ kg/m}^3$ , and the fineness modulus of 2.9.  
 75 Crushed limestone with a particle size of 5–20 mm was used as the CA, with an  
 76 apparent density of  $2670 \text{ kg/m}^3$  and approximately regular spherical shape. Particle  
 77 size distribution of raw materials is presented in Fig. 1, where OPC and SF were  
 78 measured by laser granulometry, and river sand and limestone CA were measured by  
 79 sieving method. High-performance polycarboxylate superplasticizer was used in the  
 80 mixtures to adjust the workability. Its specific gravity, water reduction rate, solid  
 81 content and pH were equal to 1.09, 40%, 42% and 6.7, respectively.

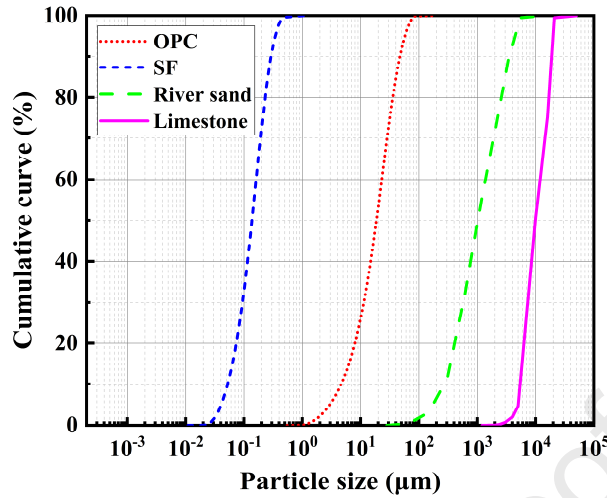
82

83

Table 1 Chemical compositions of OPC and SF (wt%).

Cementitious materials	CaO	SiO <sub>2</sub>	Al <sub>2</sub> O <sub>3</sub>	Fe <sub>2</sub> O <sub>3</sub>	MgO	SO <sub>3</sub>	Alkali content	Loss on ignition
	OPC	58.99	22.02	6.19	2.65	2.53	2.67	0.70
SF	0.76	87.42	0.29	1.75	2.49	0.48	–	3.30

84



85

86

Fig. 1. Particle size distribution of raw materials.

87

88

89

90

91

92

93

94

95

96

97

98

99

Prior works [9–11] showed that vibration could change the rheological behaviour of fresh concrete from a thixotropic fluid with yield stress to a non-thixotropic fluid with a very low or even negligible yield stress value. At this time, the CA settlement mainly depended on the plastic viscosity of mixtures and had no relation to the yield stress [8,22,38,39], and a higher viscosity helped decrease the settlement velocity of CAs [40,41]. Hence, three concrete mixtures with different plastic viscosities were designed by adjusting the dosage of SF. The mix proportions of concrete shown in Table 2 were obtained through multiple experiments. Among them, the first was normal concrete (NC), and the second and third added SF to replace 5% and 10% of OPC by mass, respectively, to obtain mixtures with higher plastic viscosities. The water to binder ratio (w/b) was controlled at 0.40, and the dosage of superplasticizer was 0.5% of cementitious materials by mass.



100

101

Table 2 Mix proportions of concrete (kg/m<sup>3</sup>).

Group	w/b	OPC	SF	River sand	Limestone	Water	Superplasticizer
NC	0.40	400.0	–	736.0	1104.0	160.0	2.0
NC-5%SF	0.40	380.0	20.0	736.0	1104.0	160.0	2.0
NC-10%SF	0.40	360.0	40.0	736.0	1104.0	160.0	2.0

102

## 103 2.2. Properties of fresh concrete

104

The main properties of these three groups of concrete mixtures are listed in Table

105

3. The apparent density, air content, slump, slump flow and bleeding rate were tested

106

according to the Chinese standard GB/T 50080-2016. The rheological parameters of

107

fresh concrete were measured by the ICAR concrete rheometer produced in Denmark.

108

In the flow curve test, the initial speed is 0.50 rps, the final speed is 0.05 rps, the

109

number of testing points is 7, and the duration of each point is 5 s. The yield stress

110

and plastic viscosity of concrete mixtures were calculated from the flow curve based

111

on the Bingham model, as shown in Eq. (1).

112

$$\tau = \tau_0 + \eta_p \dot{\gamma} \quad (1)$$

113

where  $\tau$  is the shear stress,  $\tau_0$  is the yield stress,  $\eta_p$  is the plastic viscosity, and  $\dot{\gamma}$  is

114

the shear rate.

115

116

Table 3 Main properties of fresh concrete.

Group	Apparent density (kg/m <sup>3</sup> )	Air content (%)	Slump (mm)	Slump flow (mm)	Bleeding rate (%)	Yield stress (Pa)	Plastic viscosity (Pa·s)
NC	2410	2.5	185	530	5.7	466.2	45.0
NC-5%SF	2400	2.3	175	510	4.9	527.9	48.4
NC-10%SF	2395	2.2	160	490	4.3	560.5	51.3

117

### 118 2.3. Evaluation of CA settlement

119 A method of segmented sieving was put forward to evaluate the settlement of  
120 CAs in the experiment. The schematic diagram of experimental steps is exhibited in  
121 Fig. 2. Here, a prismatic wooden mould with a cross section of 150 mm × 150 mm  
122 and a height of 500 mm was customized. The wooden boards were fixed by bolts, and  
123 the joints were coated with silicone gel to prevent leakage. A poker vibrator was used  
124 for vibrating and compacting, and its basic parameters are given in Table 4. The  
125 specimens were vibrated for 5 s, 15 s and 25 s, respectively. Note that the effective  
126 working radius of the vibrator used in experiment is 500 mm, which is much larger  
127 than the cross-sectional size of specimen, and the vibrating rod moves across the  
128 entire cross section to work during the vibration. Therefore, it is assumed that the  
129 vibration energy does not attenuate within the range of specimen, that is, the vibration  
130 amplitude and frequency of all particles in fresh concrete are approximately the same.

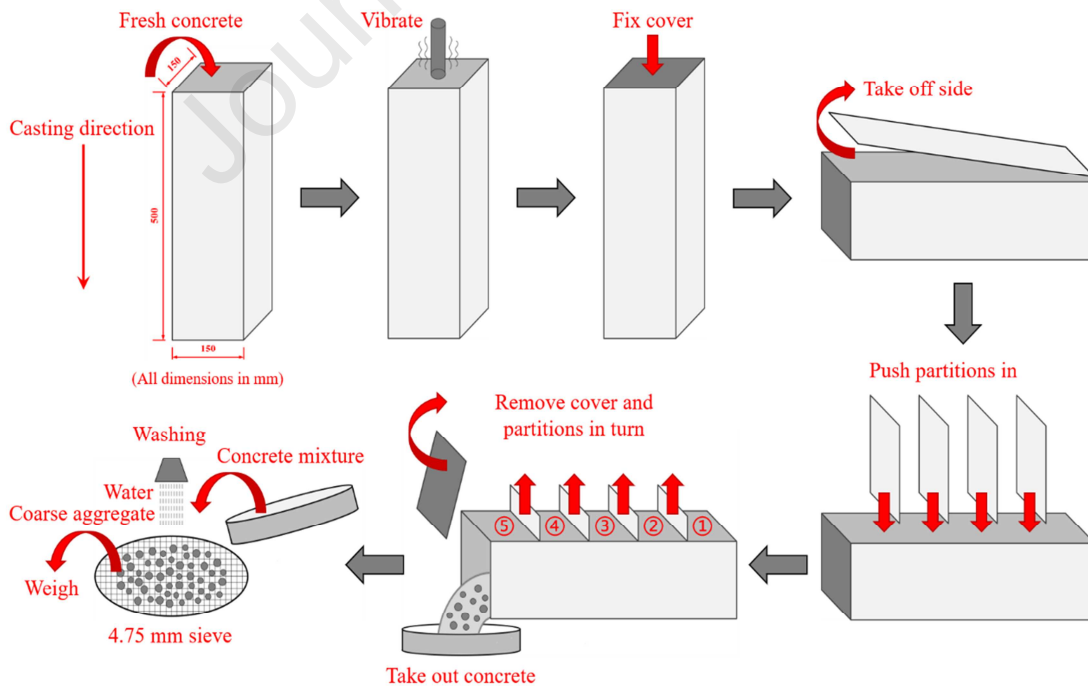
131 In the test, the right amount of fresh concrete was poured into the mould. After

132 the vibration, the top of the mould was covered with a wooden board and fastened  
 133 with bolts. Then the mould was slowly rotated by 90° from the original position, and  
 134 the side wall was taken off. Next, four pieces of metal slides were inserted vertically  
 135 along the designed iron grooves. The concrete mixtures were equally divided in five  
 136 layers along the casting direction. Subsequently, the cover and partitions were  
 137 removed in proper order. Concrete mixtures of each layer were poured into a 4.75 mm  
 138 sieve to rinse to remove mortars. Finally, the residual CAs were dried and weighed to  
 139 calculate the CA mass percentage of each layer in the specimen (see Eq. (2)).

$$140 \quad p_i = \frac{m_i}{M} \quad (i = 1, 2, 3, 4, 5) \quad (2)$$

141 where  $P_i$  is the mass percentage of CAs in the  $i$ -th layer,  $m_i$  is the mass of CAs in the  
 142  $i$ -th layer, and  $M$  is the total mass of all CAs in the specimen.

143



144

145

Fig. 2. Testing procedure of segmented sieving method.

146

147

Table 4 Basic parameters of the poker vibrator.

Type	Rod length (mm)	Rod diameter (mm)	Power (W)	Amplitude (mm)	Frequency (Hz)
YFY-01-35	1000	35	900	0.8	230

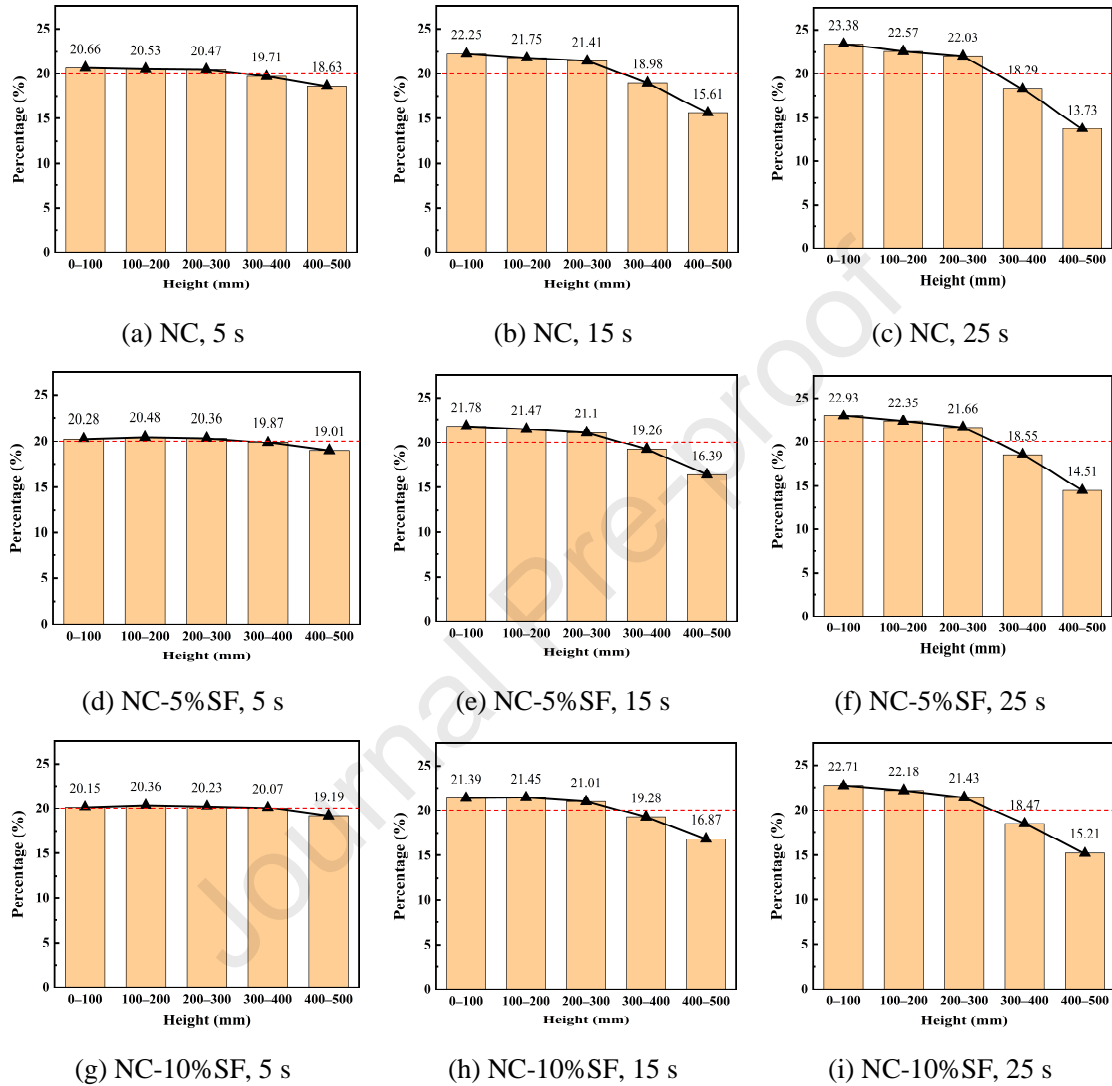
148

#### 149 *2.4. Analysis of experimental results*

150 Fig. 3 illustrates the results of CA distribution along casting direction measured  
 151 by the segmented sieving method. In order to eliminate the experimental errors and  
 152 ensure the repeatability of this method, each test result was determined by the average  
 153 of multiple groups of fresh concrete mixtures. It could be observed that, during the  
 154 vibrating procedure, CAs were gradually deposited to the bottom layer of concrete  
 155 mixtures under the action of gravity. At the same time, cement pastes and bleeding  
 156 water migrated upwards because of the buoyancy. After vibrating, settlement caused a  
 157 significant decrease in CA content of the top two layers. For the bottom part of  
 158 specimen, the content of CAs increased, but the variation was not as obvious as the  
 159 reduction in the top part. It was because a part of CAs gradually formed the close  
 160 packing in the bottom area after settling for a certain distance. The subsequent CAs  
 161 accumulated in the middle part of specimen, causing the CA mass percentages of the  
 162 second and third layers to be close to that of the first layer. The usage of SF could  
 163 increase the plastic viscosity of fresh cementitious materials [42–44]. It improved the  
 164 stability of fresh concrete and mitigated the settlement of CAs to a certain extent.

165 Besides, the larger dosage of SF had a more significant mitigation effect on  
 166 sedimentation phenomenon.

167



168 Fig. 3. Experimental results of CA settlement.

169

170 The degree of CA settlement is defined by the standard deviation of the CA mass  
 171 percentage of each layer in the specimen, calculated according to Eq. (3). It can reflect  
 172 the overall distribution of CAs, and the higher value indicates that the settlement and  
 173 heterogeneous distribution of CAs are more significant.

174

$$S = \sqrt{\frac{\sum_{i=1}^n (P_i - \bar{P})^2}{n}} \times 1000 \quad (3)$$

175

where  $S$  is the degree of settlement,  $P_i$  is the mass percentage of CAs in the  $i$ -th layer,

176

$\bar{P}$  is the average of CA mass percentage of each layer, which is 20%, and  $n$  is the

177

number of layers, which is 5.

178

The variation of the settlement degree of CAs with vibration time is displayed in

179

Fig. 4. It could be clearly understood from the figure that once vibration started, CAs

180

appeared unevenly distributed along the casting direction, and the heterogeneity of

181

CA distribution progressively increased. Adding SF into the concrete mixtures could

182

enhance the plastic viscosity, and reduce the settlement degree by 12.67%–45.33%

183

compared with NC. In addition, a part of CAs formed the dense packing and stopped

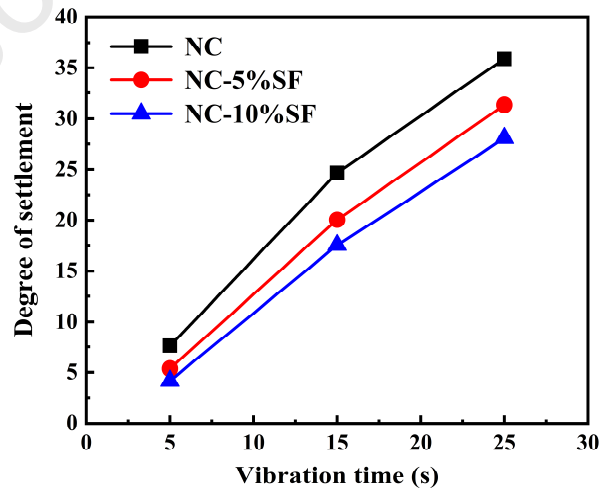
184

moving in the bottom part of specimen after a certain period of vibrating, thereby the

185

increase in the degree of CA settlement gradually weakened with the vibration time.

186



187

188

Fig. 4. Experimental results of the degree of CA settlement.

189

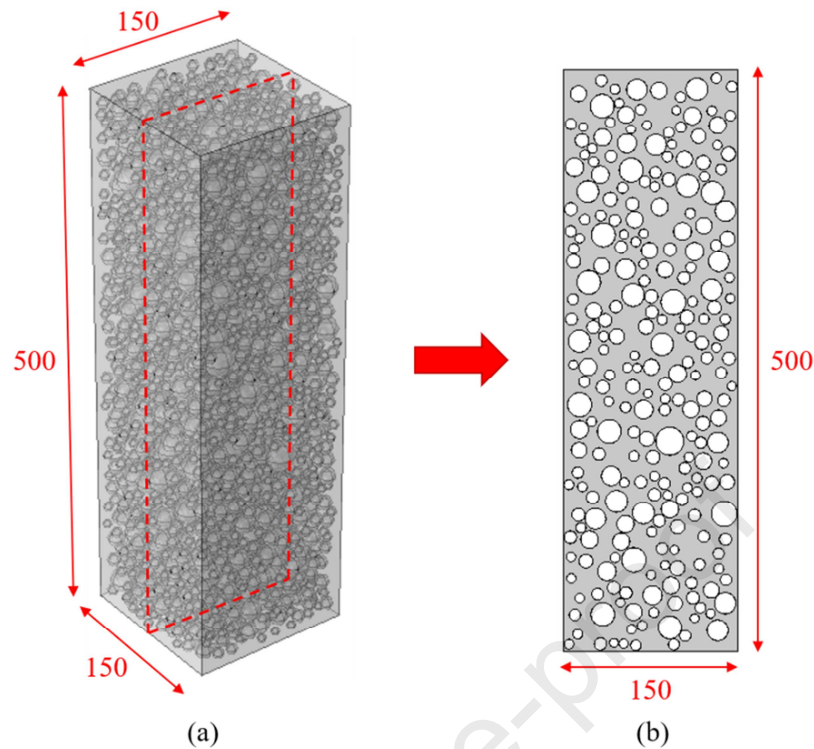
### 190 **3. Numerical model**

#### 191 *3.1. Modelling approach*

192 Numerical studies can provide accurate models at multiple scales to reflect the  
193 material compositions and meso/micro structures of concrete [45–47]. In this study, a  
194 3-D fresh concrete model is established at mesoscopic level, as shown in Fig. 5(a).  
195 The concrete is considered as a two-phase composite comprising CAs and mortars to  
196 facilitate the understanding of the settlement behaviour of CAs. The size of geometric  
197 model of the prismatic concrete specimen is 150 mm × 150 mm × 500 mm. The  
198 particle size of spherical CAs in the model is 5–20 mm, which is randomly generated  
199 according to the Fuller curve, and the volume fraction of CAs is 45%. These  
200 parameters are the same as the experiments.

201 Due to the relatively large size of the model, it contains too much CAs, which  
202 will block each other in the line of sight. For easier direct observation of the process  
203 of CA settlement, we extract some 2-D slices from the 3-D model along the vertical  
204 direction and find that the CA settlement in each slice is similar. In consequence, a  
205 slice in the middle of 3-D model is extracted vertically for the visual analysis (see Fig.  
206 5(b)). Of course, the calculation of CA content distribution is still based on the 3-D  
207 model. It can be seen from the figure that after casting and before vibrating, CAs are  
208 randomly and uniformly distributed in concrete.

209



210

211

212

213

214

215

216

217

218

219

220

Fig. 5. Schematic diagram of geometric model (all dimensions in mm).

It is generally believed that the yield stress can prevent CAs from settling in an undisturbed mortar matrix [22,39], but the yield stress is known to decrease to a very low value or even disappear at vibrating state and the plastic viscosity plays a decisive role in the settlement of CAs at this time [9–11,48,49]. Assuming that the yield stress is reduced to zero, a single CA particle is mainly subjected to three forces: gravity, buoyancy and viscous resistance in vibrated mortars. The force analysis of the CA is presented in Fig. 6.



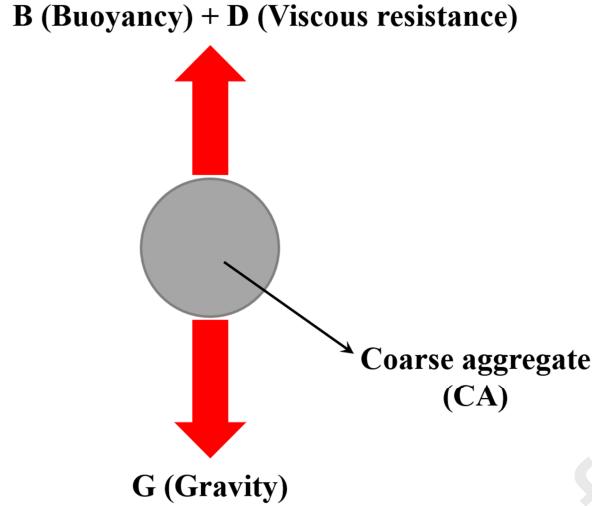


Fig. 6. Force analysis of the CA in vibrated mortars.

Gravity ( $G$ ) and buoyancy ( $B$ ) can be expressed as:

$$G = \rho_a V g = \frac{1}{6} \pi \rho_a d^3 g \quad (4)$$

$$B = \rho_m V g = \frac{1}{6} \pi \rho_m d^3 g \quad (5)$$

Here,  $\rho_a$  and  $\rho_m$  are the apparent densities of CAs and mortars, respectively. In the experiment,  $\rho_a$  is 2670 kg/m<sup>3</sup>.  $\rho_m$  is measured on a mortar sample, which is extracted from fresh concrete using a 4.75 mm sieve immediately after the completion of the mixing procedure. The apparent densities of mortars corresponding to the three groups of concrete mixtures are 2285 kg/m<sup>3</sup>, 2270 kg/m<sup>3</sup> and 2260 kg/m<sup>3</sup>, respectively.  $d$  is the diameter of CA particle in the range of 5–20 mm. And  $g$  is the acceleration due to gravity, which is 9.8 N/kg.

Stokes law describes the viscous resistance of a spherical object in the viscous fluid. The following assumptions hold: (1) the liquid extends infinitely, that is, the influence of container wall on the fluid movement is not considered; (2) the object is spherical and moves in a straight line with a constant velocity without deformation

238 during the movement; (3) the velocity of liquid on the surface of the sphere relative to  
 239 the centre is zero; (4) when the Reynolds number (Re) is small, the inertial effect can  
 240 be ignored. Here, Re is a dimensionless parameter that distinguishes the flow type of  
 241 fluid and it can be calculated as:

$$242 \quad \text{Re} = \frac{\rho_l v d}{\eta} \quad (6)$$

243 where  $\rho_l$  is the fluid density,  $v$  is the sphere velocity,  $d$  is the sphere diameter, and  $\eta$  is  
 244 the fluid viscosity.

245 When Re is less than 1, the flow is considered to be streamlined; when Re is  
 246 greater than  $10^3$ , the flow is turbulent; when Re is between the two, the flow is  
 247 transitional. In concrete mixtures, the movement velocity of CA particles is extremely  
 248 slow, and Re is much lower than 1. So the flow around the CA particles is streamlined,  
 249 and the expression of the viscous resistance ( $D$ ) is:

$$250 \quad D = 3\pi\eta v d \quad (7)$$

251 From the above analysis, it can be seen that when the density of the CA is greater  
 252 than that of the mortars, the CA will move downwards with acceleration, and the  
 253 viscous resistance also increases because of the increased CA velocity. When the  
 254 resultant force of viscous resistance, gravity and buoyancy reaches an equilibrium, the  
 255 CA will settle at a constant velocity. The final velocity can be demonstrated as:

$$256 \quad v_s = \frac{d^2 g (\rho_a - \rho_m)}{18\eta_{pl}} \quad (8)$$

257 where  $v_s$  is the final velocity of the CA, and  $\eta_{pl}$  is the plastic viscosity of mortars.

258 The CA in vibrated mortars can be divided into a varying accelerated motion  
 259 with a decreasing acceleration and a uniform motion. Through integral calculation, the

260 relationship between the vertical settlement height and vibration time can be derived  
 261 as:

$$\begin{aligned}
 \Delta h &= \frac{d^2 g (\rho_a - \rho_m)}{18\eta_{pl}} \cdot t - \frac{d^4 g \rho_a (\rho_a - \rho_m)}{324\eta_{pl}^2} \cdot \left[ 1 - \exp\left(-\frac{18\eta_{pl}}{d^2 \rho_a} \cdot t\right) \right] \\
 &= \frac{d^2 g (\rho_a - \rho_m)}{18\eta_{pl}} \cdot \left\{ t - \frac{d^2 \rho_a}{18\eta_{pl}} \cdot \left[ 1 - \exp\left(-\frac{18\eta_{pl}}{d^2 \rho_a} \cdot t\right) \right] \right\}
 \end{aligned} \tag{9}$$

263 where  $\Delta h$  is the settlement height of the CA, and  $t$  is the vibration time.

264 Since the particle size of CAs in this study is 0.005–0.02 m, the constant and  
 265 exponential terms in Eq. (9) are much smaller than the linear term. It can be seen that  
 266 the CA will accelerate to the final velocity in a rather short time, which can be ignored.  
 267 Moreover, Petrou et al. [39] find that, after the vibration, the yield stress of mortars is  
 268 restored immediately, and the dynamic CA will stop moving with a great acceleration  
 269 and stabilize in a static state. Hence, the distance of this deceleration motion can also  
 270 be ignored. It means that the CA settlement can be approximately regarded as a  
 271 uniform motion in the whole process of vibration, and its movement distance is  
 272 expressed as:

$$\Delta h = \frac{d^2 g (\rho_a - \rho_m)}{18\eta_{pl}} \cdot t \tag{10}$$

274 Eq. (10) shows the settlement height of a single CA in vibrated mortars. But, in  
 275 fact, each CA particle is also subjected to the interaction from other ones. In this case,  
 276 the plastic viscosity of mortars can be approximately replaced by that of concrete  
 277 mixtures, so as to consider the interaction between the CA particles [50–52].  
 278 Furthermore, the plastic viscosity of fresh concrete measured in Section 2.2 needs to  
 279 be calibrated, because the Bingham model is no longer completely suitable to

280 characterize the rheology of fresh cement-based materials under the action of  
 281 vibration. Consequently, the settlement height of the CA can be revised to:

$$282 \quad \Delta h' = \frac{d^2 g (\rho_a - \rho_m)}{18k\eta_{pl}'} \cdot t \quad (11)$$

283 In Eq. (11),  $\Delta h'$  is the actual settlement height of the CA,  $\eta_{pl}'$  is the plastic  
 284 viscosity of fresh concrete, and  $k$  is the non-dimensional calibration coefficient for  $\eta_{pl}'$ .  
 285 The specific value of  $k$  will be determined in Section 3.2, which is related to the raw  
 286 materials and experimental conditions.

287

### 288 3.2. Model calibration

289 Theoretically, the final height position of a single CA after settlement can be  
 290 expressed by Eq. (12) through the previous calculation and derivation.

$$291 \quad h' = h - \frac{d^2 g (\rho_a - \rho_m)}{18k\eta_{pl}'} \cdot t \quad (12)$$

292 where  $h$  is the initial height position of the CA, and  $h'$  is the final height position of  
 293 the CA after settlement.

294 It should be noted that the CAs with different particle sizes have a different  
 295 settlement rate, which will cause some of them to intersect in the model. To this end,  
 296 the whole vibration process is divided into many short-time parts, and the vibration  
 297 time of each step is set as 0.05 s. The final settlement model is generated by  
 298 superposition of each part step by step, until the expected vibration time is reached. At  
 299 the end of each part, if the CAs intersect, the involved ones are randomly bounced to  
 300 the nearby empty space and ensure that they will not intersect with other CAs again.

301 Considering that the CAs will be wrapped with a layer of pastes (interfacial transition  
 302 zone) with a thickness of 20–50  $\mu\text{m}$  [53–55], the minimum distance between the CA  
 303 surfaces is set as 100  $\mu\text{m}$  in this study.

304 In the model, the parameter information of every CA particle can be easily  
 305 determined at any time and any position. The 3-D model is equally divided into five  
 306 layers along the height direction, and all CAs are distributed in each layer based on  
 307 the final position of the centre height of them. According to Eq. (13), the CA volume  
 308 percentage of each layer in the model can be calculated.

$$309 \quad P_i' = \frac{V_i}{V} (i=1,2,3,4,5) \quad (13)$$

310 where  $P_i'$  is the volume percentage of CAs in the  $i$ -th layer,  $V_i$  is the volume of CAs in  
 311 the  $i$ -th layer, and  $V$  is the total volume of all CAs in the model.

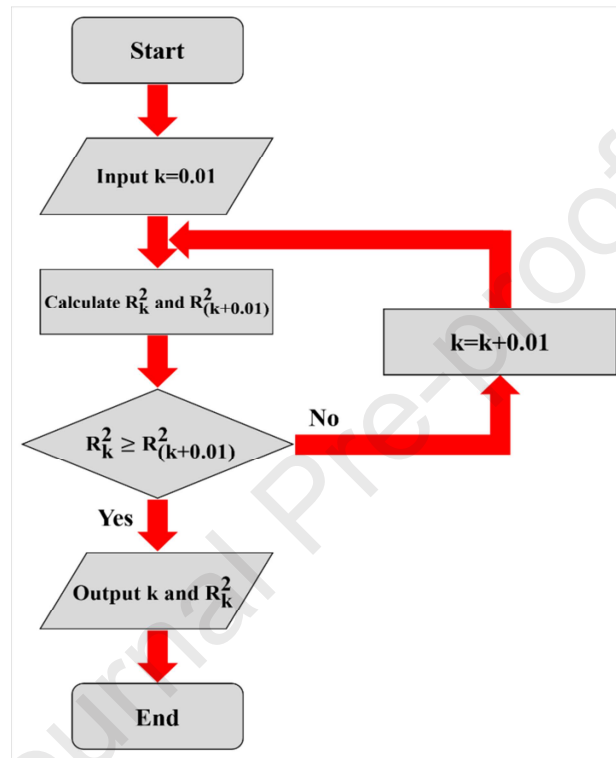
312 Since the density of all CAs is the same, the volume percentage of CAs in each  
 313 layer ( $P_i'$ ) can be fitted with the mass percentage ( $P_i$ ) according to the experimental  
 314 results of Fig. 3 to calculate the calibration coefficient ( $k$ ) used in Eq. (11). The  
 315 algorithm flow chart of  $k$  and correlation coefficient ( $R^2$ ) is presented in Fig. 7.  $R^2$  is  
 316 calculated by the linear fitting function of software. It can be predicted that the value  
 317 of  $R^2$  will increase firstly and then decrease with the increase of  $k$ , that is, there is a  
 318 peak value of  $R^2$ . When  $R^2$  reaches its maximum value, the algorithm ends. It is found  
 319 that when  $k$  is 0.62, the results of numerical model and experiment are in the best  
 320 agreement. In that case,  $R^2$  is 0.9865. The original data comparison between the  
 321 model and experimental results is shown in Table 5, and the fitting result is shown in  
 322 Fig. 8. The fitting function is self-set as  $y=x$ , and the abscissa and ordinate represent

323 the results of experiment and numerical model, respectively. Note that  $k$  is less than 1.

324 It means that vibration reduces the plastic viscosity of fresh concrete compared to that

325 in the stable state.

326



327

328

Fig. 7. Algorithm flow chart.

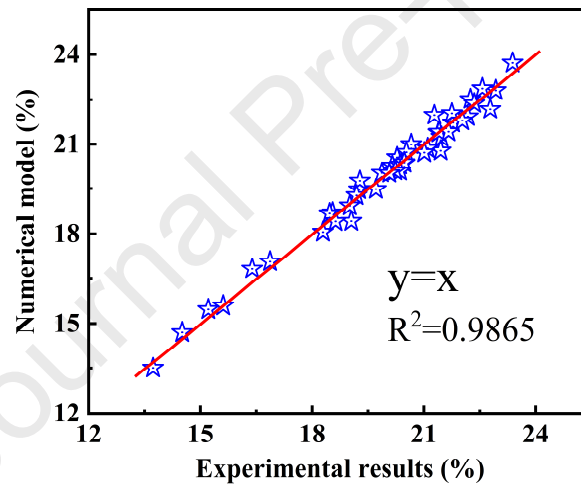
329

330 Table 5 Comparison of the percentage of CA distribution between the model and experiment.

Vibration time	Layer	NC		NC-5%SF		NC-10%SF	
		Model	Experiment	Model	Experiment	Model	Experiment
5 s	1	20.99%	20.66%	20.56%	20.28%	20.28%	20.15%
	2	20.73%	20.53%	20.37%	20.48%	20.31%	20.36%
	3	20.39%	20.47%	20.10%	20.36%	20.11%	20.23%
	4	19.48%	19.71%	20.04%	19.87%	20.03%	20.07%
	5	18.41%	18.63%	18.93%	19.01%	19.27%	19.19%

	1	22.51%	22.25%	21.71%	21.78%	21.38%	21.39%
	2	22.03%	21.75%	21.23%	21.47%	21.05%	21.45%
15 s	3	21.40%	21.41%	20.86%	21.10%	20.72%	21.01%
	4	18.47%	18.98%	19.47%	19.26%	19.77%	19.28%
	5	15.59%	15.61%	16.73%	16.39%	17.08%	16.87%
	1	23.72%	23.38%	22.81%	22.93%	22.27%	22.71%
	2	22.87%	22.57%	22.37%	22.35%	21.92%	22.18%
25 s	3	21.78%	22.03%	21.41%	21.66%	21.67%	21.43%
	4	18.06%	18.29%	18.70%	18.55%	18.67%	18.47%
	5	13.57%	13.73%	14.71%	14.51%	15.47%	15.21%

331



332

333

Fig. 8. Fitting between numerical model and experimental results.

334

335

336

337

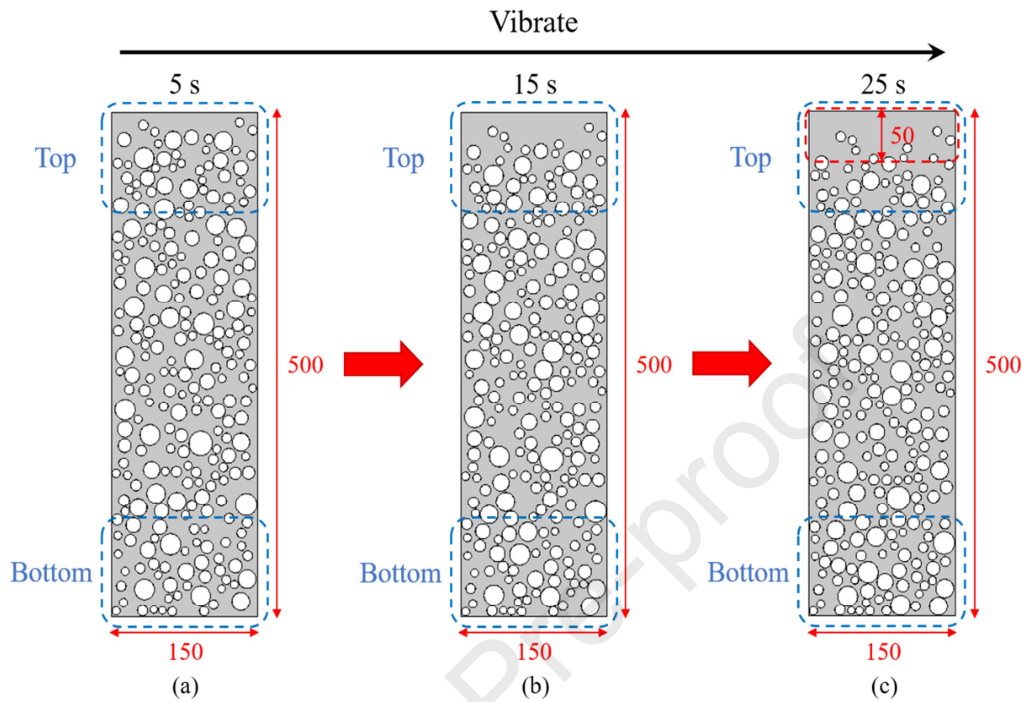
338

339

Taking the group of NC as an example, firstly, a 3-D geometric model was generated, and then a 2-D slice was extracted to facilitate the visual observation of CA settlement, as depicted in Fig. 9. As the vibration progressed, CAs gradually deposited to the bottom part of specimen, and the distribution profiles presented an increased content of CAs towards the bottom layer. For a single CA, the CA with a larger

340 particle size showed a more notable settlement distance.

341



342

343 Fig. 9. Visual analysis of CA settlement under vibration (all dimensions in mm).

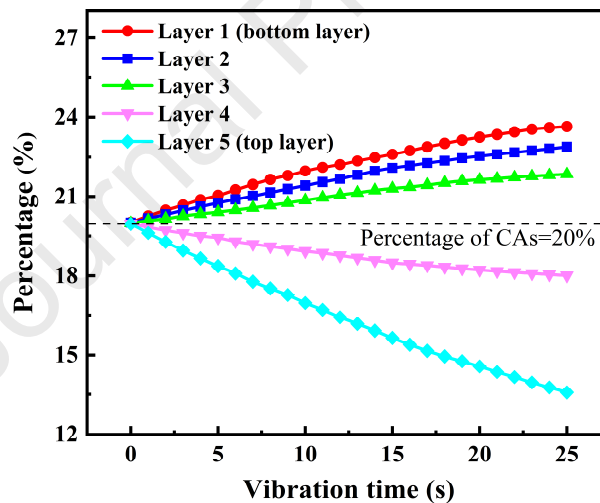
344

345 It was noteworthy that the CA content in the top part of specimen was  
 346 significantly decreased, especially when the vibration time reached 25 s, there were  
 347 most of mortars and only few of small-sized CAs in the top 50 mm-height area (see  
 348 Fig. 9(c)). Megid and Khayat [56] observed similar phenomena in their experiment.  
 349 The settlement of CAs led to the formation of a porous surface layer enriched in  
 350 cement pastes in the top part of concrete specimen, where might be prone to  
 351 experience shrinkage and cracking [57,58]. In addition, it could be clearly seen from  
 352 the figure that CAs in the bottom part indeed formed a close packing in the local  
 353 space, which confirmed the previous interpretation of the experimental results.

354 On the basis of the 3-D model, the volume percentages of CAs in the five layers



355 were calculated, as illustrated in Fig. 10. Evidently, as the vibration time increased,  
 356 the heterogeneity of CA distribution along casting direction was gradually  
 357 strengthened, which was reflected in the obvious decrease of CA content in the top  
 358 part and the increase of that in the bottom part. This was consistent with the direct  
 359 observation shown in Fig. 9. Besides, for concrete mixtures having different w/b or  
 360 mix proportions, as long as the relevant rheological parameter of mixtures and raw  
 361 material information were input into the model, the CA settlement behaviour could  
 362 also be easily displayed. The proposed methodology had potential application  
 363 prospects in large-scale structural concrete cast in practice and 3-D printed concrete.  
 364



365  
 366 Fig. 10. The CA volume percentages of these five layers in NC.

367

#### 368 4. Prediction and discussion

369 The settlement of CAs is a common phenomenon in fresh concrete due to  
 370 vibration, and the visually method can provide an important and effective way to  
 371 reveal the settlement behaviour of CAs. Based on the numerical approach proposed in

372 this study, a corresponding 3-D model can be established to predict the degree of CA  
373 settlement under different influencing factors, for example, the vibration time, the  
374 apparent density and particle size of CAs, and the plastic viscosity of mixtures. It not  
375 only has the advantages of convenience and visualization, but also can further make a  
376 theoretical explanation for such a rheological problem in vibrated concrete.

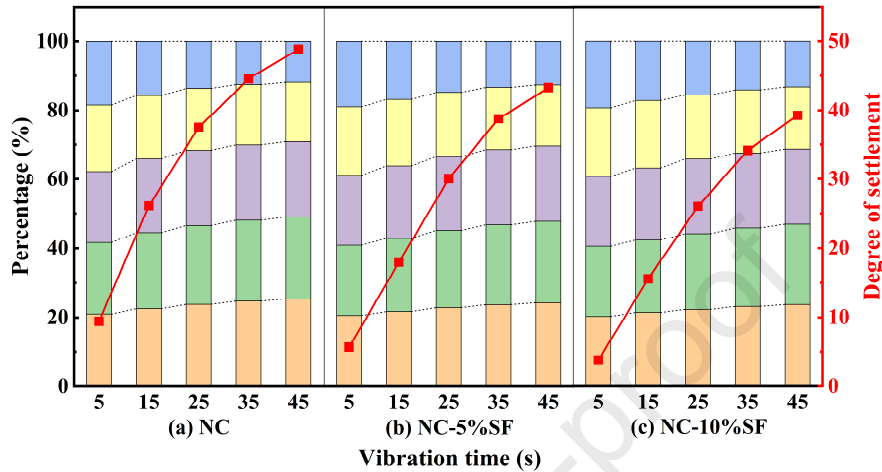
#### 377 *4.1. Influence of vibration time*

378 The distribution of CAs along casting direction under different vibration time is  
379 shown in Fig. 11. The orange, green, purple, yellow and blue histograms in the figure  
380 represent the volume percentages of CA content from the first layer to the fifth layer  
381 of the total, respectively. And the line chart shows the standard deviation of the CA  
382 volume percentages of these five layers to characterize the degree of CA settlement  
383 (like Eq. (3)). An obvious impact of vibration time on CA settlement could be  
384 observed. As the vibrating duration became longer, the heterogeneity of CA  
385 distribution gradually increased. After vibrating for a certain period of time, due to the  
386 dense packing of some CAs in the bottom part of specimen, the growing trend of  
387 settlement degree became slower. It should be noted that the addition of SF would  
388 delay the initial time of that a part of CAs in the bottom area formed a close packing.

389 In engineering practice, long-time vibration should be avoided, because  
390 excessive vibration would aggravate the settlement, segregation and bleeding of fresh  
391 concrete. On the contrary, too short vibration time might make it difficult for each  
392 component in mixtures to combine closely and entrapped air voids could not be  
393 completely removed from the surface of specimen, which also might affect the quality

394 of hardened concrete. Therefore, when casting fresh concrete, the vibration time  
 395 should be strictly controlled, usually 20–30 s.

396



397

398

Fig. 11. Influence of the vibration time on CA settlement.

399

#### 400 4.2. Influence of CA apparent density

401

402

403

404

405

406

407

408

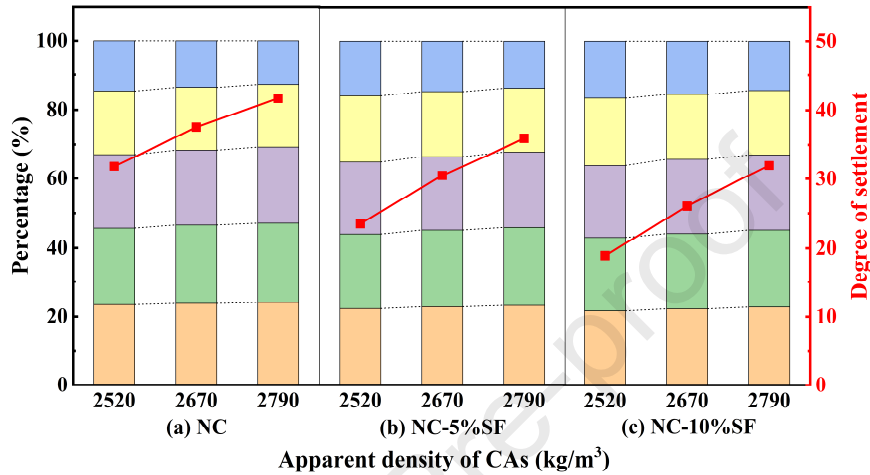
409

410

The properties of CAs, such as apparent density, particle size distribution and appearance shape, may all have a certain influence on the degree of settlement [12,38,59–66]. Considering that the laboratory could offer additional CAs with apparent densities of  $2520 \text{ kg/m}^3$  and  $2790 \text{ kg/m}^3$ , a numerical model of the influence of apparent density on settlement was carried out, and the vibration time was set as 25 s. From Fig. 12, it showed that the CAs with a larger apparent density presented a higher difference between the densities of the CA and the mortar matrix, resulting in a greater sedimentation tendency. This was in line with the finding of Navarrete and Lopez [59], who believed that the settlement rate had a linear relationship with the density difference between CAs and mortars for a given mixture. Furthermore, Chia et

411 al. [60] and Ke et al. [61] studied the settlement behaviour of lightweight CA concrete  
 412 under vibration. They claimed that when the density of CAs was less than that of the  
 413 mortars, the CAs would appear to float.

414



415

416

Fig. 12. Influence of the apparent density of CAs on settlement.

417

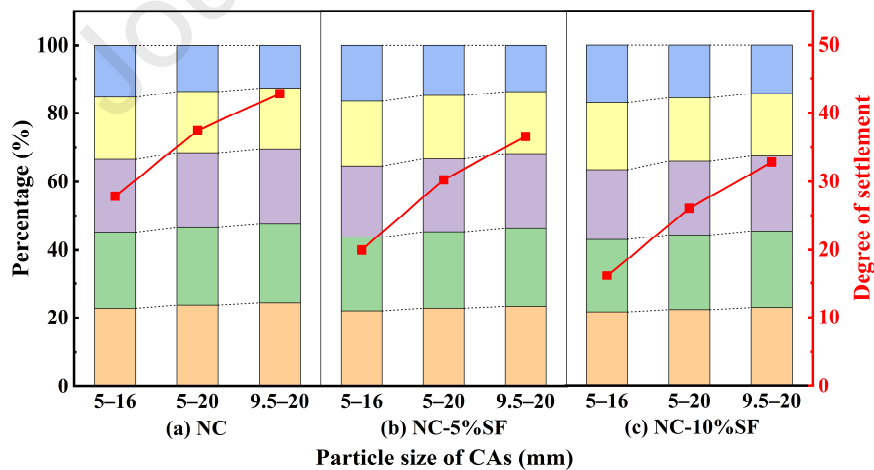
#### 418 4.3. Influence of CA particle size

419 In Fig. 13, three particle size distributions of CAs were designed, namely 5–16  
 420 mm, 5–20 mm and 9.5–20 mm, and the vibration time was also 25 s. The reason for  
 421 distinguishing the range of particle size in this way was that it could be easily  
 422 obtained through the sieves of 9.5 mm and 16 mm sizes in the laboratory, which was  
 423 beneficial to the subsequent experimental verification. Under the action of vibration,  
 424 the mixtures which contained more large-sized CAs had a greater degree of settlement  
 425 for the same CA volume fraction, that was, the distribution of CAs in concrete  
 426 presented a more evident non-uniformity. This was consistent with the results of  
 427 Safawi et al. [38]. In their experiment, the CAs with particle sizes of 5–13 mm and

428 13–20 mm were used to prepare fresh concrete mixtures, respectively. The results  
 429 showed that the large-sized CAs were more affected due to vibration than the  
 430 small-sized ones. It meant that the larger-sized CAs were more dominant in  
 431 determining the settlement degree compared with smaller ones. Similarly,  
 432 Esmailkhanian et al. [12] and Shen et al. [62] also found that concrete mixtures with  
 433 lower maximum size CAs tended to settle and segregate less.

434 Moreover, compared with the particle size distribution of CAs which increased  
 435 from 5–20 mm to 9.5–20 mm, the increase in the settlement degree of the particle size  
 436 from 5–16 mm to 5–20 mm was more obvious. It was because, although the particle  
 437 size of CAs increased in both cases, the CAs with a larger particle size were more  
 438 likely to form a dense packing when they deposited in the bottom part of specimen,  
 439 which could prevent the settlement movement to a certain extent.

440



441

442

Fig. 13. Influence of the particle size of CAs on settlement.

443

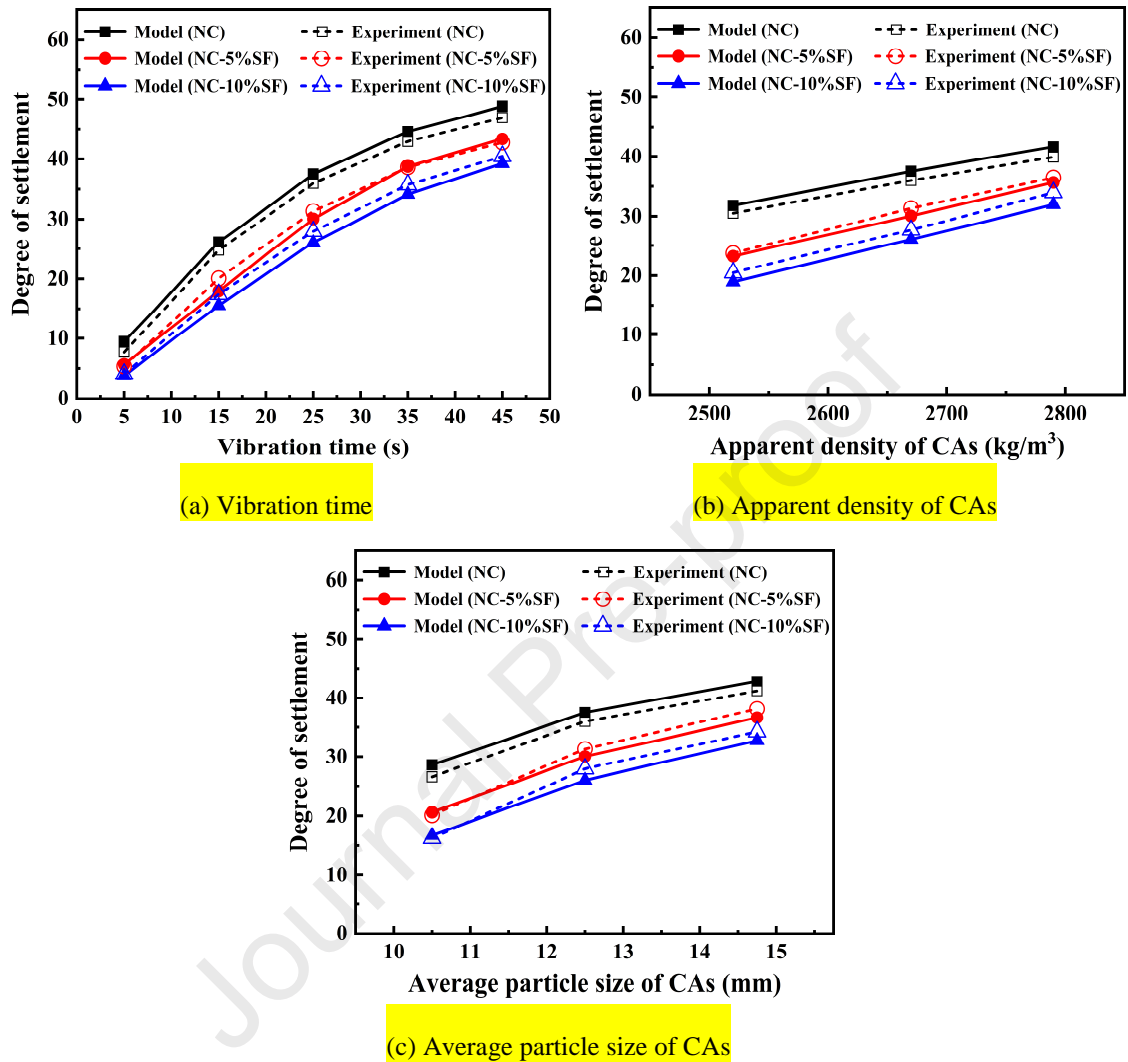
#### 444 4.4. Verification of prediction results

445 In Sections 4.1–4.3, the numerical model was used to predict the influence of  
446 vibration time, apparent density and particle size of CAs on settlement degree in the  
447 three groups of concrete mixtures. Next, the validity of the proposed model based on  
448 experimental results would be discussed in this section. Although the vibration time of  
449 fresh concrete usually did not exceed 30 s, the tests of vibrating durations of 35 s and  
450 45 s were still carried out to validate the previous prediction. In addition, the  
451 limestone with apparent densities of 2520 kg/m<sup>3</sup> and 2790 kg/m<sup>3</sup> prepared in the  
452 laboratory could be used to test the influence of the CA density on settlement. For the  
453 experiment of the effect of the CA particle size, the CAs with diameters of 5–16 mm  
454 and 9.5–20 mm could be obtained from original particle size (5–20 mm) through 16  
455 mm and 9.5 mm size sieves, respectively.

456 The experimental results determined by the segmented sieving method were used  
457 to verify the prediction results of numerical model, as presented in Fig. 14. For the  
458 vibration time, the model prediction was in good agreement with the experimental  
459 results as evident in Fig. 14(a). With the vibration time going on, both the settlement  
460 degree and heterogeneity distribution of CAs were more pronounced. When the  
461 vibration time reached a certain value, the increase of settlement degree became  
462 slower due to the close packing of some CAs in the bottom layer. Similarly, when the  
463 numerical method was used to predict the influence of the apparent density and  
464 particle size of CAs on settlement, it also showed a good correlation with the  
465 experimental results (see Fig. 14(b) and (c)), which indicated that the model was

466 applicable in this study.

467



468 Fig. 14. Experimental verification of the prediction results.

469

#### 470 4.5. Grey relational analysis

471 The grey relational analysis table of different influencing factors is summarized  
 472 in Table 6. Here, this method is used to characterize the contribution of each factor to  
 473 CA settlement. The settlement degree is taken as the reference sequence. The  
 474 influencing factors such as vibration time, apparent density and particle size of CAs,

475 and plastic viscosity of mixtures are taken as the comparable sequences.

476

477 Table 6 Grey relational analysis table of different influencing factors.

Group	Vibration time (s)	Apparent density of CAs (kg/m <sup>3</sup> )	Particle size of CAs (mm)	Plastic viscosity of mixtures (Pa·s)	Degree of settlement
1	5	2670	5–20	45.0	9.4484
2	15	2670	5–20	45.0	26.1419
3	25	2670	5–20	45.0	37.5106
4	35	2670	5–20	45.0	44.6035
5	45	2670	5–20	45.0	48.8770
6	5	2670	5–20	48.4	5.6692
7	15	2670	5–20	48.4	17.9724
8	25	2670	5–20	48.4	30.0583
9	35	2670	5–20	48.4	38.7519
10	45	2670	5–20	48.4	43.3282
11	5	2670	5–20	51.3	3.7958
12	15	2670	5–20	51.3	15.5593
13	25	2670	5–20	51.3	26.0454
14	35	2670	5–20	51.3	34.1547
15	45	2670	5–20	51.3	39.2495
16	25	2520	5–20	45.0	31.8085
17	25	2790	5–20	45.0	41.6522
18	25	2520	5–20	48.4	23.2047
19	25	2790	5–20	48.4	35.6362
20	25	2520	5–20	51.3	18.9375
21	25	2790	5–20	51.3	31.9706
22	25	2670	5–16	45.0	28.0206
23	25	2670	9.5–20	45.0	42.8769
24	25	2670	5–16	48.4	20.3044
25	25	2670	9.5–20	48.4	36.6233
26	25	2670	5–16	51.3	16.4197
27	25	2670	9.5–20	51.3	32.7796
Grey relational grade	0.7392	0.6291	0.6435	0.6222	–

478

479 Assuming the reference and comparable sequences are respectively denoted as

480  $X_0(k)$  and  $X_i(k)$ . Before conducting a grey relational analysis, the original reference

481 and comparable sequences need to be normalized by data pre-processing, as follows:



$$482 \quad x_0(k) = \frac{X_0(k)}{\frac{1}{n} \sum_{k=1}^n X_0(k)} \quad (14)$$

$$483 \quad x_i(k) = \frac{X_i(k)}{\frac{1}{n} \sum_{k=1}^n X_i(k)} \quad (15)$$

484 where  $x_0(k)$  and  $x_i(k)$  are the sequences after data pre-processing, and  $i=1, 2, \dots, m$  and  
 485  $k=1, 2, \dots, n$ .

486 When the dimensionless data are prepared, the grey relational coefficient can be  
 487 derived by Eq. (16).

$$488 \quad \varepsilon_i(k) = \frac{\Delta_{\min} + \rho \Delta_{\max}}{\Delta_{0i}(k) + \rho \Delta_{\max}} \quad (16)$$

489 Here, the absolute difference between each evaluated comparable sequence and  
 490 the corresponding element of reference sequence is calculated in turn, and then  $\Delta_{\min}$ ,  
 491  $\Delta_{\max}$  and  $\Delta_{0i}(k)$  can be obtained by Eqs. (17)–(19). Moreover,  $\rho$  is called the resolution  
 492 coefficient, and the smaller  $\rho$  indicates the greater resolution. In general, the value of  $\rho$   
 493 is 0.5.

$$494 \quad \Delta_{\min} = \min_i \min_k |x_0(k) - x_i(k)| \quad (17)$$

$$495 \quad \Delta_{\max} = \max_i \max_k |x_0(k) - x_i(k)| \quad (18)$$

$$496 \quad \Delta_{0i}(k) = |x_0(k) - x_i(k)| \quad (19)$$

497 As the calculated relational coefficients are not only large in quantity, but also  
 498 discrete, it is impossible to directly compare them. It needs to average the relational  
 499 coefficients to convert each sequence into a relational grade, as shown in Eq. (20).

$$500 \quad \gamma_i = \frac{1}{n} \sum_{k=1}^n \varepsilon_i(k) \quad (20)$$

501 where  $\gamma_i$  is the grey relational grade.

502 On the basis of the principle of grey relational analysis, a larger value of  $\gamma_i$   
503 implies that the related influencing factor has a greater impact on CA settlement. After  
504 calculation, it is found that the grey relational grades of the influencing factors are  $\gamma$   
505 (vibration time) = 0.7392,  $\gamma$  (apparent density of CAs) = 0.6291,  $\gamma$  (particle size of  
506 CAs) = 0.6435, and  $\gamma$  (plastic viscosity of mixtures) = 0.6222, respectively. It means  
507 that the order of these four influencing factors for the contribution of CA settlement in  
508 this study is vibration time > particle size of CAs > apparent density of CAs > plastic  
509 viscosity of mixtures. This supports the general observation that vibration time should  
510 be limited in practical applications.

511

## 512 **5. Conclusions**

513 In this study, an experimental and numerical work of CA settlement in vibrated  
514 fresh concrete was investigated. Based on the previous results and discussion, the  
515 following conclusions could be drawn:

516 1) The distribution profiles of CAs in vibrated concrete presented a growing  
517 tendency towards the bottom layer with vibration time. After a certain period of  
518 vibrating, some CAs in the bottom part formed the close packing, and the growth  
519 of the non-uniform distribution gradually began to weaken.

520 2) Due to the opacity of concrete, the proposed 3-D model for fresh concrete could  
521 be used as a potential approach to visualize the CA movement. For the top part of  
522 specimen, the visual analysis showed that a surface layer enriched in cement  
523 mortars formed in this area, where only contained few of small-sized CAs.

- 524 3) The heterogeneity of concrete had a positive correlation with the density  
525 difference between CAs and mortars and the particle size of CAs. SF, as a mineral  
526 admixture to improve the plastic viscosity of mixtures, could effectively reduce  
527 the settlement and segregation of fresh cement-based materials.
- 528 4) The segmented sieving method was performed to assess the validity of numerical  
529 model. The results indicated that the model prediction was well verified by the  
530 experimental results. The methodology proposed in this study provided an  
531 effective tool to further understand the settlement behaviour of CAs.
- 532 5) Grey relational analysis demonstrated that the vibration time had the greatest  
533 influence on CA settlement, followed by the particle size of CAs. Compared with  
534 the former two influencing factors, the apparent density of CAs and the plastic  
535 viscosity of mixtures contributed a little to the settlement.

536

### 537 **Acknowledgments**

538 This work was funded by the National Natural Science Foundation of China  
539 [51978396] and the Shanghai Rising-Star Program, China [19QA1404700].

540

### 541 **References**

- 542 [1] K. Kovler, N. Roussel, Properties of fresh and hardened concrete, *Cem. Concr. Res.* 41 (7)  
543 (2011) 775–792.
- 544 [2] N. Roussel, A theoretical frame to study stability of fresh concrete, *Mater. Struct.* 39 (1) (2006)  
545 81–91.

- 546 [3] D. Jiao, C. Shi, Q. Yuan, X. An, Y. Liu, H. Li, Effect of constituents on rheological properties  
547 of fresh concrete-A review, *Cem. Concr. Compos.* 83 (2017) 146–159.
- 548 [4] G. Torelli, J.M. Lees, Fresh state stability of vertical layers of concrete, *Cem. Concr. Res.* 120  
549 (2019) 227–243.
- 550 [5] W.S. Alyhya, S. Kulasegaram, B.L. Karihaloo, Simulation of the flow of self-compacting  
551 concrete in the V-funnel by SPH, *Cem. Concr. Res.* 100 (2017) 47–59.
- 552 [6] J. Zhang, X. Gao, Y. Su, Influence of poker vibration on aggregate settlement in fresh concrete  
553 with variable rheological properties, *J. Mater. Civ. Eng.* 31 (7) (2019) 04019128.
- 554 [7] W. Yan, W. Cui, L. Qi, Effect of aggregate gradation and mortar rheology on static  
555 segregation of self-compacting concrete, *Constr. Build. Mater.* 259 (2020) 119816.
- 556 [8] M.I. Safawi, I. Iwaki, T. Miura, A study on the applicability of vibration in fresh high fluidity  
557 concrete, *Cem. Concr. Res.* 35 (9) (2005) 1834–1845.
- 558 [9] G.H. Tattersall, P.H. Baker, The effect of vibration on the rheological properties of fresh  
559 concrete, *Mag. Concr. Res.* 40 (143) (1988) 79–89.
- 560 [10] G.H. Tattersall, P.H. Baker, An investigation into the effect of vibration on the workability of  
561 fresh concrete using a vertical pipe apparatus, *Mag. Concr. Res.* 41 (146) (1989) 3–9.
- 562 [11] C. Hu, F. de Larrard, The rheology of fresh high-performance concrete, *Cem. Concr. Res.* 26  
563 (2) (1996) 283–294.
- 564 [12] B. Esmailkhanian, K.H. Khayat, A. Yahia, D. Feys, Effects of mix design parameters and  
565 rheological properties on dynamic stability of self-consolidating concrete, *Cem. Concr. Compos.*  
566 54 (2014) 21–28.

- 567 [13] C. Pichler, R. Rock, R. Lackner, Apparent power-law fluid behavior of vibrated fresh  
568 concrete: Engineering arguments based on Stokes-type sphere viscometer measurements, *J.*  
569 *Non-Newtonian Fluid Mech.* 240 (2017) 44–55.
- 570 [14] W. Zhu, J.C. Gibbs, P.J.M. Bartos, Uniformity of in situ properties of self-compacting  
571 concrete in full-scale structural elements, *Cem. Concr. Compos.* 23 (1) (2001) 57–64.
- 572 [15] A. Leemann, B. Munch, P. Gasser, L. Holzer, Influence of compaction on the interfacial  
573 transition zone and the permeability of concrete, *Cem. Concr. Res.* 36 (8) (2006) 1425–1433.
- 574 [16] D.K. Panesar, B. Shindman, The effect of segregation on transport and durability properties  
575 of self consolidating concrete, *Cem. Concr. Res.* 42 (2) (2012) 252–264.
- 576 [17] X. Gao, J. Zhang, Y. Su, Influence of vibration-induced segregation on mechanical property  
577 and chloride ion permeability of concrete with variable rheological performance, *Constr. Build.*  
578 *Mater.* 194 (2019) 32–41.
- 579 [18] Y. Cai, W. Zhang, L. Yu, M. Chen, C. Yang, R. François, K. Yang, Characteristics of the  
580 steel-concrete interface and their effect on the corrosion of steel bars in concrete, *Constr. Build.*  
581 *Mater.* 253 (2020) 119162.
- 582 [19] W. Zhang, R. François, Y. Cai, J.-P. Charron, L. Yu, Influence of artificial cracks and  
583 interfacial defects on the corrosion behavior of steel in concrete during corrosion initiation under a  
584 chloride environment, *Constr. Build. Mater.* 253 (2020) 119165.
- 585 [20] Y. Cai, W. Zhang, C. Yang, R. François, L. Yu, M. Chen, H. Chen, H. Yang, Evaluating the  
586 chloride permeability of steel–concrete interface based on concretes of different stability, *Struct.*  
587 *Concr.* (2020) 1–14.

- 588 [21] C. Wu, C. Chen, C. Cheeseman, Size effects on the mechanical properties of 3D printed  
589 plaster and PLA parts, *J. Mater. Civ. Eng.* 33 (7) (2021) 04021152.
- 590 [22] M.F. Petrou, K.A. Harries, F. Gadala-Maria, V.G. Kolli, A unique experimental method for  
591 monitoring aggregate settlement in concrete, *Cem. Concr. Res.* 30 (5) (2000) 809–816.
- 592 [23] J.A. Koch, D.I. Castaneda, R.H. Ewoldt, D.A. Lange, Vibration of fresh concrete understood  
593 through the paradigm of granular physics, *Cem. Concr. Res.* 115 (2019) 31–42.
- 594 [24] Z. Tian, X. Li, F. Zhu, Z. Peng, Experimental simulation study on aggregate motion of  
595 rheological concrete, *J. Build. Mater.* 19 (1) (2016) 22–28.
- 596 [25] F.S. Barbosa, A.L. Beaucour, M.C.R. Farage, S. Ortola, Image processing applied to the  
597 analysis of segregation in lightweight aggregate concretes, *Constr. Build. Mater.* 25 (8) (2011)  
598 3375–3381.
- 599 [26] I. Navarrete, M. Lopez, Understanding the relationship between the segregation of concrete  
600 and coarse aggregate density and size, *Constr. Build. Mater.* 149 (2017) 741–748.
- 601 [27] M. Nili, M. Razmara, M. Sadeghi, M. Razmara, Automatic image analysis process to  
602 appraise segregation resistance of self-consolidating concrete, *Mag. Concr. Res.* 70 (8) (2018)  
603 390–399.
- 604 [28] M. Benaicha, O. Jalbaud, X. Roguiez, A.H. Alaoui, Y. Burtshell, Prediction of  
605 Self-Compacting Concrete homogeneity by ultrasonic velocity, *Alex. Eng. J.* 54 (4) (2015) 1181–  
606 1191.
- 607 [29] K.H. Khayat, T.V. Pavate, J. Assaad, C. Jolicoeur, Analysis of variations in electrical  
608 conductivity to assess stability of cement-based materials, *ACI Mater. J.* 100 (4) (2003) 302–310.

- 609 [30] Y. Vanhove, C. Djelal, G. Schwendenmann, P. Brisset, Study of self consolidating concretes  
610 stability during their placement, *Constr. Build. Mater.* 35 (2012) 101–108.
- 611 [31] H.S. Gokce, B.C. Ozturk, N.F. Çam, O. Andiç-Çakir, Gamma-ray attenuation coefficients  
612 and transmission thickness of high consistency heavyweight concrete containing mineral  
613 admixture, *Cem. Concr. Compos.* 92 (2018) 56–69.
- 614 [32] F. Mahmoodzadeh, S.E. Chidiac, Rheological models for predicting plastic viscosity and  
615 yield stress of fresh concrete, *Cem. Concr. Res.* 49 (2013) 1–9.
- 616 [33] J. Peng, D. Deng, Z. Liu, Q. Yuan, T. Ye, Rheological models for fresh cement asphalt paste,  
617 *Constr. Build. Mater.* 71 (2014) 254–262.
- 618 [34] V. Mechtcherine, S. Shyshko, Simulating the behaviour of fresh concrete with the Distinct  
619 Element Method – Deriving model parameters related to the yield stress, *Cem. Concr. Compos.* 55  
620 (2015) 81–90.
- 621 [35] K. Vance, G. Sant, N. Neithalath, The rheology of cementitious suspensions: A closer look at  
622 experimental parameters and property determination using common rheological models, *Cem.*  
623 *Concr. Compos.* 59 (2015) 38–48.
- 624 [36] B. Il Choi, J.H. Kim, T.Y. Shin, Rheological model selection and a general model for  
625 evaluating the viscosity and microstructure of a highly-concentrated cement suspension, *Cem.*  
626 *Concr. Res.* 123 (2019) 105775.
- 627 [37] Y. Liu, C. Shi, Q. Yuan, X. An, L. Zhu, B. Wu, The rotation speed-torque transformation  
628 equation of the Robertson-Stiff model in wide gap coaxial cylinders rheometer and its applications  
629 for fresh concrete, *Cem. Concr. Compos.* 107 (2020) 103511.

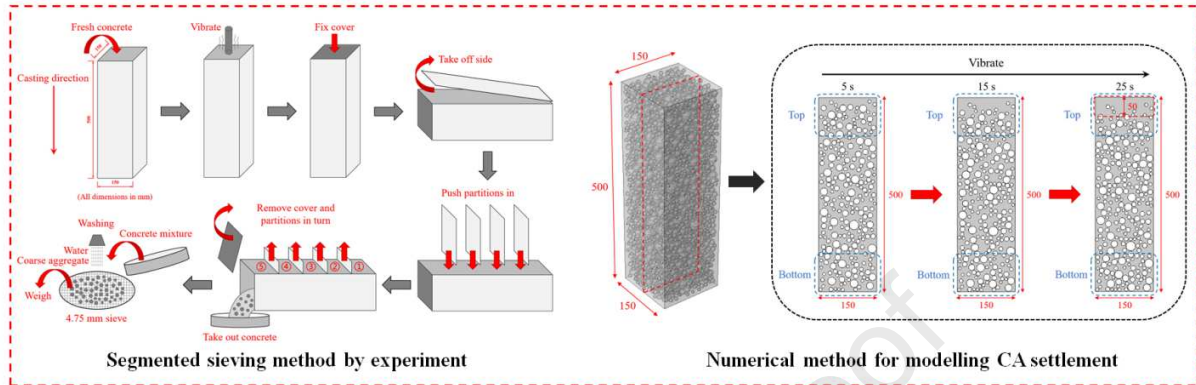
- 630 [38] M.I. Safawi, I. Iwaki, T. Miura, The segregation tendency in the vibration of high fluidity  
631 concrete, *Cem. Concr. Res.* 34 (2) (2004) 219–226.
- 632 [39] M.F. Petrou, B.L. Wan, F. Gadala-Maria, V.G. Kolli, K.A. Harries, Influence of mortar  
633 rheology on aggregate settlement, *ACI Mater. J.* 97 (4) (2000) 479–485.
- 634 [40] Y.A. Abebe, L. Lohaus, Rheological characterization of the structural breakdown process to  
635 analyze the stability of flowable mortars under vibration, *Constr. Build. Mater.* 131 (2017) 517–  
636 525.
- 637 [41] T.R. Muzenda, P. Hou, S. Kawashima, T. Sui, X. Cheng, The role of limestone and calcined  
638 clay on the rheological properties of LC3, *Cem. Concr. Compos.* 107 (2020) 103516.
- 639 [42] D. Kong, D.J. Corr, P. Hou, Y. Yang, S.P. Shah, Influence of colloidal silica sol on fresh  
640 properties of cement paste as compared to nano-silica powder with agglomerates in micron-scale,  
641 *Cem. Concr. Compos.* 63 (2015) 30–41.
- 642 [43] J.J. Assaad, Correlating thixotropy of self-consolidating concrete to stability, formwork  
643 pressure, and multilayer casting, *J. Mater. Civ. Eng.* 28 (10) (2016) 04016107.
- 644 [44] S. Zhuang, Q. Wang, Inhibition mechanisms of steel slag on the early-age hydration of  
645 cement, *Cem. Concr. Res.* 140 (2021) 106283.
- 646 [45] L.-X. Mao, Z. Hu, J. Xia, G.-L. Feng, I. Azim, J. Yang, Q.-F. Liu, Multi-phase modelling of  
647 electrochemical rehabilitation for ASR and chloride affected concrete composites, *Compos. Struct.*  
648 207 (2019) 176–189.
- 649 [46] Q.-F. Liu, M.F. Iqbal, J. Yang, X.-Y. Lu, P. Zhang, M. Rauf, Prediction of chloride  
650 diffusivity in concrete using artificial neural network: Modelling and performance evaluation,  
651 *Constr. Build. Mater.* 268 (2021) 121082.



- 652 [47] C.-L. Zhang, W.-K. Chen, S. Mu, B. Šavija, Q.-F. Liu, Numerical investigation of external  
653 sulfate attack and its effect on chloride binding and diffusion in concrete, *Constr. Build. Mater.*  
654 285 (2021) 122806.
- 655 [48] F. de Larrard, C. Hu, T. Sedran, J.C. Sztikar, M. Joly, F. Claux, F. Derkx, A new rheometer  
656 for soft-to-fluid fresh concrete, *ACI Mater. J.* 94 (3) (1997) 234–243.
- 657 [49] P.F.G. Banfill, Y. Xu, P.L.J. Domone, Relationship between the rheology of unvibrated fresh  
658 concrete and its flow under vibration in a vertical pipe apparatus, *Mag. Concr. Res.* 51 (3) (1999)  
659 181–190.
- 660 [50] Z. Li, G. Cao, Rheological behaviors and model of fresh concrete in vibrated state, *Cem.*  
661 *Concr. Res.* 120 (2019) 217–226.
- 662 [51] J.-Y. Petit, E. Wirquin, Y. Vanhove, K.H. Khayat, Yield stress and viscosity equations for  
663 mortars and self-consolidating concrete, *Cem. Concr. Res.* 37 (5) (2007) 655–670.
- 664 [52] A. Leemann, F. Winnefeld, The effect of viscosity modifying agents on mortar and concrete,  
665 *Cem. Concr. Compos.* 29 (5) (2007) 341–349.
- 666 [53] S. Diamond, J.D. Huang, The ITZ in concrete – a different view based on image analysis and  
667 SEM observations, *Cem. Concr. Compos.* 23 (2–3) (2001) 179–188.
- 668 [54] Q.-F. Liu, D. Easterbrook, J. Yang, L.-Y. Li, A three-phase, multi-component ionic transport  
669 model for simulation of chloride penetration in concrete, *Eng. Struct.* 86 (2015) 122–133.
- 670 [55] Q.-F. Liu, G.-L. Feng, J. Xia, J. Yang, L.-Y. Li, Ionic transport features in concrete  
671 composites containing various shaped aggregates: a numerical study, *Compos. Struct.* 183 (2018)  
672 371–380.

- 673 [56] W.A. Megid, K.H. Khayat, Effect of concrete rheological properties on quality of formed  
674 surfaces cast with self-consolidating concrete and superworkable concrete, *Cem. Concr. Compos.*  
675 93 (2018) 75–84.
- 676 [57] J.J. Assaad, J. Harb, Surface settlement of cementitious-based materials determined by  
677 oedometer testing, *Mater. Struct.* 44 (2011) 845–856.
- 678 [58] B.M. Aissoun, J.-L. Gallias, K.H. Khayat, Influence of formwork material on transport  
679 properties of self-consolidating concrete near formed surfaces, *Constr. Build. Mater.* 146 (2017)  
680 329–337.
- 681 [59] I. Navarrete, M. Lopez, Estimating the segregation of concrete based on mixture design and  
682 vibratory energy, *Constr. Build. Mater.* 122 (2016) 384–390.
- 683 [60] K.S. Chia, C.C. Kho, M.H. Zhang, Stability of fresh lightweight aggregate concrete under  
684 vibration, *ACI Mater. J.* 102 (5) (2005) 347–354.
- 685 [61] Y. Ke, A.L. Beaucour, S. Ortolà, H. Dumontet, R. Cabrillac, Influence of volume fraction and  
686 characteristics of lightweight aggregates on the mechanical properties of concrete, *Constr. Build.*  
687 *Mater.* 23 (2009) 2821–2828.
- 688 [62] L. Shen, H.B. Jovein, Q. Wang, Correlating aggregate properties and concrete rheology to  
689 dynamic segregation of self-consolidating concrete, *J. Mater. Civ. Eng.* 28 (1) (2016) 04015067.
- 690 [63] M.F. Iqbal, Q.-F. Liu, I. Azim, X. Zhu, J. Yang, M.F. Javed, M. Rauf, Prediction of  
691 mechanical properties of green concrete incorporating waste foundry sand based on gene  
692 expression programming, *J. Hazard. Mater.* 384 (2020) 121322.
- 693 [64] J.J. Assaad, Influence of recycled aggregates on dynamic/static stability of self-consolidating  
694 concrete, *J. Sustainable Cem.-Based Mater.* 6 (6) (2017) 345–365.

- 695 [65] W. Cui, W.-S. Yan, H.-F. Song, X.-L. Wu, DEM simulation of SCC flow in L-Box set-up:  
696 Influence of coarse aggregate shape on SCC flowability, *Cem. Concr. Compos.* 109 (2020)  
697 103558.
- 698 [66] M.F. Iqbal, M.F. Javed, M. Rauf, I. Azim, M. Ashraf, J. Yang, Q.-F. Liu, Sustainable  
699 utilization of foundry waste: Forecasting mechanical properties of foundry sand based concrete  
700 using multi-expression programming, *Sci. Total Environ.* 780 (2021) 146524.

**HIGHLIGHTS****Coarse aggregate settlement in fresh concrete under vibration**

- A rheological problem of cement-based materials has been studied both experimentally and numerically.
- The numerical method is developed for the first time to investigate the settlement behaviour of CAs in vibrated concrete.
- The validity of the model prediction is verified by the experimental results, based on the segmented sieving method.
- Grey relational analysis is performed to study the influence of related factors on the settlement of CAs.

**Declaration of interests**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:



Qing-feng LIU