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DOI 10.1021/acs.jpca.4c04923

Publication date 2024 **Document Version** Final published version

Published in Journal of Physical Chemistry A

Citation (APA)

Kramarenko, A. S., Sharapa, D. I., Pidko, E. A., & Studt, F. (2024). Ab Initio Kinetics of Electrochemical Reactions Using the Computational Fc0/Fc+ Electrode. Journal of Physical Chemistry A, 128(41), 9063-9070. https://doi.org/10.1021/acs.jpca.4c04923

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Article

Ab Initio Kinetics of Electrochemical Reactions Using the Computational Fc^{0}/Fc^{+} Electrode

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 Cite This: J. Phys. Chem. A 2024, 128, 9063–9070
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ABSTRACT: The current state-of-the-art electron-transfer modeling primarily focuses on the kinetics of charge transfer between an electroactive species and an inert electrode. Experimental studies have revealed that the existing Butler–Volmer model fails to satisfactorily replicate experimental voltammetry results for both solution-based and surface-bound redox couples. Consequently, experimentalists lack an accurate tool for predicting electron-transfer kinetics. In response to this challenge, we developed a density functional theory-based approach for accurately predicting current peak potentials by using the Marcus–Hush model. Through extensive cyclic voltammetry simulations, we conducted a thorough exploration that offers valuable insights for conducting well-informed studies in the field of electrochemistry.



INTRODUCTION

Electron transfer kinetics plays a pivotal role in oxidation and reduction reactions, which are essential phenomena across various scientific disciplines including biology, physics, and chemistry. In physical chemistry, discussion about these processes and their kinetics primarily focus on the energy barriers of the elementary reaction steps.^{1–9} In electrochemistry, these charge-transfer barriers, together with the diffusion of substrates and products to and from the electrode surface, determine the reaction kinetics and thus the form of the cyclic voltammogram, where the electric current is measured as a function of applied potential.¹⁰

The use of theoretical methods to calculate cyclic voltammograms is complicated by the fact that the barriers change as a function of the potential at the solid-liquid interface. Many studies have been devoted to simulate the full complexity of chemical transformations at the solid-liquid interface,^{1,9,11-14} with the solid being an electrocatalyst that binds intermediates and influences^{15–17} electrochemical reaction barriers.^{3,12,14,18–22} However, recent works show that the first solvation layer of the electrode surface is mainly occupied by solvent molecules and supporting electrolyte ions which hinder direct interaction of electrochemically active species to the electrode surface.²²⁻²⁶ Herein, we focus on identifying simple concepts to describe direct electron transfer from the electrode (cathode or anode) into the electrolyte (outer Helmholtz layer) without the explicit adsorption of intermediates on the electrode surface. We propose that this can be achieved by combining density functional theory (DFT) calculations with symmetric Marcus-Hush theory.²⁷⁻³⁰ This nonempirical strategy allows accurate

prediction of standard reduction potentials and voltammetric features such as peak potentials and peak current. The method is validated by computing reduction potentials and activation barriers of an extensive list of organic molecules (Figure S1), that have been discussed for a broad range of applications such as for energy storage, ^{31–34} dyes, ^{35–37} and photoresponsive membrane production.^{33,38–41}

METHODS

We start by investigating the performance of popular DFT methods in predicting the thermodynamics of electrochemical reactions. Structures of all chemical species employed in this study were fully relaxed using an unrestricted Kohn–Sham approach. We considered a representative selection of popular exchange–correlation functionals (BHANHLYP, B3LYP, BLYP, M06-2X, M06, M06-L, PBE, and PBE0) together with the ma-def2-TZVPP basis set as implemented in the ORCA (version 5.0.3) code.^{42–44} Our starting point is the redox couple ferrocene–ferrocenium (Fc⁰/Fc⁺) that is widely applied as a reference system in electrochemical reactions.^{4,45–64} Solvation effects of acetonitrile (MeCN), dimethylformamide (DMF), and acetone (ACE) have been taken into account by using the CPCM solvation model⁶⁵ implemented in ORCA. A detailed description of the

Received:July 22, 2024Revised:August 14, 2024Accepted:August 14, 2024Published:October 3, 2024





computational methodology is given in the Supporting Information (SI).

RESULTS AND DISCUSSION

We benchmark the various functionals for the (Fc^0/Fc^+) redox couple using the absolute electrode potential (AEP) of the reference electrode as described by eq 1.

$$AEP_{calc} = G_{red} - G_{ox}$$
(1)

where $G_{\rm red}$ is the Gibbs free energy of the corresponding ${\rm Fc}^0$ state and G_{ox} is the free energy of the Fc⁺ cation radical. As the Fc^0/Fc^+ system is a well-known reference due to its wide applicability in electrochemistry, there are plethora of experimental ionization potentials obtained by photoelectron and/or electron impact spectroscopy.^{4,59} In our current study, we rely on the experimental value of 6.71 ± 0.08 eV for its gasphase ionization energy reported by the National Institute of Standards and Technology (NIST).⁵⁹ The gas-phase ionization energies for all examined functionals are summarized in Figure S2 and elaborated upon in detail in the Supporting Information. Briefly, both the M06⁶⁶ and PBE^{67,68} functionals perform best, with values of 6.76 and 6.78 eV, respectively. The accuracy of the studied functionals is influenced by spin contamination, which negatively impacts the Hartree-Fock methods more significantly than the DFT methods. As a result, a higher Hartree-Fock exchange component within the functional leads to an increased incidence of spin contamination. It has been shown that the ferrocenium cation can be affected by this issue in both $DLPNO-CCSD(T)^{69}$ and double-hybrid calculations.⁷⁰

Experimentally, AEPs in solution are usually measured against reference electrodes and calculated according to

. .

$$AEP_{solv} = (E^{\circ} + E_{ref})nF$$
⁽²⁾

where AEP_{solv} denotes the AEP in a specific solvent, *F* is the Faraday constant, E_{ref} is the absolute potential of the reference electrode in a particular solvent, *n* denotes the number of electrons transferred during the process, and E^0 corresponds to the experimental standard reduction potential. The AEP_{solv} values for several most often used aprotic solvents are summarized in Table 1 and compared to our computational results using the PBE and M06 functionals (all other functionals have worse performance, see the Supporting Information).

Table 1. Comparison of Experimental and Computed AEPs in Solution (AEP_{solv}) of the Fc^0/Fc^+ System in MeCN, DMF, and ACE Solvents

solvent	AEP_{solv} [eV]		
	experiment	calculations	
		PBE	M06
MeCN	4.88 ^{,2,13} ,4.90 ^{,71} ,5.25 ⁵⁵	5.26	4.85
DMF	5.33, ^{64,72} 4.72 ^{73,74}	5.28	5.03
ACE	5.46 ^{,48,53} 4.74 ⁷⁵	5.61	6.90

As can be seen from Table 1, both functionals give reasonable results, especially considering that there is also large disagreement among the experimentally reported data.^{55,59,61} In this study, we are interested in the absolute potential of Fc^0/Fc^+ in an acetonitrile solution, where the average value of the experimentally obtained absolute

potentials is 5.01 eV with a mean absolute error (MAE) of 0.16 eV.

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We will use this computational Fc^0/Fc^+ electrode (CFE) to investigate the electroreduction of a test set of 13 different reactions (Figure 1). Figure 2 presents the results obtained

#	Reactions	E ⁰ [V vs. Fc ⁺ /Fc ⁰]
1	$())) - e \rightarrow ())$	0.84
2	$\bigcirc^{\stackrel{1}{C}} \bigcirc \cdot e^{-} \longrightarrow \bigcirc^{\stackrel{1}{C}} \bigcirc$	-2.34
3	$\operatorname{res}^{N_{n_{N}}} \to e^{-} \to \left[\operatorname{res}^{N_{n_{N}}} f^{(n_{N})}\right]^{-}$	-1.86
4	$e^{-} \rightarrow e^{-}$	-1.00
5	$_{0}$ \downarrow 0 \cdot e^{-} \rightarrow $_{0}$ \downarrow 0	-1.86
6	o ^{c™} ← e ⁻ → ^c o ^{c™} ←	-1.61
7	0=0 + e⁻ → 'o-o⁻	-1.28
8	$\sum_{n=1}^{N} (e^{-1} \rightarrow e^{-1} \rightarrow e^{-1}$	-0.33
9	$ \begin{array}{c} & & \\ & & $	-0.75
10	$(\mathbf{x}_{s}^{s})^{-} \mathbf{e}^{s} \rightarrow (\mathbf{x}_{s}^{s})^{-}$	0.77
11	$(\mathbf{y}_{\mathbf{x}_{\mathbf{y}}}^{s}) - \mathbf{e}^{*} \rightarrow (\mathbf{y}_{\mathbf{x}_{\mathbf{y}}}^{s})$	1.28
12	$\left\{ \sum_{s}^{2} + \sum_{s}^{2} \right\} - \mathbf{e} \rightarrow \left\{ \sum_{s}^{2} + \sum_{s}^{2} \right\}$	-0.16
13	$\begin{bmatrix} c_{1} \\ c_{2} \\ c_{3} \\ c_{4} \end{bmatrix} - e \rightarrow \begin{bmatrix} c_{1} \\ c_{4} \\ c_{4} \\ c_{4} \end{bmatrix}$	0.20

Figure 1. Reference reactions used for estimation of reduction potential prediction accuracy and its experimental standard reduction potentials were extracted from the published literature.

with the M06 functional, while the respective data obtained with the PBE and other DFT methods are summarized in the Supporting Information.

The error bars in Figure 2 represent the deviation of experimentally observed reduction potentials due to the error raised from the reference system. Figure 2 confirms the high accuracy of our computational Fc^0/Fc^+ electrode at the M06 level for the estimation of the reduction potentials of this test set with a mean absolute error of only 0.18 V. Note that this error is within the accuracy of typical DFT functionals (±0.20 eV). Note that the experiments also deviate in reported reduction potentials, with deviations between experiments being as large as 0.16 V. Having established that we are able to calculate SRPs and thus the thermodynamics of an electrochemical system using the CFE, we will now use this to evaluate electron-transfer kinetics in the framework of the Marcus–Hush model.^{27,28,76–81} According to Marcus–Hush theory, the activation energy (G_f^{\ddagger} and G_b^{\ddagger} for the forward and



Figure 2. Comparison of experimental and calculated reduction potentials of the test set of 13 reactions from Figure 1 using CFE with the M06 functional.

backward reactions, respectively) of an electron-transfer process can be calculated by

$$G_{\rm f}^{\ddagger} = \frac{\lambda}{4} + \alpha F(E - E^0) \tag{3}$$

$$G_{\rm b}^{\pm} = \frac{\lambda}{4} - (1 - \alpha)F(E - E^0)$$
 (4)

where λ is the reorganization energy⁸² and α is a potentialdependent symmetry factor. This parameter can be evaluated by the following equation

$$\alpha = \frac{1}{2} + \frac{F(E - E^0)}{4\lambda} \tag{5}$$

 λ consists of the inner (λ_i) and outer sphere (λ_o) reorganization energy and is

$$\lambda = \lambda_{\rm i} + \lambda_{\rm o} \tag{6}$$

In the given equation, λ_i represents the reorganization energy associated with alterations in bond lengths and angles between atoms during the electron-transfer process, which can rather be simply obtained from DFT calculations. For the forward reaction barrier (G_f^{\ddagger}) , this is done by calculating the differences of free energy of the reduced state with the equilibrium geometry of the oxidized (Q_{ox}) and reduced states (Q_{red}) . In the case of Fc⁰/Fc⁺ system $G_{red}(Q_{ox})$ equals to free energy of ferrocene in optimized ferrocenium geometry and $G_{red}(Q_{red})$ is the free energy of ferrocene with relaxed ferrocene geometry.

$$\lambda_{\rm i} = G_{\rm red}(Q_{\rm ox}) - G_{\rm red}(Q_{\rm red}) \tag{7}$$

 λ_{o} can be calculated from

$$\lambda_{\rm o} = \frac{e^2}{8\pi\varepsilon_0} \left(\frac{1}{a_{\rm o}} - \frac{1}{R} \right) \left(\frac{1}{\varepsilon_{\rm op}} - \frac{1}{\varepsilon_{\rm s}} \right) \tag{8}$$

where *e* is the elementary charge, ε_0 is the vacuum dielectric permittivity, while a_0 signifies the radius of a sphere of the corresponding molecule the volume of which is equivalent to the cavity volume in the solvation model, ε_{op} and ε_s are optical and static dielectric permittivity, *R* is a distance of the molecule from the electrode surface and usually equals to $2a_0$.

Applying this for our case of the Fc^0/Fc^+ system, λ is equal to 0.30 eV, with λ_i being calculated to 0.02 eV by DFT and λ_o being 0.28 eV. We computed the activation energy for both the forward and backward reactions of the Fc^0/Fc^+ redox couple using eqs 3 and 4, and the result is depicted in Figure 3.



Figure 3. Dependence of the activation energy (dots) and rate constants (squares) for the Fc^0/Fc^+ oxidation process on the applied potential. The white circles at 0 V correspond to the respective values at the standard reduction potential.

Having derived the expression for the activation energies for electron transfer as a function of applied potential, one can now compute the potential-dependent rate constants for the forward and backward reactions

$$k_{\rm f} = k^0 {\rm e}^{-\alpha F(E-E^0)/RT}$$
(9)

$$k_{\rm b} = k^0 {\rm e}^{(1-\alpha)F(E-E^0)/RT}$$
(10)

where k^0 is the standard rate constant, which is dependent on the total reorganization energy λ . This parameter can be calculated from the following equation

$$k^{0} = Z e^{-\lambda F/4RT}$$
(11)

$$Z = \sqrt{\frac{RT}{2\pi M}}$$
(12)

where Z is the collision frequency with the electrode surface which depends on the molar mass (M) of the molecule.

The reaction rate also depends crucially on the concentration of the molecules in the volume above the electrode surface. The concentration is dependent on the conversion and diffusion of molecules during electroreduction and oxidation. The reaction rate (and thus the current density) is thus given by eqs 13 and 14

$$\frac{\mathrm{d}C_{\mathrm{i}}}{\mathrm{d}t} = D_{\mathrm{i}}\frac{\mathrm{d}^{2}C_{\mathrm{i}}}{\mathrm{d}t^{2}} \tag{13}$$

$$-J_{\rm ox} = J_{\rm red} = k_{\rm f}C_{\rm A} - k_{\rm b}C_{\rm B}$$
⁽¹⁴⁾

where $k_{\rm f}$ and $k_{\rm b}$ are rate constants computed by the Marcus– Hush model, $C_{\rm A}$ and $C_{\rm B}$ represent the concentration of Fc⁰ and Fc⁺, respectively, and $D_{\rm i}$ is the diffusion constant of a solute.

Final current density can be calculated from eq 15

$$\frac{l_{\rm tot}}{A} = -nFJ_{\rm ox} \tag{15}$$

where *n* is the number of transferred electrons, *F* is Faraday's constant, *A* is the surface area of the electrode, and i_{tot} is the

reaction current; eqs 13–15 were computed numerically using the finite difference method.^{77,84,85} A detailed procedure of cyclic voltammetry (CV) simulation was described by Brown.⁸⁶ Python code used for CV curve production can be found on KITopen.

We computed the diffusion constant (D_i) using the Einstein–Stokes equation

$$D_{i} = \frac{k_{b}T}{6\pi\eta a_{i}}$$
(16)

where k_b is the Boltzmann constant and η is the solvent viscosity. The viscosity of acetonitrile at 298.15 K equals to 0.38 mPa·s.⁶⁰ Thus, the calculated diffusion coefficients are 0.954 × 10⁻⁵ and 0.951 × 10⁻⁵ cm²/s for Fc⁰ and Fc⁺, respectively. This fits well with experimentally obtained values of 2.00 × 10⁻⁵ and 1.60 × 10⁻⁵ cm²/s for Fc⁰ and Fc⁺, respectively.⁴⁶

Using eqs 13 and 14, we simulated the CV curves of Fc^0/Fc^+ . The simulated and experimental⁸³ CV curves are compared in Figure 4. Concentrations of all components of



Figure 4. Experimental and simulated CV curves of 5 mM ferrocene oxidation at a 0.01 V/s scan rate. Solid line represents the simulated CV curve and dashed line represents the experimental CV curve. The provided values represent simulated/experimental peak potentials and standard reduction potentials. The experimental CV curve is adapted from ref 83. Available under a CC-BY 3.0 license. Copyright 2024 K. Lehmann, O. Yurchenko and G. Urban.

the reaction medium in the simulations were set to reproduce the experimental conditions. In the simulation of ferrocene behavior, where reduction potential were established at 0 V vs Fc^0/Fc^+ , the positions of peak potentials exhibit slight variations compared to the experimental results with the peak potential difference being 0.06 V for our simulation and 0.08 V for experimental results.⁸³ We can thus nicely simulate the CV curves of our computational Fc^0/Fc^+ electrode using exclusive input from DFT calculations as well as the tabulated viscosity of acetonitrile as the input.

We now turn to simulate the CV curves of the 13 test reactions depicted in Figure 1. We do this in the same manner and use our computational Fc^0/Fc^+ electrode as the reference electrode, as was done in Figure 2 (the solvent being acetonitrile in all cases). The results are shown in Figure 5 for a selected set of reactions (see the Supporting Information for the CV curves of all 13 reactions).

Experimental CV curves from Figure 5 were adapted from published experiments.^{39,54} In all cases shown in Figure 5,





Figure 5. Experimental and simulated CV curves of nitrobenzene, benzoquinone reduction, and anthracene oxidation with 0.1, 0.1, and 0.1 V/s scan rate, respectively. Solid line represents the simulated CV curve and dashed line represents the experimental CV curves (see text). Experimental CV curves for nitrobenzene adapted with permission from ref 39. Copyright 2024 Royal Society of Chemistry. Experimental CV curves for benzoquinone and anthracene are adapted with permission from refs 38 and 41. Copyright 2024 Elsevier.

deviation from experimentally observed reaction behavior can be explained by the difference in experimental^{39,77,87,88} and predicted reduction potentials. However, experimental anthracene oxidation does not show a cathodic peak from cation radical deactivation which was observed for anthracene derivatives on the Pt electrode.⁸⁹ It might be related to the chemical step, which was not considered in the current study. This process was shown to be a fast step,⁹⁰ hence the reversed process of An⁺ reduction is hindered due to lack of cation radicals.⁹¹

Furthermore, by comparing the experimental peak potentials to the simulated values, we can evaluate the reproduction of kinetic parameters. We also stress here that the discrepancies are mostly due to errors originating from inaccuracies of the DFT functional, as an error of, e.g., 0.2 eV translates directly to a deviation of 0.2 V in the simulated CV.

Figure 6 illustrates a comparison between the experimental and simulated peak potentials for investigated test reactions in which experimental CVs have been found. The analysis indicates that the predicted peak potentials align well with the experimental results, within the typical error introduced by DFT. The mean average deviation for the model was estimated to be 0.33 V vs Fc^0/Fc^+ . Significant deviations from experimental results were primarily observed, when computational errors in reduction potentials existed.



Figure 6. Representation of accuracy for peak potential prediction by the Marcus–Hush model. E_a^{p} and E_c^{p} are anodic and cathodic peak potentials, respectively. Numbers denote the reaction indexes in Figure 1.

CONCLUSIONS

In conclusion, our study explores the development of a straightforward ab initio model for predicting electrochemical kinetics and constructing CV curves of the 13 reference reactions and the ferrocene/ferrocenium system in particular. Moving beyond potential energies, our investigation extended to the electrode reaction kinetics. Utilizing the Marcus–Hush model, we obtained activation energies for reference reactions, shedding light on the electron-transfer process. The M06 functional stood out as providing the most accurate predictions for reduction potentials and facilitating precise calculations of activation energies. Furthermore, our computational approach can be broadened to account for the electrode electronic structure^{81,92,93} with advanced models of reorganization energy calculation^{78,79,82,94,95} to study electron transfer on various materials.

Furthermore, the study employed CV simulations to gain insights into the electrochemical behavior. We introduce here the computational Fc^0/Fc^+ electrode as a convenient reference electrode in computational studies and suggest that this can be universally employed as a reference for electron-transfer processes analogous to the computational hydrogen electrode that has been shown to work well for coupled proton-/ electron-transfer processes. The model, validated against experimental data, showcased its utility in predicting peak potentials and current density responses. While deviations were observed, particularly in reduction potentials impacting peak potentials, the model provided a qualitative representation of the electrochemical processes.

ASSOCIATED CONTENT

Data Availability Statement

Python code for CV simulations can be found via https://doi. org/10.35097/VKVYEoWBRxzhwiPh.

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.jpca.4c04923.

Optimized structures of all molecules utilized in this study, experimental and computed reduction potentials, and all data points utilized for constructing figures (PDF)

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Author Contributions

The manuscript was written through contributions of all authors. All authors have given approval to the final version of the manuscript.

Notes

The authors declare no competing financial interest.

ACKNOWLEDGMENTS

The authors acknowledge support by the state of Baden-Württemberg through bwHPC and the German Research Foundation (DFG) through grant no. INST 40/575-1 FUGG (JUSTUS 2 Cluster). Financial support from the Helmholtz Association is also gratefully acknowledged. A.S.K. thanks German Academic Exchange Service (DAAD) for the financial support of this work.

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