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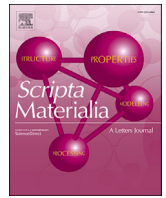
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Stresses at grain boundaries: The maximum incompatibility stress in an infinitely extended elastic bicrystal under uniaxial loading

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ABSTRACT

In a material under stress, grain boundaries may give rise to stress discontinuities. Stress localization is crucial to materials' behavior such as segregation, precipitation, and void nucleation. Here, the stress state at a grain boundary perpendicular to a uniaxial external stress is studied systematically. The grain boundary with the most extreme stress discontinuity is determined for cubic materials within the elastic limit for a bicrystal model. Additionally, grain boundaries with negligible stress discontinuity are identified. The influence of the elastic tensor components, C_{11} , C_{12} , and C_{44} , and grain orientation is studied quantitatively.

Grain boundaries (GBs) act as walls that divide the bulk into parts with different orientations and discontinuous tensorial properties. Under loading, the misorientation of grains and the intrinsic anisotropy of the crystal lead to a stress discontinuity at the GBs, resulting in stress states that deviate significantly from the average. The stress discontinuity at GBs strongly influences some phenomena at the grain scale, such as grain growth [1,2] and segregation [3]. Moreover, since the failure of materials is controlled by extreme values of localized stresses rather than by the average stress level in the material, the stress discontinuity at certain GBs strongly affects materials' mechanical behavior, such as crack initiation under loading [4], fatigue [5–7], corrosion cracking [8], and creep [9–11]. Grain boundary engineering [12] and new manufacturing methods show great promise for optimizing material performance through control of texture [13,14] and GB structure [15]. Therefore, investigating how stress states at GBs are influenced by grain orientations can help design polycrystalline materials with optimized textures [16].

Theoretically, already three decades ago, certain special GBs, such as the tilt symmetrical GB and twist GB [17–19], were studied and analytical solutions for those particular incompatibility stresses (IS) were derived. A few years ago, for bicrystals, an explicit closed-form solution for IS for general GBs was derived and verified through finite element method (FEM) simulations [20]. This solution was then applied to study

the stress state at $\Sigma 3(1\ 1\ 1)$ twin boundaries [21] and the activation of dislocations in nickel bicrystalline micropillars [22]. It was revealed that IS plays a crucial role in activating slip, which directly affects the plastic deformation of metals. For polycrystals, FEM simulations and statistical analysis have shown that the inclination angle of grain boundaries, grain size, and triple junctions have a significant influence on IS [23–26].

In addition to IS at GBs, there are several theoretical studies on the interaction of dislocations with GBs. The elastic field induced by dislocations [36] and the dislocation pile-ups behavior [35,36] near GBs in anisotropic materials are strongly affected by the orientations of the grains.

Previous works either focus on special cases, which are not guaranteed to find the stress build-up extrema [17–19], or focus on polycrystals, which yield many details but do not easily reveal general rules about specific GBs [23–26].

This work starts from a bicrystal model with an external stress σ^E perpendicular to the GB, aiming to identify the extrema of the IS and to gain insight into the stress state. We derive an analytical solution for the extreme value of the IS at the GB in terms of the elastic tensor components. It is revealed that the GB with the highest IS is the same for all cubic materials. Furthermore, the magnitude of IS for general GBs under perpendicular uniaxial applied stress is quantitatively described.

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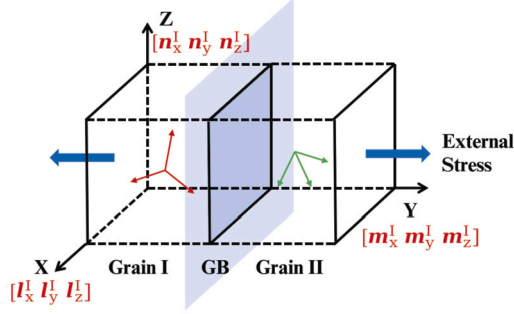


Fig. 1. (Color online) The schematic figure of the bicrystal model in this work. The size of the GB in the X and Z direction is infinite. The two grains are semi-infinite. The orientation of each grain is represented by three Miller indices. The blue arrows show the uniaxial external stress σ^E applied far from the GB, which is perpendicular to GB plane. The label of the grain is shown at the superscript.

The bicrystal model applied in this study is shown in Fig. 1. The 3-dimensional space is divided into two semi-infinite half-spaces separated by the GB. In keeping consistency with previous work [21], the GB plane is fixed parallel to the global XOZ plane, and the direction of σ^E is set along the global Y-axis, perpendicular to the GB. We firstly focus on the stress state near GBs that are perpendicular to σ^E . Experiments [27] and simulations [25] suggest that GBs perpendicular to σ^E are more likely to be the initial site of failure.

Two grains with the same material property but with different orientations are labeled as grain I and grain II. For cubic materials, the orientations of crystals can be conveniently described with Miller indices. For grain I,

$$\hat{e}^I = \begin{bmatrix} l_x^I & l_y^I & l_z^I \\ m_x^I & m_y^I & m_z^I \\ n_x^I & n_y^I & n_z^I \end{bmatrix}, \quad (1)$$

where l^I , m^I , n^I are normalized Miller indices of the crystallographic orientation of grain I corresponding to X, Y, and Z-axis in global coordinate system, respectively. Then the orientation of grain I is uniquely represented with $[l_x^I \ l_y^I \ l_z^I]$ and $[m_x^I \ m_y^I \ m_z^I]$, and analogously for grain II.

The compliance tensor S' after rotation \hat{e} , is given by

$$S'_{mnop} = \hat{e}_{mi} \hat{e}_{nj} \hat{e}_{ok} \hat{e}_{pl} S_{ijkl}, \quad (2)$$

in which S is the compliance tensor in the cubic crystal coordinate system.

Within the continuum description of GBs the following constraints apply for the bicrystal model.

1. The two grains are rigidly glued together at the GB. No relative motion is allowed at the GB.
2. The model contains only one GB with infinite size. The interaction between GBs is not included.
3. The model is valid within the linear elastic limit.
4. σ^E is along global Y-axis, which is perpendicular to the GB plane.

Considering the equilibrium equations for momentum, the stress field in the bicrystal model must be invariant with respect to the Y coordinate. The discontinuity of a scalar field $g(x_i)$ at the GB is represented as $[g] = g^I - g^{II}$ then IS can be presented as $[\sigma_{ij}]$.

The constitutive equation of a linear elastic material is

$$\epsilon_{ij} = S_{ijkl} \sigma_{kl}. \quad (3)$$

According to the first constraint listed above, strain components in the GB plane are continuous,

$$[\epsilon_{ij}] = 0, \quad i, j = 1, 3. \quad (4)$$

Since σ^E is a far-field stress, global stress equilibrium requires

$$\frac{1}{V} \int_V \sigma_{ij} dV = \Sigma_{ij}, \quad (5)$$

where Σ_{ij} is the general external stress [20]. In this problem Σ_{ij} only contains σ^E . So

$$\begin{cases} \sigma_{22}^I = \sigma_{22}^{II} = \sigma^E \\ \sigma_{23}^I = \sigma_{23}^{II} = 0 \\ \sigma_{12}^I = \sigma_{12}^{II} = 0 \end{cases}. \quad (6)$$

Since the model assumes that each grain occupies half the space, Eq. (5) is equivalent to

$$\Sigma_{ij} = \frac{1}{2} (\sigma_{ij}^I + \sigma_{ij}^{II}). \quad (7)$$

Then for in-plane stress components can be written as

$$\sigma_{ij}^I + \sigma_{ij}^{II} = 0, \quad i, j = 1, 3. \quad (8)$$

According to Eq. (6), the stress states at both sides of the GB are

$$\begin{cases} \sigma^I = [\sigma_1, \sigma^E, \sigma_3, 0, \sigma_5, 0] \\ \sigma^{II} = [-\sigma_1, \sigma^E, -\sigma_3, 0, -\sigma_5, 0], \end{cases} \quad (9)$$

with Voigt notation ($xx \rightarrow 1, yy \rightarrow 2, zz \rightarrow 3, yz \rightarrow 4, xz \rightarrow 5, xy \rightarrow 6$). Noticing σ_4 and σ_6 are zero, the global Y-axis is one of the principal directions for the stress state. When the global coordinate system is rotated around its Y-axis, the in-plane stress components can be represented by a Mohr circle. Then $(\sigma_1 + \sigma_3)$ is an invariant for $[\sigma_{ij}]$ during the rotation.

Consider the discontinuity of hydrostatic stress σ_h at the GB,

$$[\sigma_h] = \frac{2(\sigma_1 + \sigma_3)}{3}. \quad (10)$$

As our description is in the linear elastic limit, all stresses are proportional to σ^E . Therefore it is convenient to define an incompatibility factor (IF) as

$$IF = \frac{\sigma_1 + \sigma_3}{\sigma^E}. \quad (11)$$

When exchanging the labeling of the two grains, IF changes sign, so that only the absolute value of IF has physical meaning. Then σ_h at either side of GB can be expressed as

$$\sigma_h = \frac{(1 \pm IF)\sigma^E}{3} \quad (12)$$

In Supplement A a Python module is provided for computing IF analytically.

Hayes and Shuvalov proposed a parameter χ to characterize the Young's modulus anisotropy of cubic crystals [28],

$$\chi = 2s_{11} - 2s_{12} - s_{44}. \quad (13)$$

Here s_{ij} refers to compliance components written with Voigt notation and with the engineering convention ($s_{44} = 4s_{yzyz} = 4s_{xyxy} = 4s_{xzzz}$). Here we derive a property of 4^{th} rank tensors of cubic crystals using Voigt notation, with special application to the compliance matrix. The compliance matrix after rotation is given as (see Supplement B for details)

$$S' = S + \chi F(l, m, n), \quad (14)$$

where F is a 6 by 6 symmetric matrix of polynomials of l, m, n components, e.g.

$$F_{22} = -(m_x^2 m_y^2 + m_x^2 m_z^2 + m_y^2 m_z^2), \quad (15)$$

$$F_{25} = m_x^2 l_x n_x + m_y^2 l_y n_y + m_z^2 l_z n_z, \quad (16)$$

$$F_{55} = -4(n_x n_y l_x l_y + n_x n_z l_x l_z + n_y n_z l_y l_z). \quad (17)$$

Since F doesn't contain any elastic tensor components, it is common for all cubic materials.

For two grains with compliance tensor S^I and S^{II} it is convenient to properly rotate the coordinate system along Y axis to make $\sigma_1 = \sigma_3$. According to Eq. (3), (9), and (14), the strain continuity equation (Eq. (4)) can be recast as

$$\begin{cases} [(F_{11}^I + F_{11}^{II})\chi + 2s_{11} + (F_{13}^I + F_{13}^{II})\chi + 2s_{12}]\sigma_1 + (F_{12}^I - F_{12}^{II})\chi\sigma^E + (F_{15}^I + F_{15}^{II})\chi\sigma_5 = 0, \\ [(F_{33}^I + F_{33}^{II})\chi + 2s_{11} + (F_{31}^I + F_{31}^{II})\chi + 2s_{12}]\sigma_1 + (F_{32}^I - F_{32}^{II})\chi\sigma^E + (F_{35}^I + F_{35}^{II})\chi\sigma_5 = 0, \\ (F_{51}^I + F_{51}^{II} + F_{53}^I + F_{53}^{II})\chi\sigma_1 + (F_{52}^I - F_{52}^{II})\chi\sigma^E + [(F_{55}^I + F_{55}^{II})\chi + 2s_{44}]\sigma_5 = 0. \end{cases} \quad (18)$$

Then considering the orthonormality of l , m , and n of \hat{e} , the expression for σ_1 is simplified as

$$\frac{\sigma_1}{\sigma^E} = \frac{(F_{22}^I - F_{22}^{II})[(F_{55}^I + F_{55}^{II})\chi + 2s_{44}]\chi - [(F_{25}^I)^2 - (F_{25}^{II})^2]\chi^2}{[(F_{22}^I + F_{22}^{II})\chi + 4s_{11} + 4s_{12}][(F_{55}^I + F_{55}^{II})\chi + 2s_{44}] - (F_{25}^I + F_{25}^{II})^2\chi^2}. \quad (19)$$

Considering a global coordinate system rotated around Y-axis such that $\sigma_1 = \sigma_3$, it follows that

$$IF = \frac{2\sigma_1}{\sigma^E}. \quad (20)$$

Then, Eq. (19) shows the orientation dependence of σ_1 as well as of IF . Referring to Eq. (15), (16), and (17), for each grain, we can consider F_{22} as reflecting the effects of two degrees of freedom of the grain rotation, while F_{25} contains the remaining 1 degree of freedom, which represents the rotation of the grain around the Y-axis. Considering the connection between Young's modulus of the grain along the global Y-axis and compliance components, as

$$E_Y = \frac{1}{S'_{22}} = \frac{1}{F_{22}\chi + s_{11}}, \quad (21)$$

terms with F_{22} show the influence of the stiffness of the grain along the global Y-axis. Eq. (19) fits well with our intuition about the IS . Intuitively, one might link the IS to the difference of transverse strain (induced by the Poisson effect) across the GB. A grain with a low (high) Young's modulus along the loading direction has a large (small) positive longitudinal elastic strain, which leads to a large (small) negative transverse strain in the GB plane. Thus the IF is related to the discontinuity of the Young's modulus along the Y-axis.

According to Eq. (15), the range of F_{22} is estimated as

$$F_{22} = -(m_x^2 m_y^2 + m_x^2 m_z^2 + m_y^2 m_z^2) = \frac{m_x^4 + m_y^4 + m_z^4 - 1}{2}. \quad (22)$$

The maximum (minimum) of F_{22} is 0 ($-\frac{1}{3}$) when m is along $\langle 1 \ 0 \ 0 \rangle$ ($\langle 1 \ 1 \ 1 \rangle$). For F_{55} , Eq. (17) can be written as

$$F_{55} = -4(n_x n_y l_x l_y + n_x n_z l_x l_z + n_y n_z l_y l_z) = 2(l_x^2 n_x^2 + l_y^2 n_y^2 + l_z^2 n_z^2). \quad (23)$$

The maximum (minimum) of F_{55} is 1 (0) when l , n are along $\langle 1 \ 1 \ 0 \rangle$ and $\langle -1 \ 1 \ 0 \rangle$ ($\langle 1 \ 0 \ 0 \rangle$ and $\langle 0 \ 1 \ 1 \rangle$), l and n can be exchanged.

The value of F_{25} is found numerically, which gives a maximum of $\frac{1}{4}$ when l , m are along $\langle 1 \ -1 \ \sqrt{2} \rangle$ and $\langle 1 \ 1 \ 0 \rangle$ (in arbitrary order), respectively. When exchanging the sequence of l and n , F_{25} changes its sign. F_{25} approaches 0 when F_{22} approaches its extrema.

It's difficult to derive the extreme value of σ_1/σ^E mathematically since Eq. (19) contains both rotation variables and material elastic components. The following two points are considered to search for the maximum σ_1/σ^E .

1. F_{25} is much less than 1, and it appears quadratically only. This shows that the influence of the rotation of the grain around the Y-axis is relatively small.
2. When F_{22} approaches its extremum, i.e. $F_{22} = 0$ and $F_{22} = -\frac{1}{3}$, terms with F_{25} vanish.

Then the expression of σ_1/σ^E simplifies to

$$\begin{aligned} \frac{\sigma_1}{\sigma^E} &\approx \frac{(F_{22}^I - F_{22}^{II})[(F_{55}^I + F_{55}^{II})\chi + 2s_{44}]\chi}{[(F_{22}^I + F_{22}^{II})\chi + 4s_{11} + 4s_{12}][(F_{55}^I + F_{55}^{II})\chi + 2s_{44}]} \\ &= \frac{(F_{22}^I - F_{22}^{II})\chi}{[(F_{22}^I + F_{22}^{II})\chi + 4s_{11} + 4s_{12}]}. \end{aligned} \quad (24)$$

For $\chi > 0$ ($\chi < 0$), the maximum (minimum) for Eq. (24) is achieved when $F_{22}^I = 0$ and $F_{22}^{II} = -\frac{1}{3}$, which corresponds to m^I and m^{II} parallel to $\langle 1 \ 0 \ 0 \rangle$ and $\langle 1 \ 1 \ 1 \rangle$, respectively. With Eq. (11) and (24), and $\sigma_1 = \sigma_3$, the maximum value of IF is

$$\begin{aligned} IF^{\max} &= \frac{2\chi/3}{-\chi/3 + 4s_{11} + 4s_{12}} \\ &= \frac{4s_{11} - 4s_{12} - 2s_{44}}{10s_{11} + 14s_{12} + s_{44}} \\ &= \frac{-2(C_{11} - C_{12} - 2C_{44})(C_{11} + 2C_{12})}{(10C_{11} - 4C_{12})C_{44} + (C_{11} - C_{12})(C_{11} + 2C_{12})}. \end{aligned} \quad (25)$$

After conducting large-scale sampling of IF for the bicrystal model with various grain orientations, it is confirmed that Eq. (25) represents the global maximum of IF .

We found the magnitude of IF is related to the elastic instability of cubic crystals. The elastic stability conditions for cubic crystals are

$$C_{11} - C_{12} > 0, \quad C_{11} + 2C_{12} > 0, \quad C_{44} > 0, \quad (26)$$

or, equivalently

$$-\frac{1}{2} < \frac{C_{12}}{C_{11}} < 1, \quad \frac{C_{44}}{C_{11}} > 0. \quad (27)$$

The IF^{\max} values, as computed with Eq. (25), for common metals are shown in Fig. 2(a) using the experimentally determined elastic tensor components [29]. When C_{12}/C_{11} approaches 1, or C_{44}/C_{11} approaches 0, which means the stability of the crystal is low according to Eq. (27), the absolute value of IF^{\max} rises rapidly.

In alloys the IF^{\max} can be designed on purpose. The types and concentrations of alloying elements can influence the elastic properties of alloys as has been shown experimentally and computationally [30,31]. By designing alloys with low IF^{\max} using Fig. 2(a), it might be possible to improve properties that are sensitive to the stress state at GBs.

At the GB, not only the discontinuities in stresses are of interest, but large values of local stresses themselves are of importance too. Therefore, the σ_h values on both sides of the GB corresponding to IF^{\max} are calculated. The stress concentration factor F_h is defined as the ratio of the σ_h values on both sides of the GB to the value of the hydrostatic stress without a GB under σ^E ,

$$F_h = \frac{3\sigma_h}{\sigma^E} = 1 \pm IF. \quad (28)$$

The most extreme F_h for common metals are shown in Fig. 2(b). For common engineering metal bicrystals under a uniaxial σ^E perpendicular to the GB, the variation of σ_h at a GB is 14% for aluminum, 54% for iron and nickel, and 78% for copper, when compared to an isotropic material. In alkali metals, F_h can take a negative value, indicating that dilatation in bulk can give rise to compression on one side of the GB and large tension on the other side. As both σ_h and its gradient [33] play significant roles in the segregation and diffusivity [32] of interstitial atomic species and poorly fitting substitutional atomic species, precipitation processes can be affected particularly in materials with large variations in F_h values.

Based on Eq. (21) and (24), IF is further simplified as

$$\begin{aligned} IF &\approx \frac{1/E_Y^I - 1/E_Y^{II}}{(F_{22}^I + F_{22}^{II})\chi + 4s_{11} + 4s_{12}} \\ &\approx \frac{6(1/E_Y^I - 1/E_Y^{II})}{10s_{11} + 14s_{12} + s_{44}}, \end{aligned} \quad (29)$$

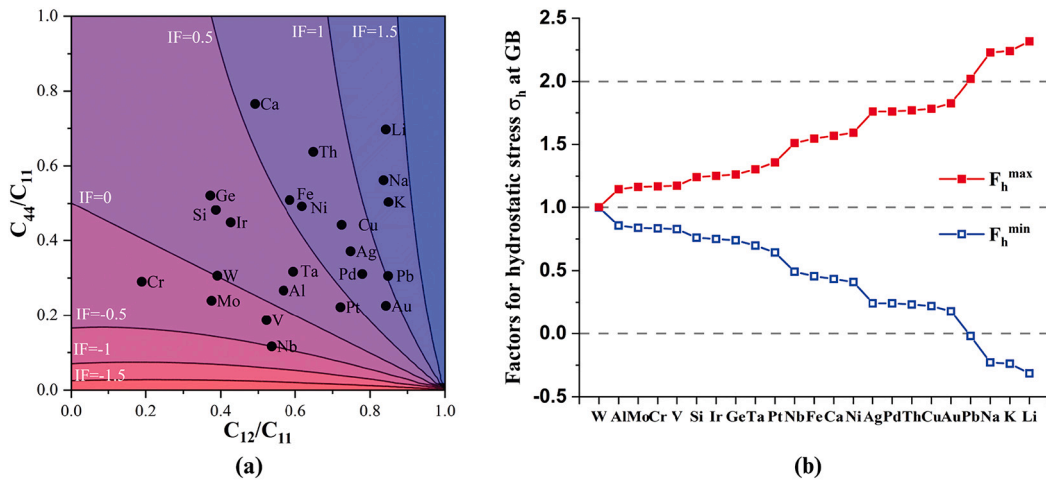


Fig. 2. (Color online) (a) The relation between elastic components and incompatibility factor, according to Eq. (25). The positions of common metals are labeled with black solid circles. (b) The maximum and minimum stress concentration factor F_h for hydrostatic stress σ_h at GBs for common metals, according to Eq. (28).

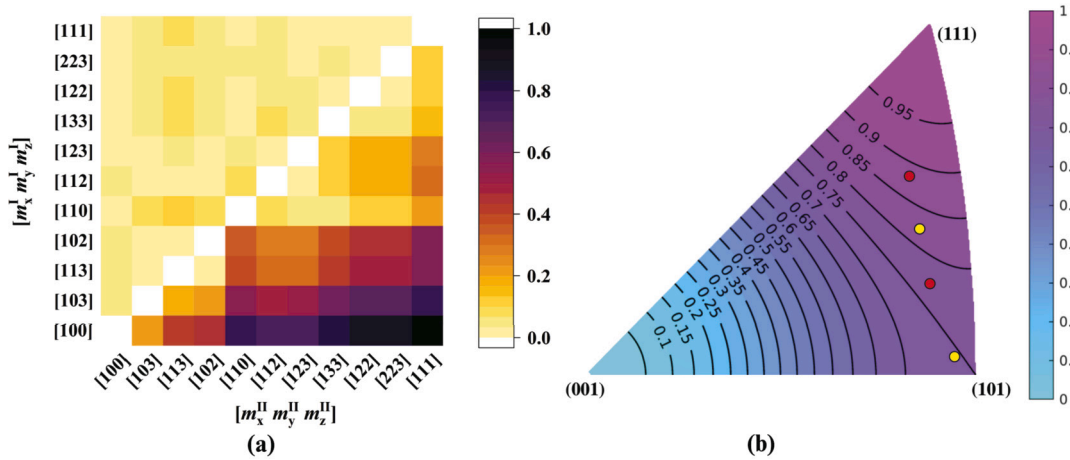


Fig. 3. (Color online) (a) For low-index GBs, IF^{GB} estimated by Eq. (32) are shown below the diagonal, while above the diagonal the maximum absolute value of IF^{GB} (exact) - IF^{GB} (Eq. (32)) that occurs when one of the two grains is rotated around the Y-axis is displayed. (b) Compliance factor as function of the grain orientation according to Eq. (31). The orientations of two bicrystals in [34] are presented by red dots for one bicrystal and yellow dots for another bicrystal.

where E_Y^I (E_Y^{II}) is the Young's modulus of grain I (II) along the global Y-axis. Here $(F_{22}^I + F_{22}^{II})\chi$ in the denominator is replaced by $-\frac{1}{3}\chi$ to ensure the accuracy of the approximation in predicting high absolute values of IF .

Eq. (29) disregards the stress variations arising from rotating the two grains around the direction of σ^E for two reasons. Firstly, IF , being defined as sum of σ_1/σ^E and σ_3/σ^E , is less sensitive to variations of individual stress components. Secondly, the bicrystal structure displays at least a four-fold symmetry during the rotation around global Y-axis. This equation is in good agreement with the analytical results (see Supplement C). Hence, while m^I and m^{II} have a strong influence on IF , the other four Miller indices have little effect. Therefore, the GB in the bicrystal model can be characterized by m^I and m^{II} .

In order to clarify the role of the orientations of the two grains, we define a rescaled incompatibility factor for GBs

$$IF^{GB} = IF/IF^{max}, \quad (30)$$

ranging from -1 to 1, which is independent of the elastic anisotropy. The IF^{GB} for low-index GBs are shown in Fig. 3(a).

For general GBs, it is convenient to define the compliance factor (CF) to separate the contributions to IF^{GB} from each grain. For grain I,

$$\begin{aligned} CF^I &= \frac{1/E^{min} - 1/E_Y^I}{1/E^{min} - 1/E^{max}} \\ &= -3F_{22}^I \\ &= 3 \left((m_x^I m_y^I)^2 + (m_x^I m_z^I)^2 + (m_y^I m_z^I)^2 \right), \end{aligned} \quad (31)$$

where E^{min} , E^{max} are the minimum and maximum Young's modulus for the material, and analogous for grain II. Then IF^{GB} is expressed as

$$IF^{GB} = CF^{II} - CF^I. \quad (32)$$

Fig. 3(b) shows a contour plot of CF as function of m of each grain in a (0 0 1) inverse pole figure. This figure displays two important features.

First, the geometry of each GB can be presented as two points, corresponding to grain I and grain II, in Fig. 3(b). Then the rescaled IF for a given GB can be read from the map according to Eq. (32), e.g. the maximum of IF^{GB} , at 1, corresponds to m^I , m^{II} parallel to [1 0 0] and [1 1 1], respectively.

Second, the IF for GBs with large misorientation is not always large. The IF vanishes for two grains with orientations located along a contour line. Therefore, even for materials with high anisotropy, it is possible to design textures with near-zero stress incompatibility at GBs.

Considering the proportional relationship between IF and $[\sigma_h]$ shown in Eq. (21), Fig. 3 is also valid for estimating the magnitude of $[\sigma_h]$ for various GBs.

In recent in-situ tensile tests of bicrystals [34], the orientations of grains at both sides of GBs are represented by pairs of dots in Fig. 3(b). The corresponding IF^{GB} is approximately 0.1. This implies that the stress incompatibility in the experiments are only 1/10 of the most extreme configuration. This may explain why the initial fracture position in the experiments did not occur at pre-existing GBs [34].

In summary, we have quantified incompatibility factor $IF = (\sigma_1 + \sigma_3)/\sigma^E$ and the discontinuity in hydrostatic stress σ_h near grain boundaries under external stress σ^E with a bicrystal model. The extreme values have been derived in terms of elastic tensor components. The incompatibility factors for general grain boundaries are estimated based on grain orientations. These findings provide valuable insights into failure phenomena, such as creep and fatigue, that occur in polycrystalline materials. Moreover, identifying grain boundaries with high and low stress concentration can guide the design of higher-performing materials.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Appendix A. Supplementary material

Supplementary material related to this article can be found online at <https://doi.org/10.1016/j.scriptamat.2023.115570>.

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