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1 **Experimental and analytical studies on shear behaviors of FRP-concrete composite sections**

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14

15 **ABSTRACT**

16 The design of FRP profile-concrete composite sections, including beams and decks, is usually  
17 governed by the shear strength of the FRP profiles. However, analytical methods that can precisely  
18 predict the shear capacity of the composite sections have not been well developed, because there  
19 is lack of knowledge of the FRP-concrete composite action and distribution of shear stress along  
20 the FRP. This paper investigates the shear behaviors of FRP-concrete composite sections and  
21 develops formulae to predict the shear capacity of the composite sections. First, flexural tests of  
22 three FRP-concrete composite beams were conducted to investigate the shear failure mode and  
23 interface behaviors. All the beams failed in FRP shear fracture along horizontal direction. Then,  
24 push-out tests were used to determine the slip property for the FRP-concrete interface which  
25 reveals that FRP stay-in-place form and steel bolts can ensure full and partial composite action,  
26 respectively. Based on the experimental study, closed-form equations to compute the maximum  
27 shear stress are derived and validated against experimental data in this paper and literature. Finally,  
28 simple yet reliable equations of shear capacity are derived and recommended for engineers to  
29 design the FRP-concrete composite sections.

30

31 **Key words:** shear capacity; FRP-concrete composite sections; composite action; slip effect; shear  
32 connection.

33 **Notation**

$A_{web}$	=	cross sectional area of FRP web(s);
$A_C, A_F$	=	cross sectional area of concrete and FRP, respectively;
$A_F(y)$	=	parameter in equations;
$b$	=	shear span length of beam specimens;
$b_C, b_F$	=	width of concrete slab and FRP flange, respectively;
$E_C, E_{Fx}$	=	elastic modulus of concrete and FRP (in longitudinal direction), respectively;
$h_0$	=	distance between the neutral axis of concrete and FRP;
$h_C, h_F$	=	height of concrete and FRP, respectively;
$I_C, I_F$	=	moment inertia of concrete and FRP, respectively;
$k$	=	smear slip modulus of the interface;
$K$	=	slip modulus per connector;
$L$	=	beam span;
$m(x)$	=	ratio given by $m(x) = h_0 k s(x) / V(x)$ ;
$m_0$	=	value of $m(x)$ at the support points of beams;
$m_{full}$	=	value of $m_0$ with full composite action;
$M_C(x), M_F(x)$	=	flexural moment carried by concrete and FRP, respectively;
$n$	=	number of rows of the connector in lateral direction;
$n_0$	=	number of studs in one push-out test specimens;
$N_C(x), N_F(x)$	=	axial force in concrete and FRP, respectively;
$p$	=	longitudinal space between two adjacent connectors;
$P$	=	total applied load;
$P_u$	=	experimental ultimate load;
$r(x)$	=	distributed normal force along FRP and concrete interface;
$s(x)$	=	interfacial slip;
$s_0$	=	slip at the load of $0.5P_u$ of push-out test;
$s_{max}$	=	maximum slip;
$S_{xy}$	=	shear strength of FRP web(s);
$S_F(y), S_C(y)$	=	parameters in equations;
$t(y)$	=	thickness of FRP web or FRP width;

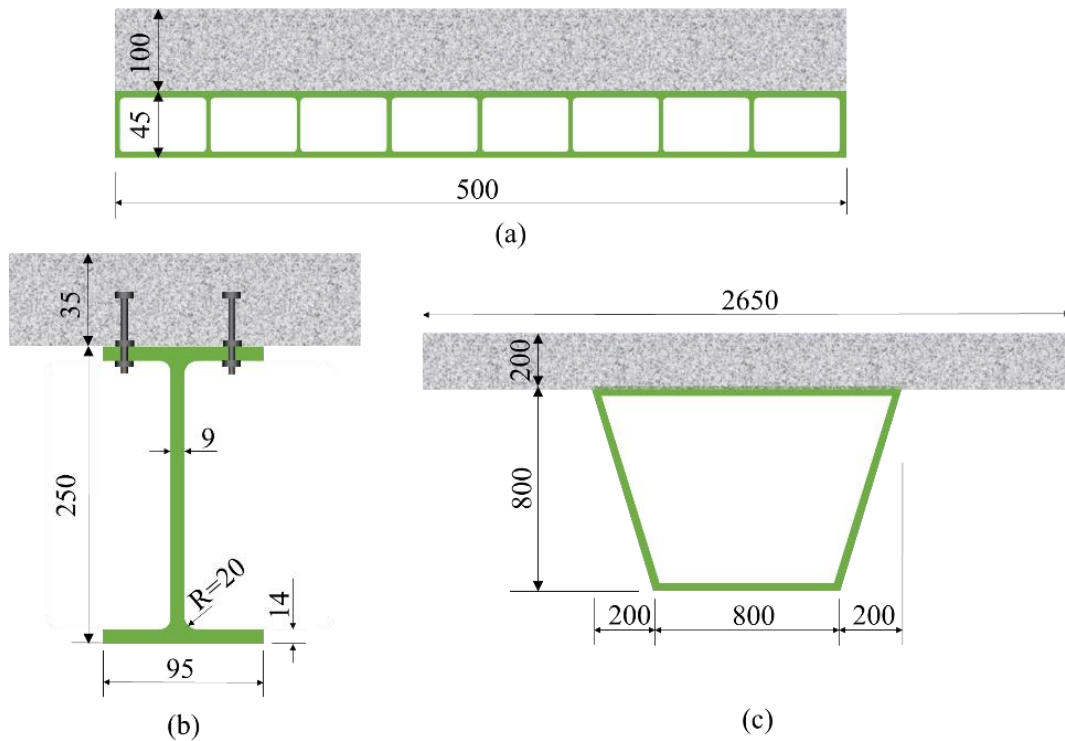
- $t_{web}$  = thickness of FRP web;  
 $V_1, V_2$  = shear capacity computed by Eq. (1) and Eq. (2), respectively;  
 $V(x), V_C(x), V_F(x)$  = shear force carried by the composite section, concrete and FRP, respectively;  
 $V_{test}$  = experimental shear capacity of beam specimens;  
 $X_C$  = compressive strength of FRP;  
 $y_0$  = vertical coordinate of the location of maximum shear stress;  
 $y_{0,ana}$  = analytical value of  $y_0$ ;  
 $y_{0,test}$  = experimental value of  $y_0$ ;  
 $\alpha, \beta, A_0, A_1, I_0$  = parameters used to simplify the equations;  
 $\alpha_E$  = ratio of  $E_{Fx}$  over  $E_C$ ;  
 $\alpha_1$  = ratio of cross sectional area of FRP flanges over concrete;  
 $\alpha_2$  = ratio of  $h_F$  and  $h_C$ ;  
 $\delta_u$  = maximum mid-span deflection;  
 $\varepsilon_C(x, y), \varepsilon_F(x, y)$  = strains of concrete and FRP, respectively;  
 $\varepsilon_{slip}(x)$  = strain difference caused by the slip at FRP-concrete interface;  
 $\eta_C, \eta_F$  = contribution ratio of concrete and FRP, respectively;  
 $\eta_{SD}$  = ratio of maximum shear stress over average shear stress;  
 $v(x)$  = distributed interfacial shear force along longitudinal direction;  
 $\sigma_F(x, y)$  = normal stress of FRP;  
 $\tau_C(x, y), \tau_F(x, y)$  = shear stress of concrete and FRP, respectively;  
 $\tau_{max}$  = maximum shear stress;  
 $\phi$  = curvature of the beam.

## 35 1. Introduction

36 Fiber reinforced polymer (FRP) has extraordinary mechanical and in-service properties, which can  
37 improve the stiffness, strength, durability, life-cycle cost, and environmental impacts when combined with  
38 other construction materials [1]. Recently, there are increasing research interests and filed applications of  
39 FRP profiles-concrete composite (or hybrid) structures, particularly in the forms of bridge decks [2], girders  
40 [3][4], and floor systems [5][6]. The FRP-concrete systems maximize the advantages of the materials by  
41 integrating FRP that is extremely durable and lightweight with concrete that is low-cost and has desired  
42 compressive strength [7][8]. Among various FRP-concrete systems, FRP-concrete composite beams/decks  
43 (see Fig. 1) demonstrated superior cost-effectiveness and high durability, compared with traditional steel-  
44 concrete composite structures and all-FRP structures [1][3][4][9][10][11]. Hereafter, FRP-concrete  
45 composite (or hybrid) beam/deck is referred as FRP-concrete composite section for a general meaning. The  
46 concrete slab is cast on top of an FRP profile (see Fig. 1). The concrete and FRP are joined by interfacial  
47 shear connection such as epoxy adhesives [5], perforated FRP ribs [2][9], steel bolts [3][11], FRP bolts [3],  
48 or FRP shear keys [4][8]. Flexural tests showed that glass FRP (GFRP)-concrete composite beams had  
49 higher stiffness and strength, compared with all GFRP profiles [12]. On the other side, compared to the  
50 equivalent reinforced concrete (RC) beams, the hybrid GFRP-concrete specimens displayed approximate  
51 50% higher ultimate capacity with 50% less weight [12].

52 Pultrusion is a cost-effective and efficient technique to manufacture FRP profiles with high quality  
53 control [1]. Pultruded FRP profiles have been widely used in FRP-concrete composite sections [13][14][15].  
54 Although FRP-concrete composite sections follow the same concept as steel-concrete composite sections,  
55 a salient difference is that the shear strength of pultruded FRP is fairly lower than that of steel profiles (see  
56 Table 1) [16][17][18][19]. Owing to the low shear strength, flexural tests on FRP-concrete composite  
57 sections often induce undesirable and catastrophic shear failure at FRP web or web-top flange junction at  
58 relatively low load levels [8][12][20][21]. Both GFRP-concrete interface failure and shear failure in GFRP  
59 webs have been observed from existing tests [20]. The GFRP-concrete bond failure can be avoided by  
60 developing effective shear connectors [8][9][22][23][24]. Therefore, the shear capacity usually governs the

61 design of the FRP-concrete composite sections, which means precisely computing the shear capacity plays  
 62 a critical role in the design.



63  
 64 **Fig. 1.** Typical cross section of: (a) FRP-concrete hybrid deck [2]; (b) open-section FRP-concrete hybrid  
 65 beam [3]; and (c) closed-section FRP-concrete hybrid beam [4]. Unit in mm.

66 **Table 1.** Typical ratio of shear strength ( $S_{xy}$ ) and compression strength ( $X_c$ ) of FRP and steel

Profile	Company	$S_{xy}$ (MPa)	$X_c$ (MPa)	$S_{xy}/X_c$
GFRP	Fiberline [16]	31	240	1/8
GFRP	Strongwell [17]	31	207	1/7
GFRP	Topglass [18]	25	220-230	1/12~1/9
GFRP	Creative Pultrution [19]	23-31	227-316	1/14~1/7
Steel		135	235 (Yield)	1/1.7

67  
 68 Currently, all the existing methods for the shear capacity of FRP-concrete composite sections neglect  
 69 the shear resistance of the concrete slab [20][21]. It is reasonable to neglect the shear resistance of the  
 70 concrete slab in steel-concrete composite beams, because the shear strength of the steel beam is typically  
 71 much higher than that of the concrete. However, since the shear strength of FRP profile is typically low,  
 72 neglecting the shear resistance of concrete may significantly compromise the accuracy of the analysis. For

73 example, it was assumed in [21] that the shear force was carried only by the FRP webs, and the shear stress  
 74 was uniform along the height of the FRP webs. Accordingly, the shear capacity of FRP-concrete composite  
 75 sections was expressed as:

$$V_1 = A_{web}S_{xy} \quad (1)$$

76 where  $V_1$  is the shear capacity;  $A_{web}$  is the total cross sectional area of the FRP web(s);  $S_{xy}$  is the shear  
 77 strength of the FRP web(s). However, the assumption of the uniform shear stress distribution is not  
 78 consistent with the reality. Hence, it was assumed in [20] that the maximum shear stress in FRP webs was  
 79 1.5 times the average shear stress. So, the shear capacity was expressed as:

$$V_2 = \frac{2}{3}A_{web}S_{xy} \quad (2)$$

80 where  $V_2$  is the shear capacity. Table 2 shows the test results of 12 specimens with a shear failure at FRP  
 81 web(s) or top-flange-web joints [5][8][12][21]. Eqs. (1) and (2) underestimated the shear capacity by 18%  
 82 and 45%, respectively. There is a need to develop a more accurate method to predict the shear capacity of  
 83 the FRP-concrete composite sections.

84 **Table 2.** Comparison between analytical [Eqs. (1) and (2)] and experimental results of shear capacity

Reference	Specimen	Profile depth (mm)	Web thickness (mm)	Web area (mm <sup>2</sup> )	$S_{xy}$ (MPa)	$V_1$ (kN)	$V_2$ (kN)	$V_{test}^*a$ (kN)	$\frac{V_1}{V_{test}}$	$\frac{V_2}{V_{test}}$
[8]	HB	150	10	1500	25.3	37.5	25.0	49.6	0.76	0.50
	HB-T	150	10	1500	25.3	37.5	25.0	74.8	0.50	0.33
	HB-R	150	10	1500	25.3	37.5	25.0	47.3	0.79	0.53
[21]	Beam C*-S	228.6	11.1×2	5075	31.0	157.3	104.9	170.5	0.92	0.62
	Beam S*-S	228.6	11.1×2	5075	31.0	157.3	104.9	191.5	0.82	0.55
[5]	HB1	200	10	2000	47.1 <sup>*b</sup>	94.2	62.8	91.00	1.04	0.69
	HB3	200	10	2000	47.1 <sup>*b</sup>	94.2	62.8	148.10	0.64	0.42
	HB5	200	10	2000	47.1 <sup>*b</sup>	94.2	62.8	87.90	1.07	0.71
[12]	M2-HB1	120	8	960	35.0	33.6	22.4	39.00	0.86	0.57
	M2-HB2	120	8	960	35.0	33.6	22.4	37.67	0.89	0.59
	M2-HB3	120	8	960	35.0	33.6	22.4	44.88	0.75	0.50
	M2-HB4	120	8	960	35.0	33.6	22.4	45.63	0.74	0.49
Average									0.82	0.55

85 \*a.  $V_{test}$  is the test result of the shear capacity of the specimens.

86 \*b. The value was provided by the authors of [12].

87 This paper investigates the shear behavior of FRP-concrete composite sections and develops formulae  
 88 to accurately predict the shear capacity of the composite sections, aiming to advance the fundamental



89 understandings of the composite behaviors and provide effective tools for the design and evaluation of FRP-  
90 concrete composite sections.

91

## 92 **2. Method**

93 This study aims at more advanced understanding of the shear behavior of FRP-concrete hybrid sections  
94 and proposing a design method for the shear capacity considering the contribution of concrete.  
95 Experimental tests were conducted in four-point bending, where the specimens were designed to be failed  
96 in shear. An analytical approach, returned to the fundamental analysis of composite action, was proposed  
97 to compute the shear stress of the specimen. The results of maximum shear stress given by derived equations  
98 were compared against the experimental results. Based on the experimental study and the analytical  
99 approach, closed-form equations of the shear capacity of the composite sections were derived, considering  
100 the contribution of concrete and interfacial slip. Finally, methods and equations that can be conveniently  
101 applied to design the FRP-concrete composite sections were explored.

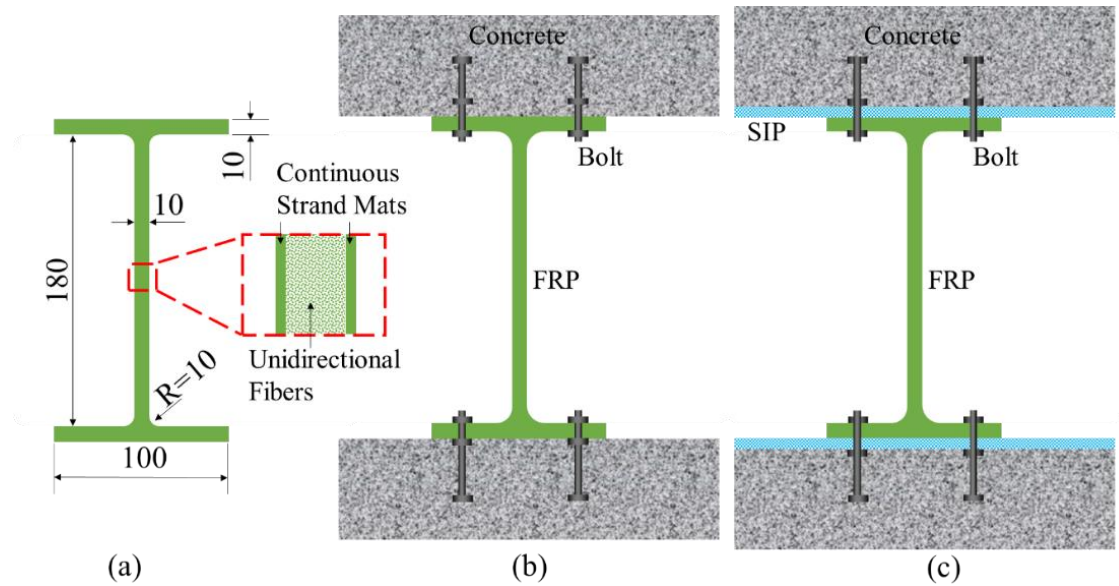
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## 103 **3. Experimental Investigation**

104 This section presents the flexural test of FRP-concrete composite beams and push-out test of FRP-  
105 concrete connectors. Subsection 2.1 introduces the materials and properties. Subsection 2.2 introduces the  
106 flexural test. Subsection 2.3 introduces the push-out test.

### 107 **3.1. Materials**

108 FRP profiles (see Fig. 2a) were made from unsaturated polyester resin reinforced by glass fibers  
109 through pultrusion technique. The FRP products are commercially available at the Nanjing Kangte  
110 Composite Material Co., Ltd., in Nanjing, China [25]. The fiber layout of the FRP profiles is unidirectional  
111 roving in the core sandwiched between two layers of continuous-strand mats along the outer surfaces (see  
112 Fig. 2a). The mass percentage of fibers is approximate 45%, the mass percentage of resin is 35%, and the  
113 left is CaCO<sub>3</sub> powder filler, according to the manufacturer.



114 (a) (b) (c)

115 **Fig. 2.** Cross sections of: (a) FRP profile, (b) push-out test specimens of Group I &II, and (c) push-out test  
 116 specimens of Group III. SIP stands for stay-in-place formwork.

117 The density of the profiles is 1,900 kg/m<sup>3</sup>, as specified by the manufacturer. The tensile, compressive,  
 118 and shear properties were obtained through testing tensile, compressive, and short three-point bending  
 119 coupons, respectively, according to Chinese standard GB 50608–2010 [26]. The coupons were cut from the  
 120 actual pultruded profiles and machined to the exact dimensions. The longitudinal tensile and compressive  
 121 strengths were 420 MPa and 350 MPa, respectively. The longitudinal tensile and compressive moduli were  
 122 25 GPa and 23 GPa, respectively. The shear strength was 9.2 MPa, which is lower than other commercial  
 123 products shown in Table 1. The low shear strength is attributed to the lack of multi-directional fibers on the  
 124 webs and the use of CaCO<sub>3</sub> powder as the filler in the resin matrix.

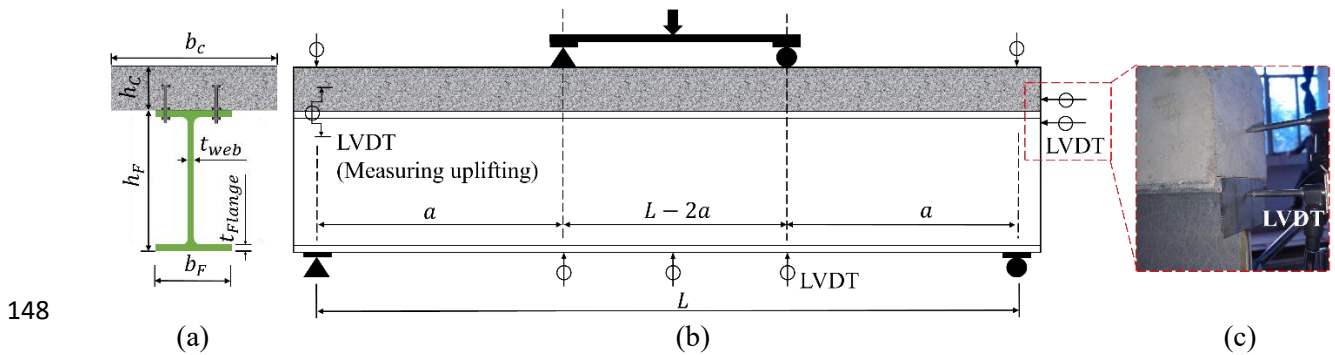
125 The concrete was designed to achieve a compressive strength of 30 MPa at 28 days. The specimens  
 126 were cast and tested in accordance with Chinese standard GB 50010–2010 [27]. The average values of the  
 127 elastic modulus, compressive strength, and compressive strain at peak stress of the concrete were 28.2 GPa,  
 128 29.5 MPa, and 0.00263, respectively. All push-out and flexural specimens were cured under identical  
 129 condition as the coupons for material properties testing.

130 Steel bolts (see Figs. 2b and 2c) were fixed on the top flanges of the FRP profiles using nuts and  
 131 washers on both sides of the FRP flange plate. The steel bolts serve as headed studs that integrate the

132 concrete and FRP. The grade of the steel was Grade M10 8.8 with the tensile and yield strengths of 800  
 133 MPa and 640 MPa, respectively. For the meaning of the Grade  $Ma\ b.c$ , the diameter of the stud shank is  $a$   
 134 mm, the tensile strength is  $b \times 100$  MPa, and the ratio of yield strength over tensile strength is  $c \times 0.1$ . The  
 135 steel stud in this study had a diameter of 100 mm. The embedded length in concrete, defined as the distance  
 136 from the top of the stud to the top of the FRP flange, was 80 mm. Steel washers, with an outer diameter of  
 137 20 mm, inner diameter of 10.5 mm (slightly larger than the diameter of the studs) and a thickness of 2 mm,  
 138 were used to distribute the local stress caused by axial pre-tightening force of the studs.

139 **3.2. Flexural test of FRP-concrete composite beams**

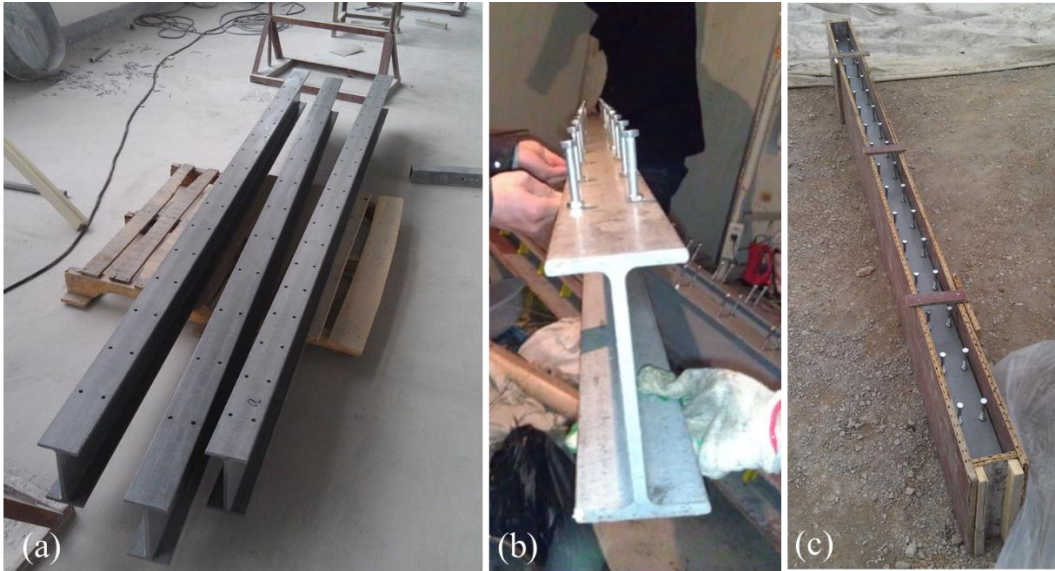
140 Three FRP-concrete composite beams were tested, as shown in Fig. 3. Each beam was composed of  
 141 an I-shaped pultruded GFRP beam (see Fig. 2a, Fig. 3a) and a concrete slab (see Fig. 3). All specimens  
 142 were simply supported and loaded under four-point bending. The deflections and the slippages were  
 143 measured by linear variable differential transformers (LVDTs). The strains in FRP and concrete were  
 144 measured by strain gauges. Two LVDTs were used to measure the horizontal displacements of FRP and  
 145 concrete, respectively, and the different horizontal displacements indicated the interfacial slip. The web  
 146 thickness ( $t_{web}$ ) and flange thickness ( $t_{Flange}$ ) of the FRP profile were 10 mm. The transversal space of  
 147 the steel studs was 55 mm.



149 **Fig. 3.** FRP-concrete composite beam: (a) cross section, (b) side view, and (c) deployment of the LVDTs  
 150 measuring slip.

151 The specimens were fabricated in four steps: (i) drill holes in the upper flanges of FRP profiles (see  
 152 Fig. 4a), (ii) install steel studs at the predefined locations (see Fig. 4b), (iii) fabricate the wood formwork

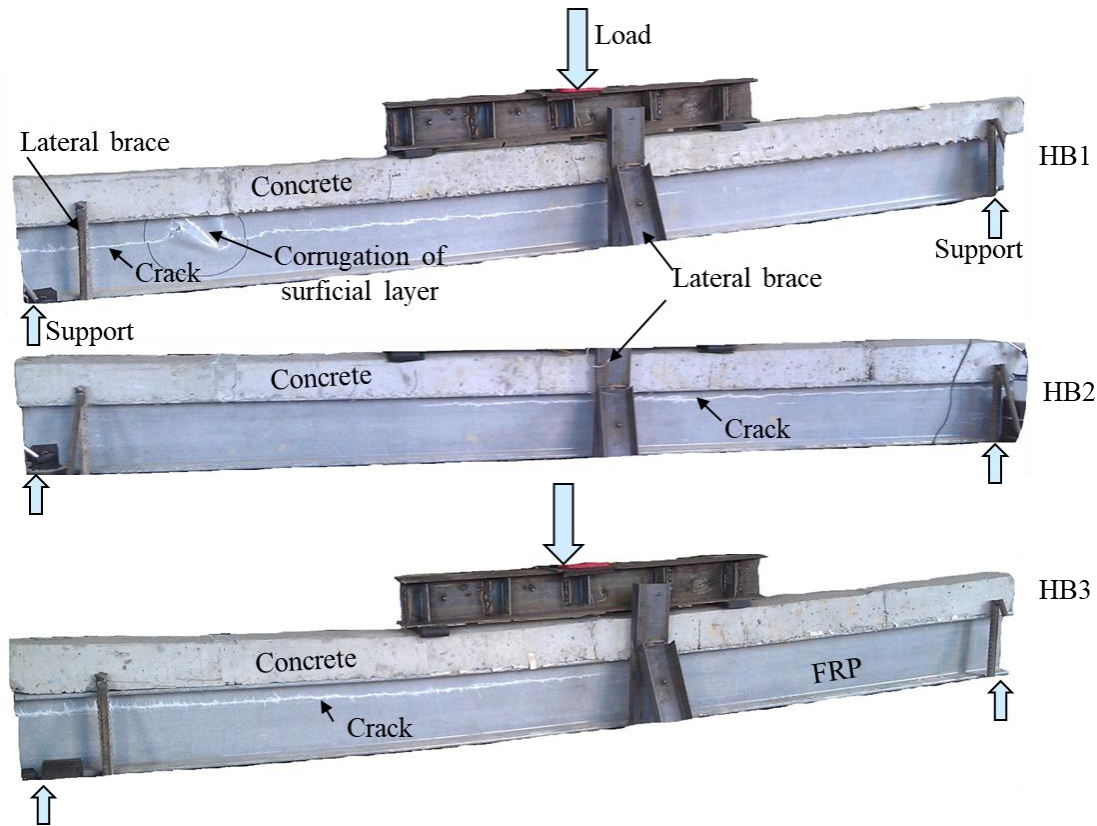
153 (see Fig. 4c), and (iv) cast concrete slab.



154

155 **Fig. 4.** Construction of FRP-concrete composite beam specimens: (a) FRP beams with drilled holes, (b) an  
156 FRP beam with steel studs, and (c) wood forms.

157 Similar failure processes and modes were observed from the three specimens. Before the failure, there  
158 was no notable acoustic activities and visible cracks. As the load reached the ultimate capacity, a crack on  
159 FRP web occurred from the support and suddenly propagated to the mid-span in a few seconds (see Fig. 5),  
160 resulting in a catastrophic and brittle failure.



161

162 **Fig. 5.** Failure modes of the FRP-concrete composite beam specimens tested under four-point bending.

163 The results are summarized in Table 3, where  $P_u$  is the experimental ultimate load,  $y_{0,test}$  is the  
 164 average vertical coordinate (the coordinate system will be introduced in the next section) of the main crack  
 165 (see white lines in Fig. 5),  $y_{0,ana}$  is the value which will be introduced in next section,  $\delta_u$  is the maximum  
 166 mid-span deflection, and  $s_{max}$  is the maximum slip.

167

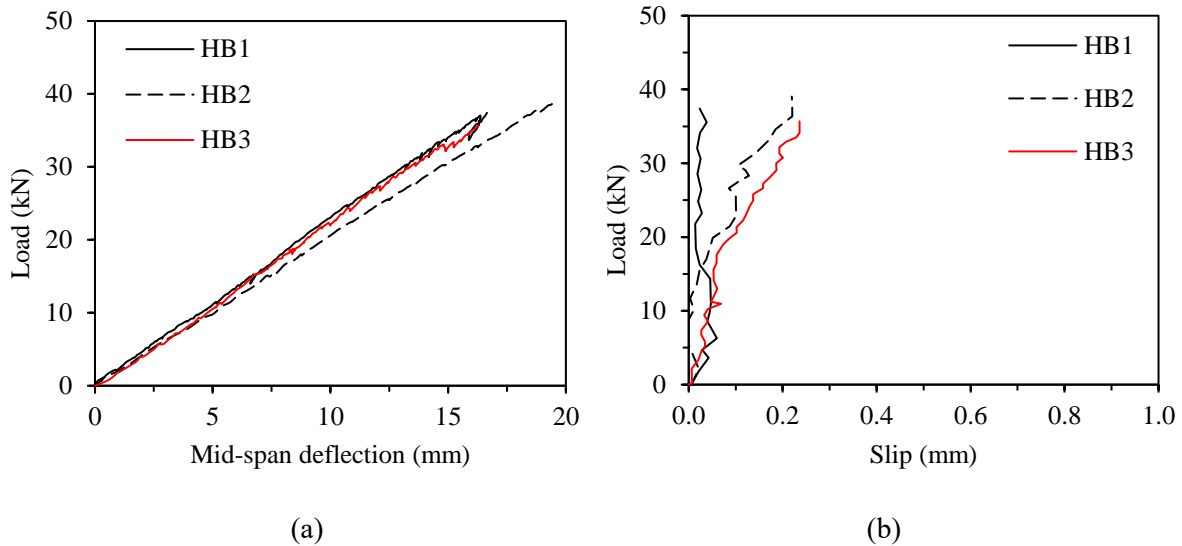
**Table 3.** Results of flexural tests

Specimen	$h_c$ (mm)	$b_c$ (mm)	$P_u$ (kN)	$y_{0,test}$ (mm)	$y_{0,ana}$ (mm)	$\frac{y_{0,ana}}{y_{0,test}}$	$\delta_u$ (mm)	$s_{max}$ (mm)
HB1	100	100	37.4	-56.5	-49.28	0.87	16.7	0.060
HB2	100	100	39.0	-61.5	-55.78	0.91	17.7	0.219
HB3	100	100	35.7	-58.6	-61.48	1.05	16.3	0.236

168

169 The load-deflection curves are plotted in Fig. 6a. The load increases approximately linearly with the  
 170 mid-span deflection until the brittle shear failure. The load-slip relationships are plotted in Fig. 6b. The slip  
 171 of HB1 was less than 0.06 mm, smaller than the rest two specimens, because HB1 had more steel studs as  
 172 the shear connection. The slips of HB2 and HB3 were close, with a maximum value of 0.219 mm and 0.236

173 mm, respectively. The interfacial uplifting - vertical separation, measured by the vertical LVDT at the left  
 174 side of the beam in Fig. 3b - was almost zero for all the beams during the loading.



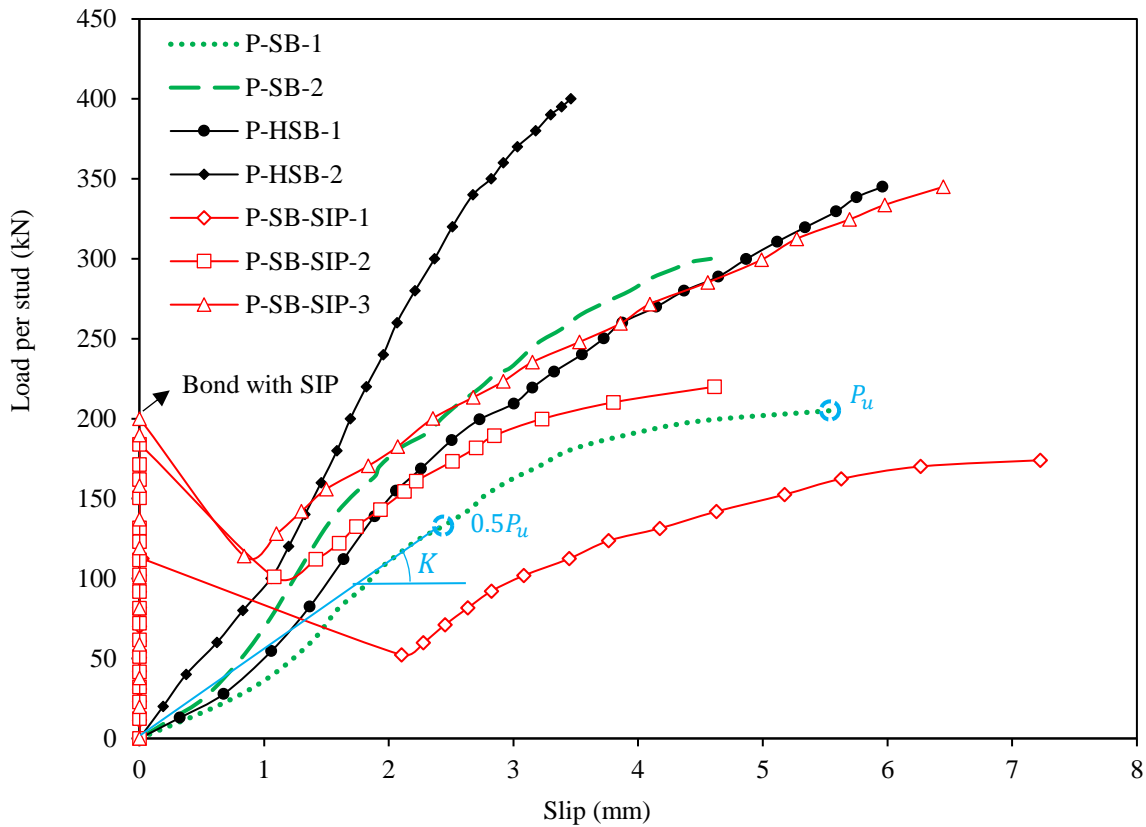
175  
 176 (a) (b)  
 177 **Fig. 6.** Test results of FRP-concrete composite beam specimens: (a) load-deflection responses, and (b) load-  
 178 slip responses.

179 **3.3. Determining slip modulus from the load-slip response of push-out specimens**

180 In order to consider the slip between FRP and concrete, the slip stiffness for each connector,  $K$ , was  
 181 experimentally determined through push-out tests (see Figs. 2b and 2c), as reported in [8]. Three groups of  
 182 connectors were tested, namely Groups I, II, and III. Group I had ordinary steel studs (SB), Group II had  
 183 high steel studs (HSB, the same as the studs used in beam test of this paper, see Section 2.2), and Group III  
 184 used stay-in-place formwork (see Fig. 2c) between the FRP and concrete. The formwork provided bond  
 185 with the concrete slab and eased the construction of concrete. Groups I and II showed two failure modes,  
 186 namely the studs shank shear fracture and shear-out failure of FRP flange, as elaborated in [24]. Fig. 7 plots  
 187 the load-slip response, which is a pivotal factor to evaluate the composite action of the FRP-concrete  
 188 composite sections. The secant slope at half of the ultimate load,  $0.5P_u$ , is defined as slip modulus –  $K$  (see  
 189 Fig. 7), which is given as:

$$K = \frac{0.5P_u}{n_0s_0} \quad (3)$$

190 where  $n_0$  is the number of studs in a push-out test;  $s_0$  is the slip at the load  $0.5P_u$ . Table 4 lists the results  
 191 of  $K$  of push-out specimens in [5][8][24].



192  
 193 **Fig. 7.** The relationship between the load per stud and interfacial slip between FRP and concrete. The bond  
 194 between the SIP and concrete caused a zero-slip phase at the beginning of loading.

195  
 196

**Table 4.** Parameters and results of push-out tests

Reference	Specimen	$n_0$	$p$ (mm)	Studs	$0.5P_u$ (kN)	$s_0$ (mm)	$K$ (kN/mm)
[8]	P-SB-1	8	200	M10 4.6	105	1.91	6.87
	P-SB-2	12	150	M10 4.6	150	1.73	7.23
	P-HSB-1	8	200	M10 8.8	170	2.26	9.40
	P-HSB-2	12	150	M10 8.8	200	1.69	9.86
[24]	Specimen 1	4	150	M10 6.8	47.9	2.13	5.70
	Specimen 2	4	150	M10 6.8	61.0	2.74	5.65
	Specimen 3	4	150	M10 6.8	61.4	2.31	6.67
	Specimen 4	4	150	M10 6.8	46.9	3.78	3.09
	Specimen 5	4	150	M10 6.8	55.3	2.54	5.53
[5]	SCS1	4	200	M8 8.8	40	0.92	10.87
	SCS2	4	200	M10 8.8	80	1.00	20.00
	SCS3	4	200	M10 8.8	60	1.25	12.00

197

#### 198 4. Analytical Study on Shear Capacity

199 This section conducts analytical study on the shear behavior of FRP-concrete composite sections  
200 considering slip effect and the distribution of shear stress in the FRP profile. Subsection 3.1 investigates the  
201 interfacial slip behaviors. Subsection 3.2 investigates the shear stress distributions in FRP and concrete  
202 considering the interfacial slip. Subsection 3.3 shows the validation of analytical results against the tests.

##### 203 4.1. Interfacial slip

204 Similar to steel-concrete composite sections [28], an FRP-concrete composite section is composed of  
205 an FRP profile and a concrete slab that are discontinuously connected, as shown in Fig. 8. Mechanical  
206 analysis is conducted to analyze the FRP-concrete composite section based on the following assumptions:

- 207 (i) Only the shear connectors and SIP formwork contribute to the shear connection between the FRP  
208 and concrete. **The discrete connectors were smeared to the whole length of the interface, which is**  
209 **similar to the analysis of steel-concrete composite sections [29][30][31]. By so doing, the model**  
210 **does not distinguish between discontinuous and continuous layers connection.** For the specimens  
211 with epoxy shear connection [32], FRP shear keys [8], and perforated FRP ribs [24], the interface  
212 has full composite action, because the slip is very small compared with the specimens with steel  
213 bolts.
- 214 (ii) The curvature and deflection of the FRP and concrete are the same. In other words, there is no  
215 vertical separation (uplifting effect) at the interface, which has been the test results in Section 2.2.
- 216 (iii) Bernoulli's hypothesis on strain distribution is applicable to sections of FRP and concrete separately,  
217 i.e., the shear deformation has been neglected, this may cause some error so the influence will be  
218 discussed according to experimental test.

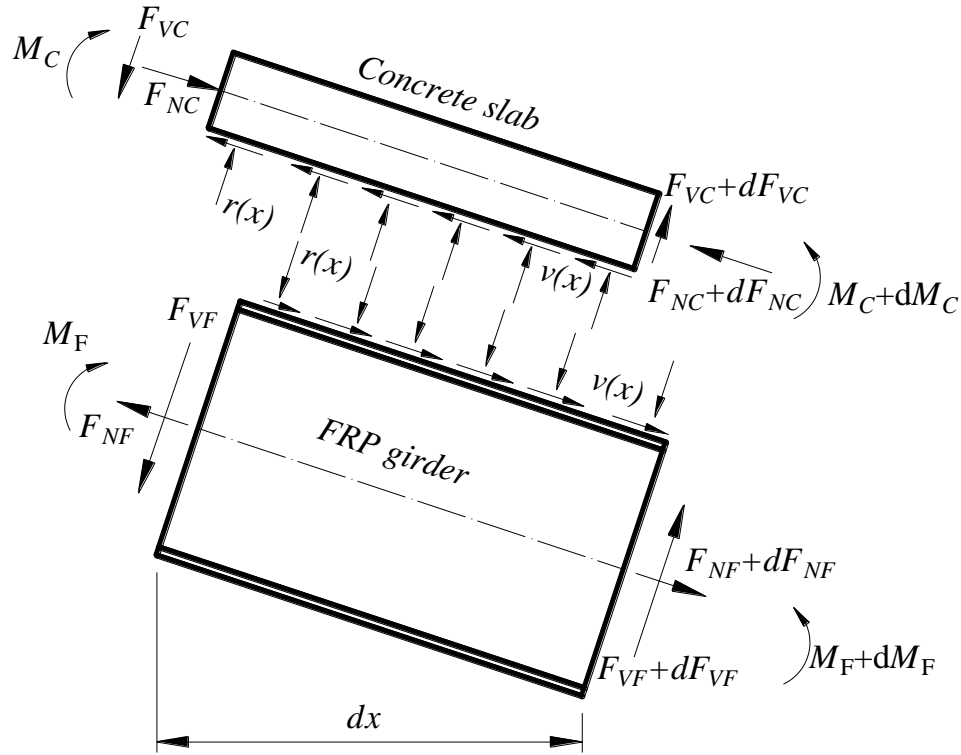
219 According to assumption (i), Eqs. (4) and (5) are obtained:

$$v(x) = ks(x) \tag{4}$$

$$k = nK/p \tag{5}$$



220 where  $v(x)$  is the distributed interfacial shear force (see Fig. 8);  $x$  is the longitudinal coordinate with the  
 221 origin at support point;  $k$  is the smeared slip modulus of the interface;  $s(x)$  is the interfacial slip (see Fig.  
 222 8);  $n$  is the number of rows of the connector in lateral direction;  $K$  is the slip modulus per connector defined  
 223 by Eq. (3) from the push-out tests (see Fig. 7);  $p$  is the longitudinal space between two adjacent connectors.



224

**Fig. 8.** Model of sectional analysis of section  $dx$ .

225

226 According to equation of equilibrium of the infinitesimal ( $dx$ ), in the horizontal ( $x$ ) direction:

$$\frac{dN_C(x)}{dx} = \frac{dN_F(x)}{dx} = -v(x) \quad (6)$$

227

where  $N_C(x)$  and  $N_F(x)$  are the axial forces carried by concrete and FRP, respectively.

228

According to equation of equilibrium of the infinitesimal ( $dx$ ), in the vertical ( $y$ ) direction, the shear

229

force satisfies:

$$V_C(x) + V_F(x) = V(x) \quad (7)$$

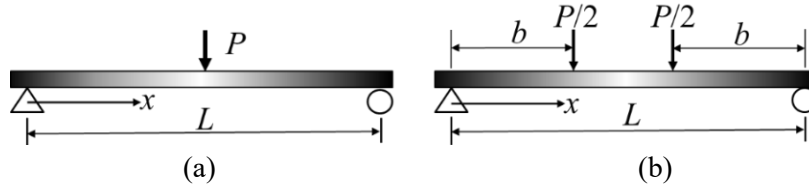
230

where  $V_C(x)$  and  $V_F(x)$  are the shear forces carried by the concrete and FRP, respectively;  $V(x)$  is the total

231

shear force. Under three-point bending (Fig. 9a) or four-point bending (Fig. 9b):  $V(x) = P/2$ , where  $P$  is

232 the total applied load.



233  
234 **Fig. 9.** Typical load definitions: (a) three-, and (b) four-point bending.

235 The moment equilibrium of the concrete and FRP segments gives:

$$\frac{dM_C(x)}{dx} - v(x) \frac{h_C}{2} + r(x) \frac{dx}{2} + V_C(x) = 0 \quad (8a)$$

$$\frac{dM_F(x)}{dx} - v(x) \frac{h_F}{2} - r(x) \frac{dx}{2} + V_F(x) = 0 \quad (8b)$$

236 where  $M_C(x)$  and  $M_F(x)$  are the moments carried by the concrete and FRP, respectively;  $h_C$  and  $h_F$  are the  
237 depths of concrete and FRP, respectively (see Fig. 4a);  $r(x)$  is the normal force along the FRP-concrete  
238 interface.

239 According to assumption (ii), the curvature compatibility of the concrete and FRP gives:

$$\phi(x) = \frac{M_F(x)}{E_{Fx} I_F} = \frac{M_C(x)}{E_C I_C} \quad (9)$$

240 where  $E_{Fx}$  is the elastic modulus of FRP in  $x$  direction;  $I_F$  and  $I_C$  are the moment inertias of FRP and  
241 concrete, respectively;  $E_C$  is the elastic modulus of concrete;  $\phi(x)$  is the curvature of the beam.

242 For the constitutive relationships of the materials, linear elastic properties of the FRP and concrete are  
243 adopted. The FRP is inherently linear elastic; the stresses in the concrete remain low before the FRP fails  
244 with a shear failure, as supported by the test results in Section 2 and previous experiments in [8][11][21].  
245 The longitudinal modulus of FRP is employed to compute the sectional rigidity, assuming the compressive  
246 and tensile moduli of FRP are the same. Strains in the concrete  $\varepsilon_C(x, y)$  and FRP  $\varepsilon_F(x, y)$  are calculated  
247 from the moment and axial force as:

$$\varepsilon_C(x, y) = \frac{M_C(x) \left( \frac{h_C}{2} - y \right)}{E_C I_C} - \frac{N_C(x)}{E_C A_C}, \quad 0 \leq y \leq h_C \quad (10a)$$

$$\varepsilon_F(x, y) = -\frac{M_F(x) \left( \frac{h_F}{2} + y \right)}{E_{Fx} I_F} + \frac{N_F(x)}{E_{Fx} A_F}, -h_F \leq y \leq 0 \quad (10b)$$

248 where  $A_C$  and  $A_F$  are the cross sectional areas of the concrete and FRP, respectively;  $y$  is vertical coordinate.

249 Eq. (11) gives the strains in the concrete and FRP at the interface.

$$\varepsilon_C(x, 0) = \frac{M_C(x) h_C}{2E_C I_C} - \frac{N_C(x)}{E_C A_C} \quad (11a)$$

$$\varepsilon_F(x, 0) = -\frac{M_F(x) h_F}{2E_{Fx} I_F} + \frac{N_F(x)}{E_{Fx} A_F} \quad (11b)$$

250 The strain difference caused by the slip at the interface, denoted as  $\varepsilon_{slip}(x)$ , is calculated as:

$$\varepsilon_{slip}(x) = \varepsilon_C(x, 0) - \varepsilon_F(x, 0) \quad (12)$$

251 The strain difference is equal to the first order derivation of the relative slip at the interface:

$$s'(x) = \varepsilon_{slip}(x) \quad (13)$$

252 Substituting Eqs. (8), (9), (11), and (12) into (13),

$$s'(x) = \phi(x) h_0 - \frac{N_C(x)}{E_C A_C} - \frac{N_F(x)}{E_{Fx} A_F} \quad (14)$$

253 where  $h_0$  is the distance between the neutral axis of concrete and FRP, given by  $h_0 = \frac{h_C + h_F}{2}$ .

254 Solving Eqs. (6) and (14) yields:

$$\phi'(x) = \frac{V(x) - h_0 k s(x)}{E_{Fx} I_0} = \frac{V(x)}{E_{Fx} I_0} [1 - m(x)] \quad (15)$$

255 where  $I_0 = I_C/\alpha_E + I_F$ ,  $\alpha_E = E_{Fx}/E_C$ , and  $m(x) = h_0 k s(x)/V(x)$ .

256 At the supports ( $x = 0, L$ ),  $m(x) = m_0$ , where  $m_0$  is a dimensionless factor depending on the shear  
257 connection. The physical meaning of  $m_0$  will be discussed in Section 4. Table 5 shows the solutions of  $m_0$ .

258 Plugging Eq. (14) in Eq. (15), the governing equation of the relative slip is obtained:

$$s''(x) - \alpha^2 s(x) = -\alpha^2 \beta V(x) \quad (16)$$

259 where  $\alpha = \sqrt{k A_1 / (E_{Fx} I_0)}$ ,  $\beta = h_0 / k A_1$ ,  $A_1 = I_0 / A_0 + h_0^2$ , and  $A_0 = A_F A_C / (\alpha_E A_F + A_C)$ .

260 To solve Eq. (16), the boundary conditions are considered:  $s(L/2) = 0$ , and  $\frac{ds(0)}{dx} = \frac{ds(L)}{dx} = 0$ . Table

261 5 shows the solutions of interfacial slip under the three-point and four-point bending tests.

262 **Table 5.** Loads and corresponding solutions

Loads	Solution of $s(x)$	$m_0$	$m_{0,full}$
Fig. 9a	$\frac{\beta P}{2} \left[ 1 - \cosh(\alpha x) / \cosh\left(\frac{\alpha L}{2}\right) \right], 0 < x < L/2$	$\frac{h_0^2}{A_1} \left[ 1 - \operatorname{sech}\left(\frac{\alpha L}{2}\right) \right]$	$\frac{h_0^2}{A_1}$
Fig. 9b	$\begin{cases} \frac{\beta P}{2} \left\{ 1 - \operatorname{sech}\left(\frac{\alpha L}{2}\right) \cosh\left[\alpha\left(\frac{L}{2} - b\right)\right] \cosh(\alpha x) \right\}, 0 < x < b \\ \frac{\beta P}{2} \operatorname{sech}\left(\frac{\alpha L}{2}\right) \sinh\left[\alpha\left(\frac{L}{2} - x\right)\right] \sinh(\alpha b), b < x < L/2 \end{cases}$	$\frac{h_0^2}{A_1} \left[ 1 - \operatorname{sech}\left(\frac{\alpha L}{2}\right) \cosh\left[\alpha\left(\frac{L}{2} - b\right)\right] \right]$	$\frac{h_0^2}{A_1}$

263

#### 264 4.2. Shear stress distributions in FRP and concrete

265 Fig. 10 shows the normal stress distribution in the FRP-concrete composite section. According to  
 266 equation of equilibrium of the infinitesimal ( $dx$ ) in  $x$  direction, Eq. (17) is obtained:

$$\tau_F(x, y)t(y)dx + \int_{-h_F}^y \sigma_F(x, y)t(y)dy = \int_{-h_F}^y \left[ \sigma_F(x, y) + \frac{\partial \sigma_F(x, y)}{\partial x} dx \right] \cdot t(y)dy \quad (17)$$

267 where  $\tau_F(x, y)$  is the shear stress of FRP;  $t(y)$  is the thickness of FRP web or FRP width;  $\sigma_F(x, y)$  is the  
 268 normal stress of FRP.

269 Simplifying Eq. (17) and cancelling out the same items yield:

$$\tau_F(x, y)t(y) = \int_{-h_F}^y \frac{\partial \sigma_F(x, y)}{\partial x} t(y)dy \quad (18)$$

270 According to the Hook's law, the stress in the FRP can be expressed as:

$$\sigma_F(x, y) = E_{Fx} \varepsilon_F(x, y) \quad (19)$$

271 Substituting Eqs. (10a) and (19) to Eq. (18) yields:

$$\tau_F(x, y) = [V(x) - h_0 k s(x)] \frac{S_F(y)}{I_0 t(y)} + \frac{k s(x)}{t(y)} \cdot \frac{A_F(y)}{A_F}, -h_F \leq y \leq 0 \quad (20)$$

272 where  $S_F(y) = \int_{-h_F}^y \left( y + \frac{h_F}{2} \right) t(y)dy$  and  $A_F(y) = \int_{-h_F}^y t(y)dy$ .

273 Analogously, the shear stress of concrete is written as:

$$\tau_C(x, y) = [V(x) - h_0 k s(x)] \frac{S_C(y)}{\alpha_E I_0 b_C} + \frac{k s(x)}{b_C} \cdot \frac{h_C - y}{h_C}, -h_F \leq y \leq 0 \quad (21)$$

274 where  $\tau_C(x, y)$  is the shear stress of concrete, and  $S_C(y) = \int_y^{h_C} b_C \left( y - \frac{h_C}{2} \right) dy$ .

275 Eq. (20) can be used to obtain the shear stress of FRP web ( $-h_F + t_{Flange} \leq y \leq -t_{Flange}$ ), where  
 276  $t_{Flange}$  is the thickness of FRP flange:

$$\tau_{F,web}(x, y) = \frac{V(x)}{t_{web}} \left[ [1 - m(x)] \frac{S_F(y)}{I_0} + m(x) \frac{A_F(y)}{h_0 A_F} \right] \quad (22)$$

277 The maximum shear stress occurred symmetrically at two supports ( $x = 0, L$ ), thus,

$$\tau_{F,web}(0, y) = \frac{P}{2t_{web}} \left[ (1 - m_0) \frac{S_F(y)}{I_0} + m_0 \frac{A_F(y)}{h_0 A_F} \right] \quad (23)$$

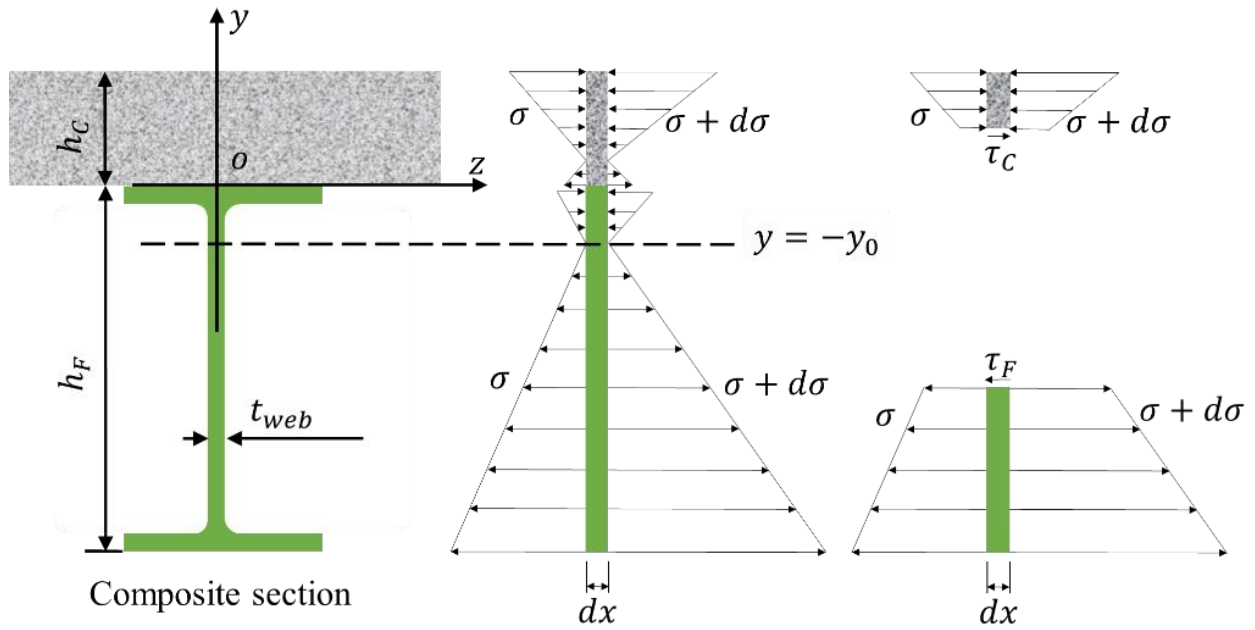
278 To locate the maximum shear stress, it is enforced that:

$$\frac{\partial \tau_{F,web}(0, y)}{\partial y} = 0 \quad (24)$$

279 Solving Eq. (24) gives the maximum shear stress ( $\tau_{max}$ ) at the point  $(0, y_0)$ , where  $y_0$  is given by:

$$y_0 = \frac{I_0}{A_F h_0} \cdot \frac{1}{\frac{1}{m_0} - 1} - \frac{h_F}{2} \quad (25)$$

280 The analytical and experimental results of  $y_0$  for the specimens in Section 2 are listed in Table 4. It  
 281 can be deduced from the computation of  $y_0$  that  $-h_F/2 \leq y \leq -t_{Flange}$ , meaning that the maximum shear  
 282 stress ( $\tau_{max}$ ) is within the FRP web (Fig. 11a);  $y \geq -t_{Flange}$ , meaning that the maximum shear stress is  
 283 within the FRP web-flange joint (Fig. 11b). Different failure criteria were used to predict the failure of FRP  
 284 in past research. In this study, since the normal stress in the FRP web is far less than its strength, the  
 285 maximum shear stress failure criterion is employed.



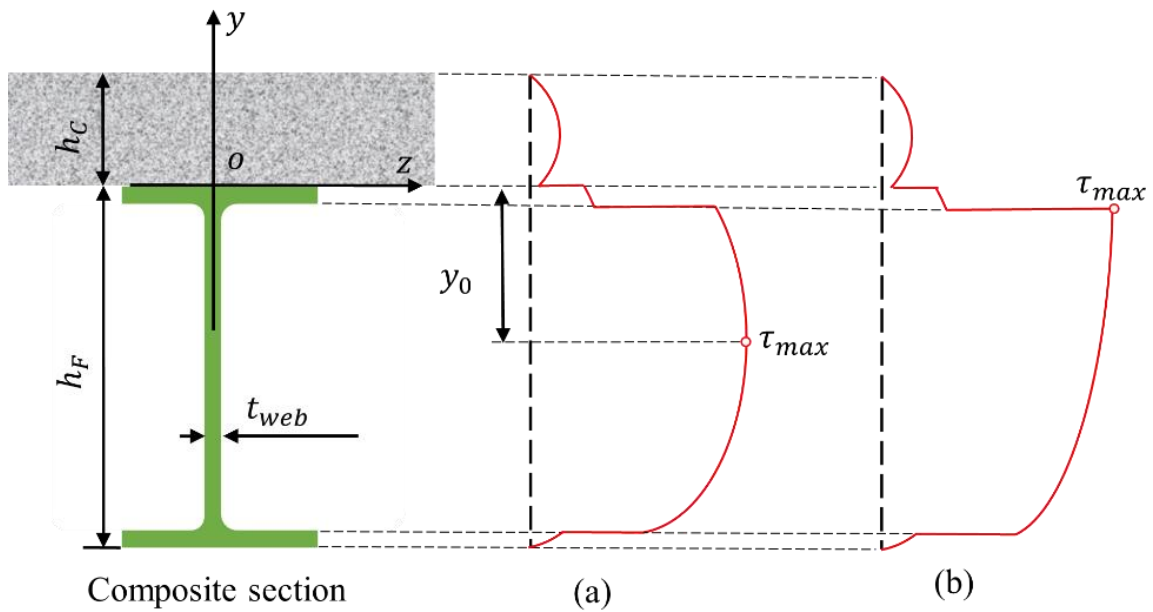
286

Composite section

287

Fig. 10. The distribution of the normal stress in the FRP-concrete composite section.

288



289

Composite section

(a)

(b)

290

Fig. 11. The maximum shear stress may occur in (a) the FRP web, and (b) the FRP web-flange joint.

291

#### 4.3. Validation

292

Table 6 compares the shear strengths of specimens determined using the derived formulae and

293 experiments [5][12]. The average result of  $\frac{\tau_{max}}{S_{xy}}$  is 1.023 with a coefficient of variation (CoV) of 0.162. The  
 294 analytical results of  $y_0$  are in Table 4, which shows good agreement with the measured values. The  
 295 relatively high variation of  $\frac{\tau_{max}}{S_{xy}}$  of the specimens in [5] is likely due to incorrect material strength data. For  
 296 the rest of the specimens,  $\frac{\tau_{max}}{S_{xy}}$  is close to 1.0, and CoV is small, revealing that Eq. (22) can be used to  
 297 compute the shear stress.  $\tau_{max}$  of specimen HB-T is 22% lower than  $S_{xy}$ , which is because the thick and  
 298 wide concrete slab had some cracks when FRP failed. The influence of these cracks indicates that concrete  
 299 damage should be considered when the concrete is thick compared with the depth of the FRP, which will  
 300 be further researched.

301 Fig. 12 compares the shear strength of the FRP with the shear stress distribution along the depth of the  
 302 FRP profile of each specimen listed in Table 6. In each specimen, the shear stress distribution is nonuniform  
 303 and shows a parabolic shape. The shear stresses in the concrete are significantly lower than the shear stresses  
 304 in the FRP profiles. This is associated with the larger thickness of the concrete.

305

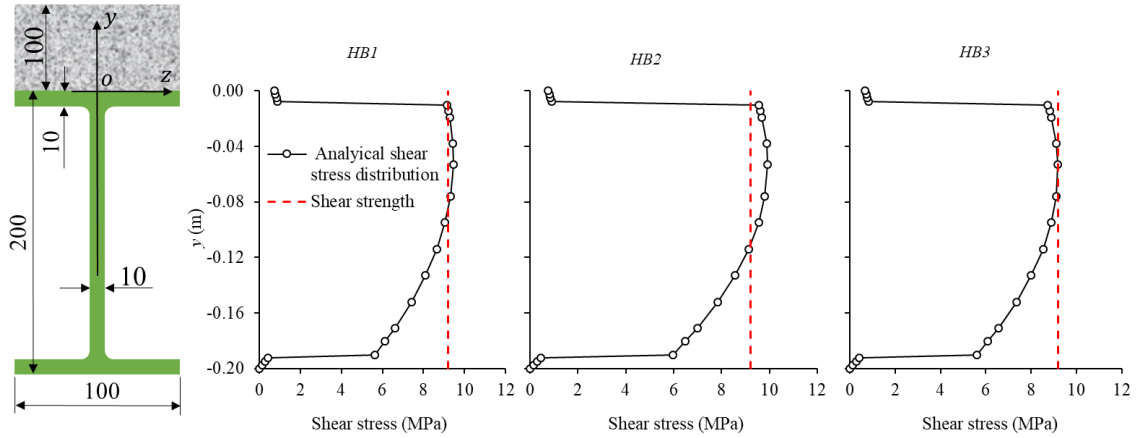
306 **Table 6.** Validation of shear stress in tested specimens with shear failure

Ref.	Specimen	$b_C \times h_C$ (mm×mm)	$h_F$ (mm)	$b_F$ (mm)	$t_{Flange}$ (mm)	$t_{web}$ (mm)	$p$ (mm)	Push-out specimen	$K$ (kN/mm)	$L$ (m)	$m_0$	$V_{test}$ (kN)	$S_{xy}$ (MPa)	$\tau_{max}$ (MPa)	$\frac{\tau_{max}}{S_{xy}}$	$\eta_F$	$\eta_{SD}$
This study	HB-1	100×100	200	100	10	10	140	P-HSB [8]	9.63	2.6	0.597	18.7	9.2	9.43	1.025	0.85	1.15
	HB-2	100×100	200	100	10	10	170		9.63	2.6	0.582	19.5	9.2	9.93	1.079	0.86	1.10
	HB-3	100×100	200	100	10	10	220		9.63	2.6	0.558	17.9	9.2	9.20	1.000	0.87	1.18
[8]	HB	730×60	150	100	10	7	120	P-SB-SIP [8]	*a	2.1	0.538	49.6	25.3	28.30	1.119	0.59	1.29
	HB-T	730×110	150	100	10	7	120		*a	2.1	0.302	74.8	25.3	19.66	0.777	0.25	2.03
	HB-R	730×60	150	100	10	7	120		*a	2.1	0.538	47.3	25.3	27.19	1.075	0.59	1.35
[5]	HB1	400×100	120	60	10	10	130	SCS2 [5]	20	4.0	0.585	91.0	47.1	39.98	0.849	0.55	1.87
	HB3	400×100	120	60	10	10	130	SCS3 [5]	12	1.8	0.316	148.1	47.1	67.87	1.441	0.48	1.47
	HB5	400×100	120	60	10	10	130	SCS6 [5]	*b	1.8	0.592	87.9	47.1	38.62	0.820	0.55	2.01
[12]	M1-HB3	400×50	120	6	8	8	300	M6 [12]	5.78*c	1.8	0.329	81.1	35.0	33.62	0.961	0.63	1.31
	M1-HB4	400×50	120	6	8	8	300		5.78*c	1.8	0.329	85.6	35.0	35.48	1.014	0.63	1.24
	M2-HB3	400×50	120	6	8	8	300		5.78*c	1.8	0.336	89.8	35.0	37.21	1.063	0.63	1.19
	M2-HB4	400×50	120	6	8	8	300		5.78*c	1.8	0.329	91.3	35.0	37.84	1.081	0.63	1.16
Average															1.023	0.63	1.41
CoV															0.162	0.27	0.24

307 \*a. Full composite action was employed in the specimens because SIP formwork was used and there was no slip at  
 308 the interface in [8].

309 \*b. Full composite action was ensured by using epoxy resin as connection SCS6 in [5].

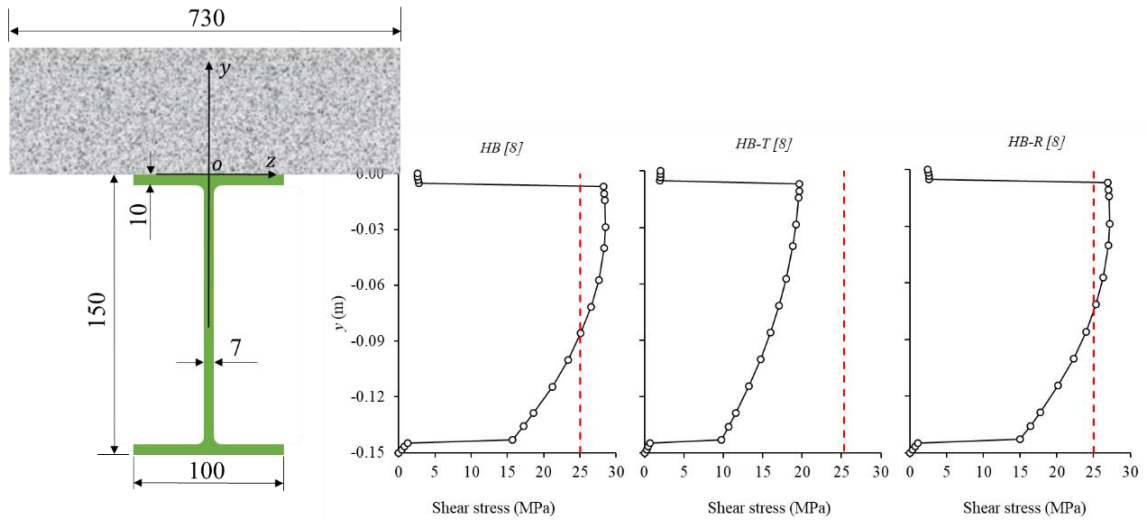
310 \*c. The value of  $K$  was assumed as 80% of M10 stud, because of lack of push-out test data for the studs.



311

312

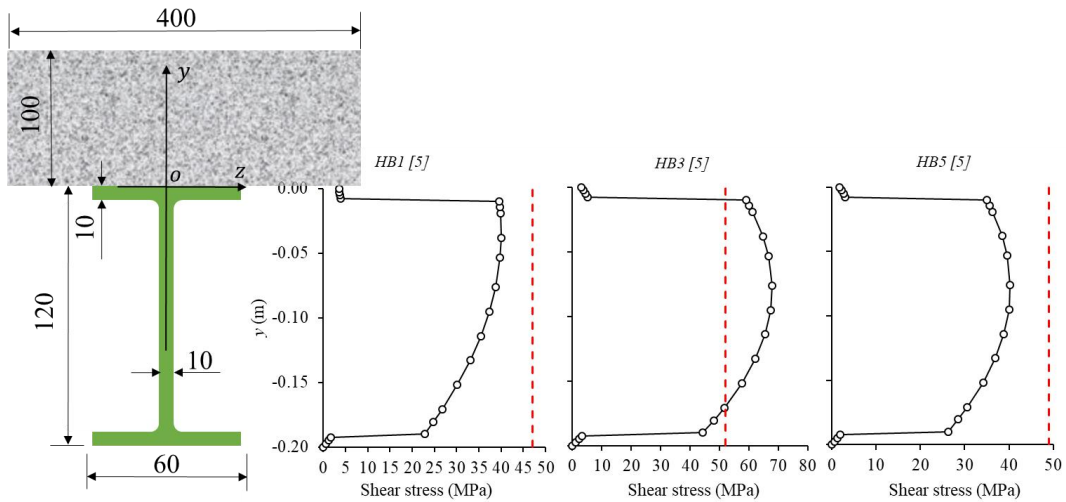
(a)



313

314

(b)

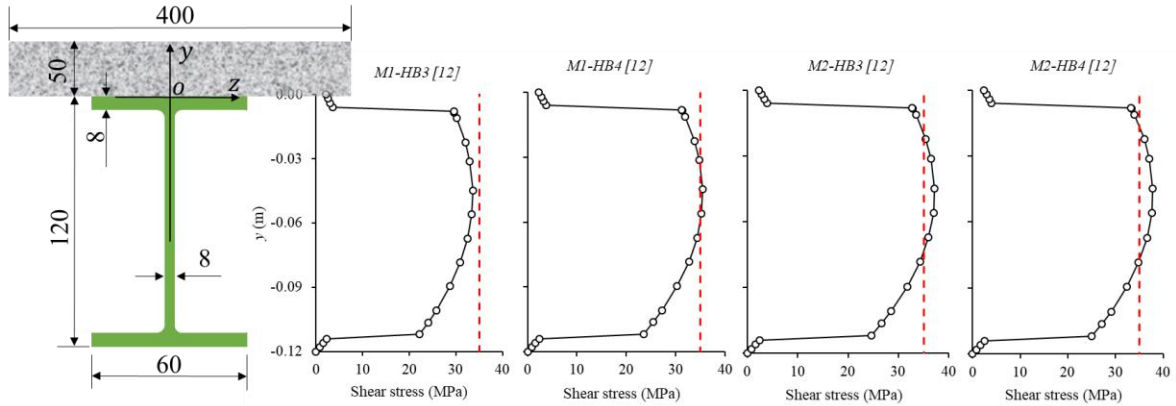


315

316

(c)





(d)

**Fig. 12.** Analytical shear stress distribution of FRP at failure load of specimens in: (a) the present study, (b) [8], (c) [5], and (d) [12]

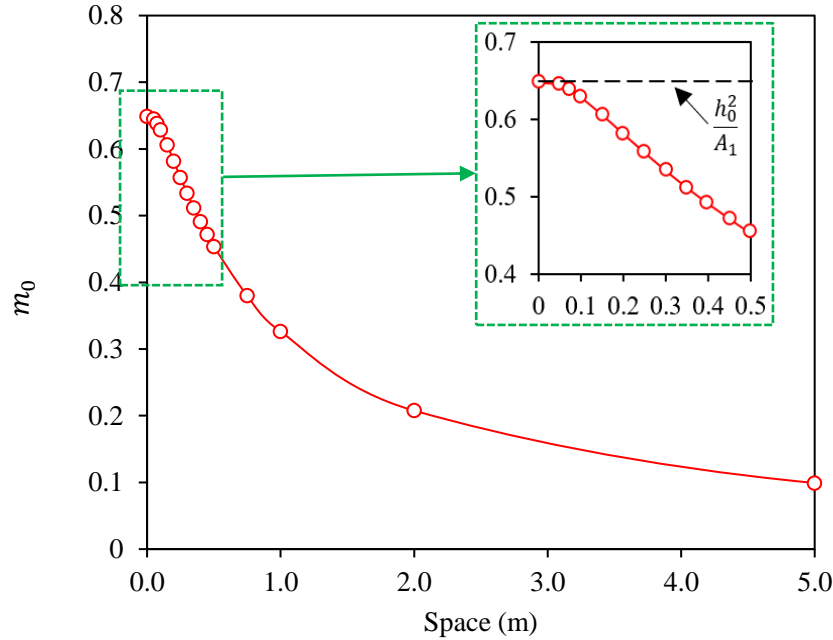
## 5. Discussions

Based on the formulae derived in Section 3, parametric studies are performed to understand the effects of key parameters on the shear behavior and discuss the composite actions. The investigated parameters include the space of adjacent connectors, the thickness of FRP web, longitudinal modulus of FRP, and thickness of the concrete slab.

### 5.1. Parametric study

The geometry and materials in specimens HB1 to HB3 are used as the control in the parametric study for a FRP-concrete composite deck:  $h_C = 100$  mm,  $h_F = 200$  mm,  $b_C = b_F = 100$  mm,  $t_{Flange} = t_{web} = 10$  mm,  $p = 200$  mm,  $K = 8$  kN/mm,  $L = 2.6$  m,  $E_{Fx} = 12.8$  GPa, and  $E_C = 29.5$  GPa.

Fig. 13 shows that as the space of adjacent connectors,  $p$ , increases from 0 to 5 m,  $m_0$  decreases from 0.65 to 0.10. At  $p = 0$ , the FRP-concrete composite deck has full composite action, resulting in  $m_0 = \frac{h_0^2}{A_1}$ . As  $p$  approaches to infinite, there is no composite action, and  $m_0$  decreases to 0. Thus, it is rational to use the ratio of  $m_0$  and  $\frac{h_0^2}{A_1}$  to characterize the degree of composite action of the composite sections: full composite action is represented by  $\frac{m_0}{(h_0^2/A_1)} = 1.0$ ; non-composite action is represented by  $\frac{m_0}{(h_0^2/A_1)} = 0$ .



335

336

**Fig. 13.** The relationship between the space of connector and  $m_0$ .

337

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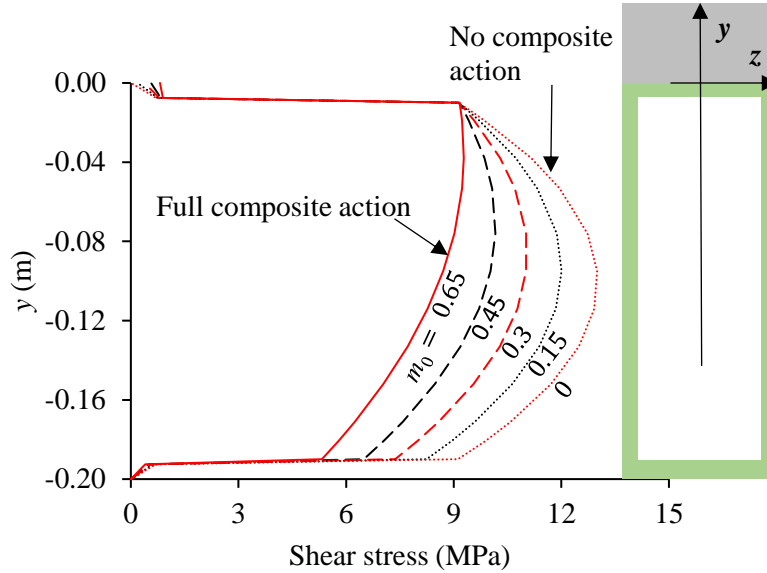
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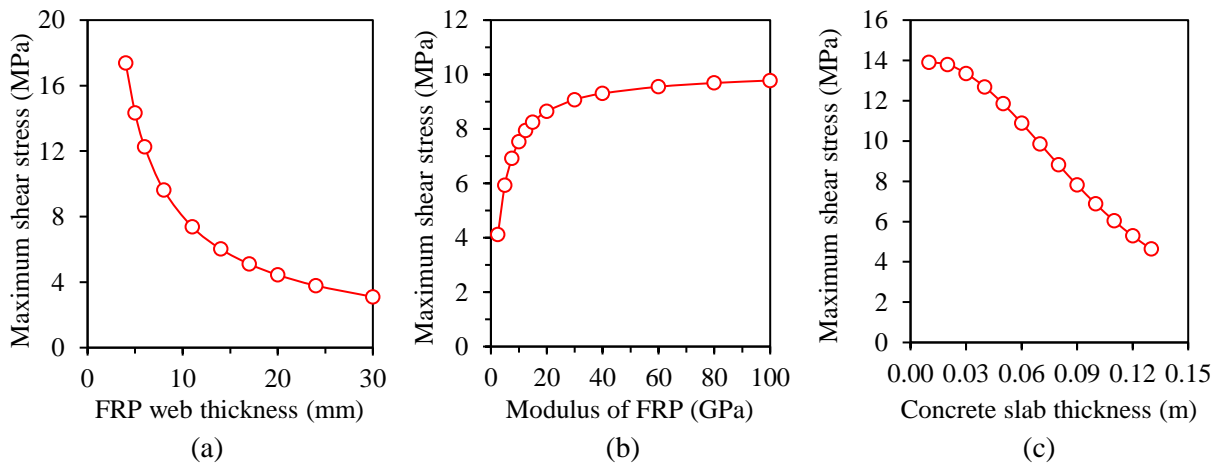
Fig. 14 shows that as  $m_0$  increases from 0 to  $h_0^2/A_1(=0.65)$ , the maximum shear stress decreases, and the neutral axis of the FRP moves from the center of the FRP web to the upper flange-web joint. For a beam with the same geometry and material properties, as the shear connection changes from non-composite action to full-composite action ( $\frac{m_0}{(h_0^2/A_1)}$  increases from 0 to 1), the maximum shear stress decreases from 12.9 MPa to 9.4 MPa. Therefore, the shear connection plays a significant role in the shear capacity of the FRP-concrete composite sections.



344

345 **Fig. 14.** Effect of composite action degree on the shear stresses in FRP-concrete composite section.

346 Fig. 15 shows the effects of the thickness of FRP web, longitudinal modulus of FRP, and thickness of  
 347 the concrete slab on the maximum shear stress. As the thickness of FRP web ( $t_{web}$ ) increases from 4 mm  
 348 to 30 mm, the maximum shear stress decreases from 17.4 MPa to 3.1 MPa (see Fig. 15a). As the longitudinal  
 349 modulus of FRP ( $E_{Fx}$ ) increases from 2.5 GPa to 100 GPa,  $\tau_{max}$  increases from 4.1 MPa to 9.8 MPa (see  
 350 Fig. 15b). As the thickness of the concrete slab ( $h_c$ ) increases from 0.01 m to 0.13 m, the maximum shear  
 351 stress decreases from 13.9 MPa to 4.6 MPa (see Fig. 15c).



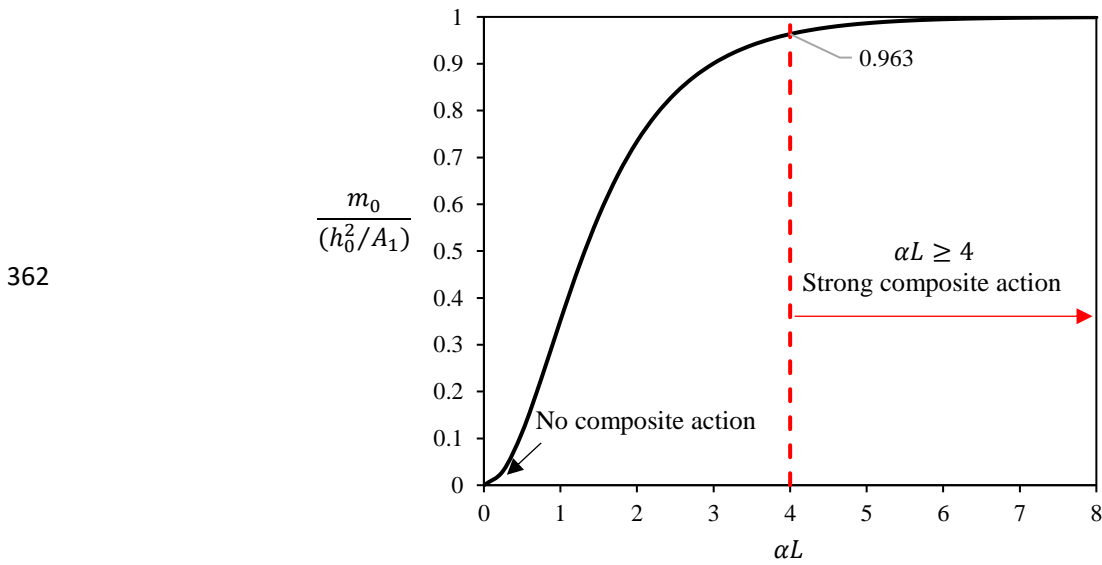
352

353 **Fig. 15.** Parametric study of the effect of (a) thickness of FRP web, (b) longitudinal modulus of FRP, and

354 (c) height of concrete slab on the maximum shear stress.

355 **5.2. Composite action**

356 Fig. 16 plots the relationship between  $\alpha L$  and  $\frac{m_0}{(h_0^2/A_1)}$  under three-point bending. With  $\alpha = 0$ , it can be  
 357 calculated that  $m_0 = 0$  and  $y_0 = -h_F/2$ , which means the neural axis locates in the center of the FRP  
 358 section. Previous tests showed that strong shear connections along the FRP-concrete interface were  
 359 obtained using adhesive-studs mixed connection [5], FRP shear keys [32], or perforated FRP ribs [24]. With  
 360 a high degree of composite action,  $\alpha L \geq 4$ , and  $\frac{m_0}{(h_0^2/A_1)} \geq 0.963$ . Since 0.963 is close to 1.0, the above  
 361 equations can be reconstructed by replacing  $m_0$  with  $m_{0,full}$  (see Table 5) when  $\alpha L \geq 4$ .



363 **Fig. 16.** The influence of the degree of composite action.

364 **6. Design Method**

365 At the supports, the shear forces carried by concrete and FRP are obtained by integrating the shear  
 366 stress in the height ( $y$ ) direction:

$$V_C = \int_0^{h_C} \tau_C(0, y_0) b_C dy = \frac{P}{2} \left[ (1 - m_0) \frac{I_C / \alpha_E}{I_0} + m_0 \frac{h_C}{h_C + h_F} \right] \quad (26a)$$

$$V_F = \int_{-h_F}^0 \tau_F(0, y_0) t(y) dy = \frac{P}{2} \left[ (1 - m_0) \frac{I_F}{I_0} + m_0 \frac{h_F}{h_C + h_F} \right] \quad (26b)$$

367 where  $b_C$  is the width of concrete. **It should be noted that the shear lag effect has been observed and**  
 368 **analyzed in steel-concrete composite sections where wider concrete slabs were used and higher stress**

369 level were reached, so an effective width was used instead of the whole width of concrete [33][34][35].  
 370 But in this study, effective width was not considered. Further studies about the shear lag effect of concrete  
 371 slab and FRP flange can be conducted, and the effective width can be used to replace  $b_c$  here.

372 Rewriting Eq. (26) gives the contributions of concrete and FRP girder:

$$V_C = \frac{P}{2}\eta_C \quad (27a)$$

$$V_F = \frac{P}{2}\eta_F \quad (27b)$$

373 where,  $\eta_C$  and  $\eta_F$  denote the contribution ratios of concrete and FRP, respectively ( $\eta_C + \eta_F=1$ ):

$$\eta_C = (1 - m_0) \frac{I_C/\alpha_E}{I_0} + m_0 \frac{h_C}{h_C + h_F} \quad (28a)$$

$$\eta_F = (1 - m_0) \frac{I_F}{I_0} + m_0 \frac{h_F}{h_C + h_F} \quad (28b)$$

374 Eqs. (27) and (28) indicate that the contributions of FRP and concrete depend on the degree of  
 375 composite action (related to  $m_0$ ) and the flexural rigidity ratio ( $\frac{I_C/\alpha_E}{I_0}$  or  $\frac{I_F}{I_0}$ ), assuming that the elastic  
 376 modulus and height ratio ( $\frac{h_C}{h_C+h_F}$  or  $\frac{h_F}{h_C+h_F}$ ) are constant. It should be noted that when thicker and wider  
 377 concrete slab was used, the concrete will crack under tensile stress, which may reduce the moment inertias  
 378 of concrete, see  $I_C$  in Eqs. (9) and (23a). So more test data for wider and thicker concrete slab are needed  
 379 to modify the shear capacity of concrete slab.

380 In  $I_F$ , the contribution of the FRP web can be neglected. Therefore, Eq. (27b) can be rewritten as:

$$\eta_F = (1 - m_0) \frac{1}{1 + \frac{b_c h_c^3}{24\alpha_E t_F b_F h_F^2}} + m_0 \frac{h_C}{H} = \frac{1 - m_0}{1 + \frac{1}{12\alpha_E \alpha_1 \alpha_2^2}} + \frac{m_0}{1 + \alpha_2} \quad (29)$$

381 where  $\alpha_1 = \frac{2t_F b_F}{b_c h_c}$ , which is the ratio of cross sectional area of FRP flanges over concrete;  $\alpha_2 = \frac{h_F}{h_c}$ , which  
 382 is the ratio of height of FRP girder over concrete;  $\eta_F$  can be used to evaluate the composite action between  
 383 FRP and concrete.

384 Eq. (29) shows that  $m_0$  and  $\alpha_2$  are the two main parameters that determine the contribution of FRP on

385 the shear capacity. The value of  $\eta_F$  using Eq. (27b) has an average value of 0.63, as shown in Table 5. In  
 386 this study,  $\eta_F$  is larger than 0.85, because the width of concrete is small; the average result of  $\eta_F$  is less than  
 387 0.63 for the rest of specimens in [5][12], because the section of concrete is wide compared with the FRP.

388 The design equation can be given by modifying Eq. (1):

$$V = \frac{1}{\eta} A_{web} S_{xy} \quad (30)$$

389 Herein, rewriting Eq. (30) gives:

$$\eta = \frac{A_{web} S_{xy}}{V} \quad (31)$$

390 Considering the ultimate state  $S_{xy} = \tau_{max}$ ,  $\eta$  is expressed as:

$$\eta = \frac{A_{web} \tau_{max}}{V} \quad (32)$$

391 Rewriting Eq. (32) gives:

$$\eta = \eta_F \frac{A_{web} \tau_{max}}{V_F} = \eta_F \frac{\tau_{max}}{\tau_{avg}} = \eta_F \eta_{SD} \quad (33)$$

392 where  $\tau_{avg} = V_F/A_{web}$ , which is the average shear stress of FRP web, and  $\eta_{SD} = \tau_{max}/\tau_{avg}$  is the ratio  
 393 of the maximum shear stress over the average shear stress.

394 It is interesting that Eq. (1) can be obtained from Eqs. (30) and (33) by enforcing:  $\eta_F = 1.0$  and  $\eta_{SD} = 1.0$ .  
 395 Similarly, Eq. (2) can be obtained by enforcing:  $\eta_F = 1.0$  and  $\eta_{SD} = 1.5$ . Eqs. (30) and (33) show that there  
 396 are two factors that affect the accuracy, which are the contribution of the concrete and the nonuniform  
 397 distribution of shear stress along the FRP profile.  $\eta_F$  can be quantified using Eq. (27b) or approximately by  
 398 Eq. (29). The value of  $\eta_{SD}$  mainly depends on the location of the neutral axis and the distribution of shear  
 399 stress. In order to get a design value for  $\eta_{SD}$ , the beams in Table 5 are used to inversely calibrate  $\eta_{SD}$ . To  
 400 be specific, the following equation can be used:

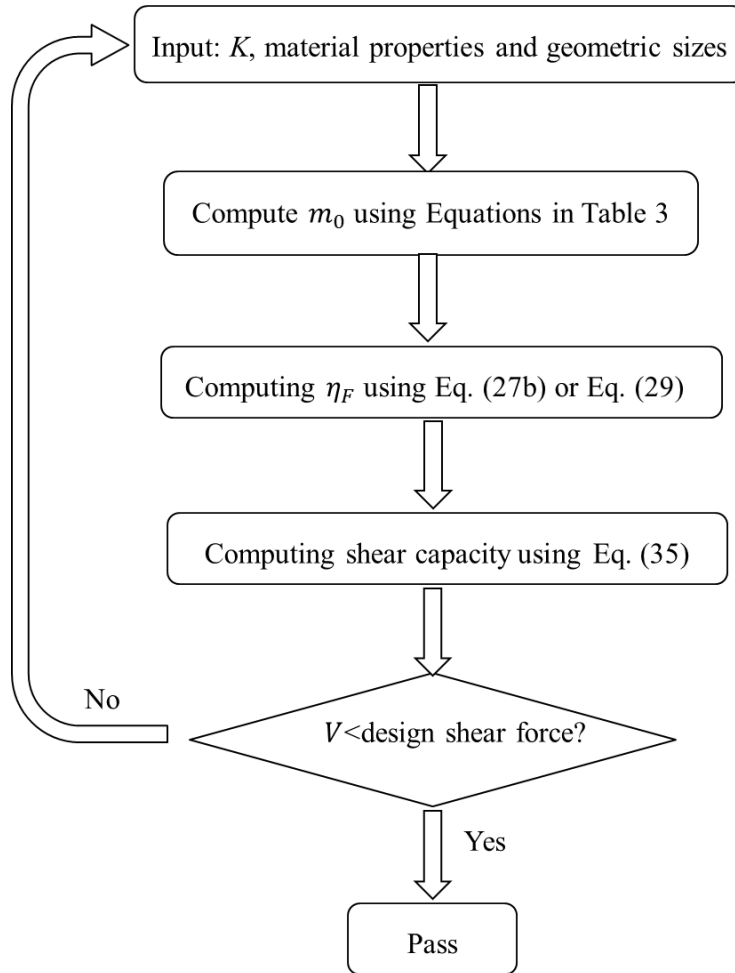
$$\eta_{SD} = \frac{\eta}{\eta_F} = \frac{A_{web} S_{xy}}{\eta_F V_{u.test}} \quad (34)$$

401 It can be seen that  $\eta_{SD}$  has an average value of 1.41, which is between 1.0 and 1.5 given by Eqs. (1)  
 402 and (2), respectively. Herein, it is suggested that  $\eta_{SD} = 1.41$  can be used for the design. Therefore, the final

403 design equation is given as:

$$V = \frac{1}{1.41\eta_F} A_{web} S_{xy} \quad (35)$$

404 However, since it remains unclear whether the value of 1.41 is suitable for all cases. Further research  
405 is needed to obtain more test data to determine  $\eta_{SD}$ . The design procedure can be depicted using Fig. 17.



406

407 **Fig. 17.** The procedure to design an FRP-concrete composite section with adequate shear capacity.

408

## 409 7. Conclusions

410 This study investigates the shear behaviors of FRP-concrete composite sections by experiments and  
411 analysis. Practical formulae were developed to predict the shear capacity of the composite sections. Based  
412 on the above experimental and analytical investigations, the following conclusions are drawn:

- 413 (i) The shear failure mode of FRP-concrete composite sections is brittle and characterized by the  
414 fracture along the horizontal direction at FRP webs or the upper web-flange joint.
- 415 (ii) When steel studs are used to connect the FRP and concrete, partial composite action is achieved,  
416 which yields to an increase of shear stress compared with full composite action scenario.
- 417 (iii) The partial interaction between FRP and concrete is modeled by considering slip effect and  
418 composite action degree that depends on the stiffness and spacing of the shear connectors. A  
419 closed-form equation for shear capacity of the composite sections is derived based on the  
420 maximum shear strength failure criterion of FRP webs.
- 421 (iv) The derived analytical equations can provide adequate predictions of the shear capacity and shear  
422 stress distributions in the FRP-concrete composite sections. Based on the parametric analysis, a  
423 simplified equation was derived for design.
- 424 (v) Parametric study shows that the shear capacity of the FRP-concrete composite sections is  
425 significantly affected by the characteristics of the shear connectors (size, slip stiffness, and  
426 spacing), the thickness of FRP web(s), and the thickness of concrete slab.

427 In the future, more tests are suggested to advance the understanding of the cracking of concrete slab  
428 when wider and thicker concrete slab was used. Thus possible modification can be made on the parameter  
429  $\eta_F$  in the proposed design equation. Also, effective width can be used for concrete slab and FRP flange  
430 when the shear lag effect is observed for larger or full-scale FRP-concrete hybrid sections.

431

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436

## 437 9. Declaration of interests

438 Declarations of interest: none.



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441

442 **11. CRediT author statement**

443 **Xingxing Zou:** Conceptualization, Methodology, Experimental test, Writing- Original draft  
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445 Reviewing and Editing. **Jingquan Wang:** Supervision, Funding acquisition, Laboratory work support,  
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447

448 **12. Data availability**

449 The raw data required to reproduce these findings cannot be shared at this time as the data is a part of  
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451

452 **13. References**

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