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# The hydro-mechanical interaction in novel polyurethane-bound pervious pavement by considering the saturation states in unbound granular base course

Lu, Guoyang; Wang, Haopeng; Zhang, Yuging; Liu, Pengfei; Wang, Dawei; Oeser, Markus; Grabe, Jürgen

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# The hydro-mechanical interaction in novel polyurethane-bound pervious pavement by considering the saturation states in the unbound granular base course

#### 4 Abstract.

Based on the recent development of novel polyurethane-bound pervious mixtures (PUPM), 5 the widespread application of fully permeable pavement (FPP) structures has become viable, 6 7 which entails significant environmental benefits for the transport infrastructure. However, the saturation state has a major influence on the performance and durability of FPP, especially on 8 9 the UGB material. The build-up and dissipation of pore-water pressure generated by intermit-10 tent dynamic vehicle loading is recognized as a critical factor influencing the bearing capacity of UGB layer. The majority of research on the FPP has focused on phenomenological ap-11 proaches, while the underlying mechanisms of hydro-mechanical interaction in UGB layer and 12 the influence on FPP structure are still mostly unclear. This study aims to characterize the 13 changes in dynamic response in FPP under various saturation conditions by considering the 14 15 hydro-mechanical interaction within UGB layer. To achieve this objective, a full-scale test track with a PUPM wearing course was designed and constructed. Pressures and water distri-16 bution were characterized from embedded sensors within different layers of test track when 17 18 subjected to the accelerating pavement test (APT). Additionally, based on the coupled stressdependent moisture-sensitive cross-anisotropic elastic (SMAE) model, the water distribution 19 within FPP structure and the dynamic response of UGB in the rainfall events were both char-20 acterized and solved by finite element modeling (FEM). The results predicted by the proposed 21 SAME model correspond to the field measurements. Based on the developed SAME model, 22 23 the distribution of water in the whole pavement structure was evaluated; also, the influence of the water content on the resilient modulus distribution within the UGB layer was analyzed. 24 Based on the predictions for the stress state of the UGB layer, sensitive analysis based on sur-25 26 face thickness was proposed.

- **Keywords:** Water content, Matric suction, Unsaturated flow, Hydro-mechanical interaction,
- 2 Polyurethane bound pervious material (PUPM).

#### 1 1 Introduction

To recover the natural hydrological cycle and restore the resilience regarding the risk of urban flooding, fully permeable pavements (FPP) are implemented by directly allowing the rainwater to seep through the pavement surface into the subgrade. This consequently relieves the urban drainage system and supports the natural hydrological cycle (Li, H. et al. 2012, Sun, W. et al. 2018).

Apart from the high hydraulic conductivity, the porous pavement can also make contribu-7 tions to the noise absorption in the transportation system (Ding, Y. and Wang, H. 2019, Cao, R. 8 9 et al. 2020). However, with a lower content of fine aggregate, the weak resistance of the pore structure to shear-stress leads to high susceptibility to grain raveling (Mo, L. et al. 2009, Zhang, 10 Y. and Leng, Z. 2017). Adhesion failure and short lifespans of porous mixtures have been the 11 12 main challenge, restricting the widespread application of FPP. The presented innovative poly-13 urethane (PU) bound permeable material was developed to gain highly favorable mechanical properties. The PU bound pervious material (PUPM) shows that the combination of high func-14 15 tionality and favorable mechanical properties can be achieved by replacing conventional binders with PU. High resistance to deformation and fatigue of PUPM were also observed in later 16 lab-research, which made it possible to promote the large-scale application of FPP (Lu, G. et 17 al. 2019a, Lu, G. et al. 2019b). 18

19 However, in the actual service environment, the porous pavement structures are mostly in 20 the unsaturated state with the filtration and the upward movement of moisture in sublayers and soil, where multi-physical processes occur, such as freezing and spalling, drying and shrinkage, 21 hydro diffusion and subsidence, capillarity and cracking (Wang, C.Y. and Cheng, P. 1997, Kha-22 lili, N. et al. 2014). Each one of these processes can result in complex effects which will lead 23 to significant influences on the pavement behavior. (Khalili, N. et al. 2004, Kettil, P. 2005). 24 The underlying mechanisms of the hydro-mechanical interaction between pore-water and the 25 solid skeleton, which dictates the structural behavior of FPP remain unknown. 26

FPP system including permeable surface, unbounded granular base (UGB) layer and subsoil must function under the stress of both water and traffic loading. Due to the high porosity and permeability of the pervious surface, water can quickly infiltrate through the surface layer and accumulate in the UGB layer. In which case, the UGB layer is more sensitive to moisture, which is one of the serious problems affecting the performance of the whole FPP structure (Gu, F. et al. 2014, Gu, F. et al. 2018).

7 Based on preliminary research, the failure on the fully permeable pavement (FPP) constructed with a PUPM surface is mainly caused by the failure in the unbound granular material 8 9 (UGB) in the substructure, which provides the foundational support to the surface layer and distributes the stresses (Lu, G. et al. 2020). In addition, a large number of studies have shown 10 that the UGB layer behavior is highly nonlinear and anisotropic, which makes the UGB layer 11 more complicated in the case of permeable pavement structures. In particular, hydro-mechani-12 cal interaction can significantly change the modulus of UGB, which in turn affect the service 13 life of FPP, and results in completely different mechanical distributions in the pavement layers. 14 Hence, a good understanding of the corresponding constitutive behavior of the UGB under the 15 influence of moisture is vital for the design of permeable pavements and the analysis of the 16 mechanical response. Recently, several successful constitutive models have been established 17 for UGB based on the cross-anisotropic and nonlinear behavior (Zhang, Y. et al. 2018, Gu, F. 18 et al. 2018). Simulations which included the meso-scale mechanism of anisotropy in granular 19 materials corresponded very well with the laboratory test results (Zhang, J. et al. 2018, Gu, F. 20 et al. 2014). However, due to the lack of systematical, large scale experimental investigation of 21 the mechanical and hydraulic properties in the pavement, the coupled models remain to be fully 22 validated. 23

To further investigate the vehicle loading response of FPP with the novel PUPM, a full-scale test track was constructed with a series of embedded sensors including total pressure sensors, pore pressure sensors and water content meters. With the aid of accelerating the pavement test (APT), the dynamic responses of the permeable pavement were studied. The water distribution
mechanism in the FPP structure during a rainfall event was characterized by the unsaturated
flow model. Additionally, based on the modified hydro-mechanical model, FEM simulations
were conducted under different saturation states. The basic recommendation of optimizing FPP
structural design under heavy traffic loading has been eventually suggested.

6 2 Materials and experimental setup

## 7 2.1 Materials and test track

Previous studies have demonstrated the excellent performance of polyurethane bound pervious mixtures (PUPM) with respect to its mechanical and functional performance compared to conventional porous asphalt mixtures (Lu, G. et al. 2019a). In the present research, PUPM was selected as the permeable surface material. Unbound granular materials, Schottertragschicht (STS) 0/45mm and Frostschutzschicht (FSS) 0/63mm, were utilized for constructing the UGB and subgrade layer of the test track respectively. The gradations of the materials applied in the test track are given in Figure 1.





the previous study (Lu, G. et al. 2019a and Lu, G. et al. 2019b ). The PUPM used in the laboratory and the test track contained 6 % PU binder and achieved an air void content of 28 %; the construction process is shown in Figure 2. Before mixing with the aggregate, the two components (Polyol and Isocyanate) of the binder must be fully mixed around 2 minutes to ensure the full polymerization. The mixing process of PU binder and aggregates needs to be kept within 5 minutes, and the paving and compaction process needs to be completed within 25-30 minutes.



Figure 2. The preparation process of the PUPM pavement surface: (a) The mixing of polyurethane binder; (b) The mixing process of aggregate and PU binder; (c), (d)and (e) The paving
and compaction process of PUPM layer; (f) Paved test track;

# 10 2.2 The multi-physical measurement system

- 11 To monitor the service performance of the FPP, sensors were instrumented in all five layers,
- 12 included total pressure sensor, pore-water pressure sensor, temperature sensor, and volumetric
- 13 water content sensor. The location of the instruments and their technical properties are listed in
- 14 Figure 3 and Table 1 respectively. All sensors were strictly controlled to be level with the road
- 15 surface and exactly under the wheel loading path.





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#### Table 1 The technical data of sensors

Number	Sensor	Name	Model	Measurement Range	Accuracy	
1		Tensiometer T4 +1000 hPa to -85 hPa		+1000 hPa to -850 hPa	$\pm 5$ hPa	
2		Pore air pressure sensors	ore air pressure sensorsDPM 321100 mbar to 600bar -25 °C to 85 °C		< ±0.25% FSO	
3	S S	Earth pressure/ temperature cell	E 20/30 AU 20T Type C	0 to 20 bars -25 °C to 60 °C	< 0.5% < 0.5%/ °C	
4	X	Soil moisture sensor	GS1	0 to 57% VWC	$\pm 0.03 \text{ m}^3/\text{m}^3$	

## 6 2.3 Accelerated pavement testing

To gain a deeper understanding of the hydro-mechanical behavior of the pavement and the 7 impacts of saturated and partially saturated conditions on the stability of the structure, an ac-8 celerated pavement testing (APT) was performed on the test track (Figure 4, a). The greatest 9 advantage of APT is the ability to use maintain constant speeds, ensure a regular wheel path 10 and the large number of axle load repetitions in short periods (Liu, P. et al. 2017). In collabo-11 ration with the Bundesanstalt für Straßenwesen (BASt), the Mobile Load Simulator MLS30 12 was operated on the test track at the RWTH Aachen University as shown in Figure 4. The 13 MLS30 can simulate wheel loads between 40 and 75 kN through 4 bogie-mounted wheels 14 moving in a continuous circular motion within the device (Figure 4, b). The tire pressure is set 15

to 0.85 MPa while the speed of the bogies can be varied between 7 and 22 km/h, allowing for 1 load repetitions between 2000 and 6000 per hour. Apart from the ability to accurately study the 2 hydro-mechanical behavior of the unbound layers and the evolution of undesirable accumu-3 lated pore pressure, the high loading rate of the MLS30 allows for an accurate evaluation of 4 the expected service life. The APT test was carried out on the test track for two different satu-5 ration states: (a) dry or lower saturated state: no external water added into the test track with -6 7 0.67 m water level; (b) saturated state or high saturated state: the test track was fully saturated by pouring water through the pavement surface, after one day relaxing a steady water level of 8 9 -0.26 m was measured). Three different velocities were used for each saturation state, namely 7km/h, 14km/h and 22km/h. Each speed was set total 20.000 daily axle passages. 10

11



- Figure 4 (a) The APT test based on MLS30; (b) A schematic diagram of FPP in two different saturation states
- 15 **3** Theoretical background

# 16 **3.1 Unsaturated flow model through the pervious pavement**

In most circumstances, the permeable pavement is in a partially saturated state. The pores in the unsaturated zone are filled with water as well as air; matric suction is also active in the area. A gradient in the hydrological head leads to the flow of water. More specifically, the difference in matric potential causes water to flow towards the unsaturated area (Fredlund, D.G. et al. 1993). The Richards equation has been widely adopted to analyze water flow under unsaturated conditions (Hall, C. 1977; Van Genuchten, M.T. 1980):

$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial x} \left[ K(h) \frac{\partial h}{\partial x} \right] + \frac{\partial}{\partial z} \left[ K(h) \frac{\partial h}{\partial z} \right] + \frac{\partial K(h)}{\partial z}$$
Eq. 1

1 Where, z is the vertical coordinate along with the pavement depth [m], x is the horizontal 2 coordinate along the wheel path [m], t = time [s],  $\theta$  is the volumetric water content, K is the 3 permeability [m/s], and h denotes the hydraulic head [m].

Studies on water flow in the unsaturated zones have shown that the volumetric water content,
the permeability and the matric suction are interconnected (i.e., volumetric water content and
hydraulic conductivity can both be formulated as a function of the matric suction) (Celia, M.A.
et al. 1990; Gray, W.G. and Hassanizadeh, S.M. 1991).

### 8 **3.1.1 Soil Water Characteristic Curves**

In unsaturated porous media, the Soil Water Characteristic Curves (SWCC) describes the 9 10 relationship between matric suction and saturation and plays a significant role in predicting the 11 hydraulic as well as the mechanical properties of porous material. Empirical models to describe the water retention properties of porous material were mainly presented by Brooks and Corey 12 (Brooks, R. and Corey, T. 1964), van Genuchten (Van Genuchten, M.T. 1980), and Fredlund 13 and Xing (Fredlund and Xing, 1994). Based on the research conducted previously (Törzs, T. et 14 al. 2019), the van Genuchten model for water characterization was selected in this research for 15 16 the porous pavement material. In Eq. 2,  $\alpha_{VG}$ ,  $m_{VG}$  and  $n_{VG}$  are constants in the constitutive equation. For the determination of the parameter m<sub>VG</sub>, the simplified approach by Mualem 17 (Mualem, Y. 1977) was selected, see Eq. 3. 18

$$S_{e}(s) = \frac{1}{(1 + (\alpha_{VG}s)^{n_{VG}})^{m_{VG}}}$$
 Eq. 2

$$m_{VG} = 1 - \frac{1}{n_{VG}}$$
 Eq. 3

19 The term of effective saturation,  $S_e$  is mainly used in the present study, which was defined 20 in terms of the actual saturation,  $S_r$ :

$$S_{e} = \frac{S_{r} - S_{r,res}}{S_{r,max} - S_{r,res}}$$
Eq. 4

Where, S<sub>r,res</sub> is the actual-residual saturation and S<sub>r,max</sub> is the actual-maximum saturation
 under fully saturated condition.

#### **3 3.1.2 Models for the unsaturated hydraulic conductivity**

Pore structure characteristics are usually used to estimate the permeability K in porous media. 4 Most existing models are based on the pore characteristics in terms of grain size distribution 5 (GSD) or other measured indices. Because different pore indices regarding the pore structure, 6 7 pore shape factor and tortuosity are very difficult to measure, this modeling approach is often 8 based on a number of assumptions; in contrast, the model based on the GSD is more convenient 9 and allows for empirical refinement. Two famous approaches for predicting the permeability (K) based on the GSD are the Hazan equation and the Kozeny-Carman Model (KCM). Contrary 10 11 to the Hazan model based on the effective aggregate diameter, the KCM considers the entire GSD, the void ratio as well as the shape factor to predict K. The accuracy of the KCM was 12 observed to surpasses that of the Hazan equation (Carrier III, W.D. 2003). As a result, the KCM 13 has become widely adopted for modelling the hydraulic conductivity in porous materials and 14 pavements (Oeser, M. et al. 2012). For the pervious pavement materials, the modified KCM 15 model developed in previous research (Lu, G. et al. 2020a) was adopted to derive the unsatu-16 rated flow model: 17

$$K_{\text{KCM}}^{\text{m}} = \frac{\gamma_{\text{w}}}{\mu_{\text{w}} \cdot C_{\text{k-c}}} \cdot \frac{n_{\text{e}}}{\tau^2 S_{\text{Ae}}^2}$$
Eq. 4

18 Where,  $\mu_W$  denotes the viscosity of water, which is approximately  $1 \times 10^{-6}$  KPa s at 20°C; 19  $\gamma_W$  represents the unit weight of water, which is 9810 N/m<sup>3</sup>;  $C_{K-C}$  is the empirical Kozeny– 20 Carman coefficient for which a value of 5 is suggested. For the pore characteristics,  $n_e$  repre-21 sents for effective porosity,  $\tau$  denotes to tortuosity while  $S_{Ae}$  is specific surface area. Most previous 22 studies on the hydraulic conductivity of porous material are conducted for saturated flow within 1 individual fields. From the semi-empirical relationship firstly proposed by Brooks & Corey,

2 the permeability of partially saturated materials can be described as follows:

$$K_{W} = K_{E} \cdot S_{e}^{\left[\frac{2+3\lambda_{p}}{\lambda_{p}}\right]}$$
Eq. 5

In Eq. 5,  $K_E$  denotes to the permeability of porous media for water tested under normal laboratory testing standards and  $\lambda_p$  gives the value of the pore-size distribution index determined as the average slope of the SWCC in this research. Similarly, the unsaturated permeability of the air phase can be presented in the following equation:

$$K_{A} = K_{E} \cdot (1 - S_{e})^{2} \left( 1 - S_{e}^{\left[\frac{2+3\lambda_{p}}{\lambda_{p}}\right]} \right)$$
Eq. 6

By substituting  $K_E$  with  $K_{KCM}^m$  from the KCM model, the partial permeability of both phases can be directly derived from the grain size distribution. Hence, the modified unsaturated permeability model for the water and the air phase can be written as shown in Eq. 7 and Eq. 8:

$$K_{W}^{m} = K_{KCM}^{m} \cdot S_{e}^{\left[\frac{2+3\lambda_{p}}{\lambda_{p}}\right]}$$
Eq. 7

$$K_{A}^{m} = K_{KCM}^{m} \cdot (1 - S_{e})^{2} \left( 1 - S_{e}^{\left[\frac{2 + \lambda_{p}}{\lambda_{p}}\right]} \right)$$
Eq. 8

# 10 **3.2** The constitutive model for pervious pavement material

#### 11 **3.2.1** The Resilient Modulus Model for UGB

The resilient modulus of unbound aggregates has been widely recognized as the primary mechanical property of the base course required in the mechanistic-empirical design of pavement structures. In order to determine the resilient modulus of unbound aggregates, various models have been developed (Uzan, J. 1985).

Among these, the most recognized one is the generalized model as follow (Zhang, Y. et al.
2018):

$$E_{Z} = k_{1} P_{atm} \left(\frac{I_{1}}{P_{atm}}\right)^{k_{2}} \left(\frac{\tau_{oct}}{P_{atm}}\right)^{k_{3}}$$
Eq. 9

1 where  $I_1$  represents the first invariant of the stress tensor;  $\tau_{oct}$  stands for the octahedral shear 2 stress;  $P_{atm}$  is the atmospheric pressure; and  $k_1$ ,  $k_2$ , and  $k_3$  are regression coefficients.

3 **3.2.2** Cross-anisotropy of UGB material

It has been widely researched and proven that the cross–anisotropic model of UGB should be considered in the numerical investigation of pavement performance under consideration of nonlinear material (Tutumluer, E. and Thompson, M.R., 1997, Adu-Osei, A.et al. 2001, Zhang, Y. et al. 2018). Cross-anisotropy means that material properties are different between the horizontal and vertical planes while the material properties remain the same in the horizontal plane. Eq. 10 and 11 were employed for characterizing the cross-anisotropic properties of the UGB layer in FPP systems.

$$\begin{split} \sigma_{ij}' &= \begin{bmatrix} \sigma_{xx}' \\ \sigma_{yy}' \\ \sigma_{zz}' \\ \sigma_{yy}' \\ \sigma_{yz}' \\ \sigma_{yz}' \\ \sigma_{zx}'' \end{bmatrix} = \frac{E_z}{\alpha_0 \beta_0} \begin{bmatrix} n(1 - nv_{2x}^2) & n(v_{xy} - nv_{2x}^2) & nv_{zx} \alpha_0 & 0 & 0 & 0 \\ n(v_{xy} - nv_{2x}^2) & n(1 - nv_{2y}^2) & nv_{zx} \alpha_0 & 0 & 0 & 0 \\ n(1 - nv_{2y}^2) & n(1 - nv_{2y}^2) & 1 - nv_{2y}^2 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{2} n\beta_0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & m\alpha_0 \beta_0 & 0 \\ 0 & 0 & 0 & 0 & 0 & m\alpha_0 \beta_0 & 0 \\ 0 & 0 & 0 & 0 & 0 & m\alpha_0 \beta_0 \end{bmatrix} \begin{bmatrix} \varepsilon_{xx} \\ \varepsilon_{yy} \\ \varepsilon_{zx} \\ \varepsilon_{zx} \\ \varepsilon_{zx} \end{bmatrix} \\ Eq. 11 \\ m &= \frac{E_x}{E_z} \\ \alpha_0 &= 1 + v_{xy} \\ \beta_0 &= 1 - v_{xy} - 2nv_{zx}^2 \end{split}$$

11 Where,  $G_{ZX}$  is shear modulus in the vertical plane,  $E_Z$  is the resilient modulus in the vertical 12 plane,  $E_x$  is the resilient modulus in the horizontal plane,  $v_{zy}$  and  $v_{zx}$  represent Poisson's ratio 13 in the vertical and horizontal planes respectively.

# 14 **3.2.3** The hydro-mechanical constitutive model for pervious pavement material

Fundamentally, permeable pavements can be considered as a three-phase material containing solids, moisture and gas, especially when the pavement is in an unsaturated state. It must be addressed that, when vehicles traverse the pavement, the generation and dissipation of pore pressure in the water and air phases play a critical role in the failure mechanisms of permeable
 pavement (Alobaidi, I. and Hoare, D.J. 1996).

3 Based on this, the effective stress concept was developed to determine the strength of the unsaturated materials by considering the pore pressures (Loret, B. and Khalili, N. 2002). In its 4 mathematical formulation, Terzaghi's effective stress  $\sigma'$ , is defined as the difference between 5 6 the total stress and pore-water pressures. One of the most renowned modified effective stress concepts is generally attributed to the approach established by Bishop (Bishop, A.W. 1954), 7 where the effective stress can be rewritten as shown in Eq. 12, with the introduction of the 8 effective stress parameter  $\chi$ , which governs the interaction between the solid and the liquid 9 phase. 10

$$\sigma' = \sigma - \chi s = \sigma - \chi (P_a - P_w)$$
 Eq. 12

11 Wherein the effective stress parameter can be defined as following:

$$\chi = \begin{cases} 1 & s_e \ge s \\ \left(\frac{s_e}{s}\right)^{\Omega} & s_e < s \end{cases}$$
 Eq. 13

Ω is determined as 0.55 in the current research based on empirical regression (Oeser, M. et
 al. 2012). To incorporate the moisture-dependent properties of UGB's resilient modulus, a new
 constitutive model can be derived based on the effective stress:

$$E_{z}^{m} = k_{1}P_{atm} \left(\frac{I_{1} - 3\chi s}{P_{atm}}\right)^{k_{2}} \left(\frac{\tau_{oct}}{P_{atm}}\right)^{k_{3}}$$
Eq. 14

By coupling Eq. 1, 9, 10 and 14, the Stress-dependent moisture-sensitive cross-anisotropic elastic (SMAE) model was derived and is proposed to investigate the hydro-mechanical interaction in the permeable pavement.

# 4 The Finite Element Modeling of FPP considering the hydro-mechanical interaction

- 20 4.1 The development of the FEM for FPP
- 21 Weak form based FEM in COMSOL program

A number of researches have modeled asphalt concrete behavior by using the weak-form 1 techniques differential equation (PDE)-based FEM partial in the COMSOL 2 MULTIPHYSICS® program (Liu, Z. and Yu, X., 2014, Zhang, Y. et al. 2015, Zhang, J. et al. 3 2018, Luo, X. et al. 2020). The weak-form PDE-FEM has been found to have advantages when 4 solving various coupling problems with interdependent variables regarding the model inputs 5 and the dependent variables. Modeling a UGB material with a SMAE modulus is a complex 6 7 coupling process that includes an interdependence between modulus, stress, deformation and saturation. However, the interdependence can be solved by creating additional dependent var-8 9 iables in the weak-form PDE FEM to define the SMAE model. Unlike using Abaqus, there is no need for this method to program any material subroutine. In this study, the authors model 10 the permeable pavement based on the PDE-FEM. 11

# 12 Load and Boundary Conditions.

The pavement structure with the APT test was modeled in COMSOL MULTIPHYSICS® as 13 shown in Figure 5. Based on the dimensions of the test track and the in-situ loading section, 14 the simulated structure was created with a length of 3500 mm. The three layers were modeled 15 with the following thickness: 100 mm PUPM surface, 300 mm UGB layer and 500 mm sub-16 grade layer. The purpose of the experiment design was to control the water content in the entire 17 pavement structure. In the actual test, the side and bottom of the pavement were sealed by a 18 waterproof membrane. Correspondingly, in the simulation, the design rainfall event can only 19 be applied from the surface layer and is retained in the pavement structure. 20

Corresponding to the APT test, a traveling tire patch with a uniform vehicle contact stress of 350 kPa was applied on the PUPM surface on a 150 mm wide loading area with a maximum speed of 22 km/h. The loads were simplified as uniform vertical loads. The loading speed was defined with the square wave function Rect() and the analytic function Pulse(X) = Rect (X – Loadspped \* t) of the applied loads and coordinate, which re already embedded in the COMSOL software.



Figure 5 The FEM model of FPP based on PUPM layer

## 3 **4.2** Determination of the model parameters

In the present research, the modeling of unsaturated flow included the van Genuchten prediction of SWCC, the modified KC permeability model as well as the Richard flow model for unsaturated flow. The parameters of the SWCC model were derived based on the measurements from a hanging water column apparatus in accordance with ASTM D6836-16. The saturated and unsaturated flow model, used in the current model was also validated in the previous research based on permeability results from the laboratory (Oeser, M. et al. 2012, Törzs, T. et al. 2019). Table 2 lists the key parameters of unsaturated flow modeling.



1

2

Table 2. Unsaturated flow parameters used in the finite element modeling

Materials	$\gamma_W$ (N/m <sup>3</sup> )		S <sub>r,max</sub> (-)	<i>S<sub>r,res</sub></i> (-)	$lpha_{VG}$ $(1/m)$	<i>m<sub>VG</sub></i> (-)	n <sub>VG</sub> (-)
PUPM Layer	9810	10 <sup>-3</sup>	0.295	0.011	4.255	0.82	5.54
UGB Layer	9810	$10^{-3}$	0.252	0.020	8.102	0.4	1.66
Subgrade soil layer	9810	10 <sup>-3</sup>	0.186	0.048	0.226	0.17	1.20

Different constitutive material models, i.e., Linear Isotropic Elastic (LIE) model, Linear Cross-anisotropic Elastic (LAE) model, Stress-dependent Cross-anisotropic Elastic (SAE) model and Stress-dependent Moisture-sensitive cross-Anisotropic Elastic (SMAE) model, were all taken into account and evaluated in finite element simulations. Table 3 lists the parameters required for these constitutive material models. The PUPM was modeled as an elastic

1	material, and its elastic modulus was obtained from the uniaxial compression test documented
2	in the previous study (Lu, G. et al. 2019). Crushed graywacke aggregates were used to construct
3	the UGB layer, which has a maximum dry density of $2.15 \times 10^3 kg/m^3$ and an optimum water
4	content of 7.3%. The non-linear and cross-anisotropic parameters of UGB material can be
5	obtained by conducting repeated load triaxial tests at different stress levels. In the current study,
6	the values of modeling parameters for UGB were adopted based on the previous research,
7	which corresponds to the medium resilient modulus of the base material (Zhang, Y. et al. 2019).
8	Based on the average vertical modulus value predicted by SAE, 110 MPa was selected as the
9	constant vertical modulus of LAE and LIE. The subgrade was also predicted as an elastic ma-
10	terial ( with maximum dry density of $2.17 \times 10^3 kg/m^3$ and optimum water content 7.8%).
11	The elastic modulus of subgrade was estimated from the California bearing ratio tests (ASTM
12	D1883-14) based on the empirical equation $E = 2.55 \times CBR^{0.64}$ abording to APA 2004. The
13	finite element modeling was then conducted using the commercial COMSOL
14	MULTIPHYSICS® software.

15

Table 3. Material parameters used in the finite element modeling.

Materials	k <sub>1</sub>	k2	k3	n	m	V <sub>ZX</sub>	Vxy
PUPM Layer	E <sub>1</sub> = 3.31GPa; v <sub>1</sub> =0.16						
UGB-SMAE	1281	0.81	-0.08	0.45	0.35	0.38	0.43
UGB-SAE	1281	0.81	-0.08	0.45	0.35	0.38	0.43
UGB-LAE	Ez= 110 MPa			0.45	0.35	0.38	0.43
UGB-LIE	Ez= 110 MPa						
Subgrade soil layer	er $E_3 = 69 \text{ MPa}; v_3 = 0.4$						

Notes:  $E_1$  and  $E_3$  are elastic modulus values of the PUPM layer and the natural subgrade soil layer, respectively;  $v_1$  and  $v_3$  represent the Poisson's ratios of the PUPM surface layer and the natural subgrade soil layer. Ez is the vertical modulus of the UGB layer.  $k_1$ ,  $k_2$ ,  $k_3$ ,  $V_{zx}$ ,  $V_{xy}$  are the nonlinear and cross-anisotropic parameters of SAME, SAE and LAE, the value of which were selected based on the previous study (Zhang, Y. et al. 2019).

# 21 5 Results and Analysis

# 22 5.1 Multi-physical monitoring of pervious pavement

23 Figure 6 shows the responses in terms of total vertical stresses and pore-water pressures for

the load cases (low saturation state and high saturation state, respectively), considering a tire

speed of 7 and 22 km/h. Contrary to the observations in previous truck passages experiments 1 (Lu, G. et al. 2020b), no pumping effect was observed in the lower layers as a result of accu-2 mulated pore-pressures. However, the magnitudes of the variation in vertical stress and pore-3 pressure were considerably higher, especially for the UGB layers. As can be seen in Figure 6, 4 both vertical stress and pore water pressures increase as the saturation increases. When com-5 paring the low saturation state and the high saturation state, it was found that large discrepan-6 7 cies were observed: more than 50kPa and 10kPa for the vertical stress and the pore water pressure of UGB layer, respectively. 8

9 Due to the high porosity and permeability of the PUPM layer, the pore water pressure in the surface layer was nearly zero. When comparing to the high stiffness of PUPM, the impact of 10 pore-water pressure can be neglected (Lu, G. et al. 2019a). However, high stresses and defor-11 mation in the unbound base layers may lead to the formation of growing cavities between the 12 bound and unbound layers below the loading area, leading to failure. The causes for the signif-13 icant deformations may be attributed to the damage mechanisms which are accelerated by the 14 presence of water and the high loads transferred to the unbound layers through the rather thin 15 surface layer. Hence, the detailed investigation of the behavior of unbound granular material in 16 terms of hydro-mechanical interaction is crucial to the long-term performance and design of 17 pervious pavement structures. Based on different loading speeds and pavement saturations, the 18 development of temperature within the pavement was also recorded (Figure 6, c & d) 19









(c)



Figure 6 Field measurement of vertical stress and pore-water pressure subjected to one loading process of the APT test: (a) Dry state (Low saturated state); (b) Saturated state (High saturated state); (c) pavement temperature of the dry state; (d) pavement temperature of the saturated states (The air temperature of the day was approximate 2-6 °C).

#### **5.2** The unsaturated flow modeling for pervious pavement material

2 To achieve the designed permeability, the maximum design rainfall event of  $270 \, \text{l/}$  (s·ha) (l=liter, s=second and ha=hectare) was determined based on the previous laboratory column 3 irrigation test (Lu, G. et al. 2020b). The rainfall of 0.7h duration was applied to the pervious 4 5 surface. Figure 7 presents the effective saturation distribution in the entire FPP structure in terms of different watering durations. Due to the permeability levels of different layers 6  $(H_{PUPM} > H_{UGB} > H_{subgrade})$  in the test track, rain water quickly saturated the PUPM layer 7 from the bottom at the beginning of a rainfall event. After 0.4h of irrigation, the PUPM layer 8 was nearly fully saturated with an average effective saturation of 92.80% (Figure 7, a). In the 9 UGB layer, saturation developed from top to bottom. In the beginning of the irrigation event, 10 less water infiltrated into UGB layer, with most of rainwater accumulating in the interface be-11 tween the PUPM and the UGB. However, the infiltration rate increased after the PUPM layer 12 was saturated. In this case, the water infiltrating into the UGB layer is not only driven by gravity 13 14 but also by the hydraulic head in the PUPM layer (Figure 7, b). After 0.7h of irrigation, both PUPM and UGB layers are nearly fully saturated, where water cannot infiltrate into the subsoil 15 due to the very low hydraulic conductivity in a well-compacted subsoil layer. Once this stage 16 17 is reached, additional rainwater will not directly enter the pavement structure but only accumulate on the road surface (Figure 7, c). The process of saturation in the subgrade is very slow. 18 Around one hour after the rainfall event is completed, this process exhibits significant changes. 19 After about 2.3 hours, the irrigation is stopped and only a significant downward movement of 20 rainwater in the pavement structure can be observed (Figure 7, d). This phenomenon corre-21 sponds to the observations during the experimental process and was selected for the further 22 23 simulation of the hydro-mechanical interaction.

The results of the simulated water content distribution are very close to the state of the water distribution in the actual experiment, as can be seen from the measured volumetric water content in Figure 8.



Figure 7 The effective saturation distribution based on unsaturated flow modeling: (a) The effective saturation distribution after 0.2-hour rainfall; (b) The effective saturation distribution after 0.4-hour rainfall; (c) The effective saturation distribution after 0.7-hour rainfall; (d) The effective saturation distribution after 3- hour rainfall (0.7h rainfall event +2.3h rest).



1 2

#### Figure 8 The measured volumetric content

# 5.3 The validation and pavement response analysis based on hydro-mechanical models

5 The validation of the analytical model

To validate the established FEMs, the vertical stress underneath the wheel path in the base course was compared for different UGB models, including the SMAE model, the SAE model, the LAE model and the LIE model; these were compared to the field measurements from the embedded total pressure sensors. It should be noted that under fully saturated conditions the measured vertical stress was given in a range due to the large fluctuation stated in the previous section; under dry conditions, the vertical stress exhibited less variation and was given as an average value.

As can be seen in Figure 9, the results of all models follow a similar pattern. The vertical stresses are similar in magnitude and decrease with depth. In general, the vertical stresses measured in the saturated state were higher than the stresses measured in dry conditions. It is because the total vertical pressure measured is the sum of water pressure and effective pressure, and the water pressure in the saturated state is higher than that in the dry state. For the saturated state, only the vertical stresses predicted by SMAE model were in the range of the measured value. For the dry state, only the prediction made by SAE model is consistent with the measured

vertical stress, while the other models significantly underestimated the actual stress state by 1 neglecting the effect of non-linear and anisotropic characteristics. It should be noted that in the 2 3 subgrade, the measured vertical stresses were lower than the predictions made by the SAME and SAE model, it may be caused by the soil arching effect over the pressure sensors during 4 the construction process, which has also been observed in the previous research (Gu, F. et al. 5 6 2018). Nevertheless, the results showed that the proposed SMAE model and the weak form 7 equation-based FEM simulation can accurately describe the response of real scale permeable pavement structures subjected to accelerated loading under different degrees of saturation. 8







# Analysis of the resilient modulus distribution and the pavement response under different saturations

Figure 10 shows the resilient modulus distribution in the UGB layer by taking into account both the stress states and the pore-water pressures. The resilient modulus is not uniformly distributed in UGB layer when considering stress-dependency. The high resilient modulus values are observed near the interfacial edges between the PUPM layer and the UGB layer. The first principal stress in these areas is very high and the octahedral shear stress is relatively small.

Many research studies have shown that increasing the first principal stress (confinement effect) 1 and decreasing the octahedral shear stress (shearing effect) lead to a higher material stiffness. 2 3 Furthermore, it is also found out that the resilient modulus of the UGB layer based on the SMAE model (Figure 10, b, high saturated state) is generally higher than that based on the SAE 4 model (Figure 10, a, dry state). This phenomenon can be attributed to the fact that matric suc-5 6 tion (pore water pressures) acts as a confinement stress increasing the resilient modulus in partially saturated porous material (Gu, F. et al. 2014, Darkshanamurthy, V. et al. 1984). Therefore, 7 8 both SAE and SMAE models can be used to describe the influence of the stress level on the 9 resilient modulus of the UGB layer under dry and partially saturated states respectively.



Figure 10 Resilient modulus distribution in UGB layer based on: a) the SAE model (Dry conditions) and b) the SMAE model (92% saturated).

In order to further study the variation of stress states in the FPP structure during a rainfall event, the resilient modulus of the UGB layer was calculated with the SMAE model for different saturation states (Figure 11). As can be seen from the results, the resilient modulus of the UGB layer changes due to the water distribution. With the increase of rainfall time, the saturation level of the UGB increases; the resilient modulus also increases. Under fully saturated conditions, the resilient modulus researches a maximum of 384.5 MPa at the top of the UGB layer (Figure 11c). After the rainfall event, as the water distribution percolates into the subsoil,



1 the resilient modulus of the UGB layer experiences a decrease (Figure 11, d).

Figure 11 The resilient modulus of the UGB layer subjected to different saturation states in different rainfall stages: (a) 0.2h rainfall event with average effective saturation of 46% in the UGB layer; (b) 0.4h rainfall event with average effective saturation of 58% in the UGB layer; (c) 0.7h rainfall event with average effective saturation of 96% in the UGB layer; and (d) 5h rainfall event (0.7h rainfall + 4.3h rest), with average effective saturation of 55% in the UGB layer

## 8 5.4 Prediction of the stress state in UGB subjected to heavy vehicle loads

9 In order to facilitate the wide application of permeable pavements, the pavement needs to be 10 more stable and able to withstand heavier loads, especially in fully saturated conditions. To 11 verify the response of the original permeable pavement structure under heavy vehicle loads, a

uniform load of 700 kPa and 900 kPa are applied to the pavement structure through the pro-1 posed FEM models. Since there is no absolutely dry state in the real application, a low satura-2 3 tion state was also considered to be compared with the fully saturated state. Figure 12 shows that as the applied stress increases, the stress level of the whole UGB layer is greatly increased. 4 The vertical stress at the top of UGB layer even reached at 300MPa and 400MPa under surface 5 6 loading of 700kPa and 900kPa respectively in fully saturated state. In addition, water distribu-7 tion also has a larger influence on the stress level when higher loads are applied. However, unbound granular materials are unable to sustain such high vertical stresses. This indicates that 8 9 it is necessary to modify the design of current permeable pavement structure, to ensure the 10 stable stress state in the UGB layer.



Figure 12 The simulation of stress state in UGB layer subjected to heavy vehicle loads of 700kPa and 900kPa

To ensure that the hydraulic conductivity of fully permeable pavements is not diminished, optimized design can be only aimed to increase the modulus of the structural layers of the pavement and by increasing the thickness of the pervious surface. The modulus of the PUPM has already reached a very high level for porous materials; and the modulus of the base layer is difficult to increase by construction processes without adding other materials (Geogrid etc).

The most simple and effective approach to improve the design is to increase the thickness of the surface layer and investigate the critical design thickness of the PUPM layer for fully permeable pavement subjected to different load levels.

Based on the simulation results in Figure 13, the vertical stress of the UGB is reduced significantly compared to the results in Figure 12 by increasing the thickness of the surface layer.
Therefore, to ensure reasonable and stable vertical stress levels in the UGB layer for engineering applications, the minimum thickness of PUPM layer could be designed to be 15 and 20 cm
when the applied design load is 700 kPa and 900 kPa respectively.



9

Figure 13 The simulation of vertical stress in the UGB layer in the permeable pavement
 under fully saturated conditions based on different PUPM surface thickness and load levels
 with the SAME model

# 13 6 Conclusions

In the present research, the responses of permeable pavement structures to heavy vehicle loads under different saturations were determined based on the in-situ measurements as well as numerical simulations. Based on the developed SAME model, the distribution of water in the whole pavement structure was evaluated; also, the influence of the water content on the resilient modulus distribution within the UGB layer was analyzed. By estimating the stress state of the UGB layer subjected to different loading conditions, the sensitivity analysis was
 also proposed.

3

The main results can be summarized as follows:

Based on the full-scale APT tests on a test track under different saturations, the stress
 state of the pavement was observed to vary with the content and distribution of water
 within the pavement structure. To be precise, the higher the water content or satura tion of each layer, the higher the stress level was observed to be. Additionally, the
 pore water pressure also increases with the saturation level. This may cause moisture
 damage to the structural layer as well as erosion.

- Based on Richard's equation, the unsaturated flow in the fully permeable pavement
   can be simulated and used to evaluate the distribution of water in the pavement in
   terms of watering time. Due to the difference in permeability of each layer, the PUPM
   layer is saturated first at the beginning of a rainfall event, followed by the UGB layer.
   When the PUPM and the UGB layers are both saturated, the rainwater will not infil trate into the underlying layers because the base soil has a relatively low permeability.
- Among the proposed constitutive models, the results of the SAME simulation are 16 most consistent with the experimental stress levels under partially saturated condi-17 18 tions, while the SAE approach presents consistent results under dry conditions. If the models only consider linear elasticity, the predicted stress level is much smaller than 19 the measured one. The results confirmed the importance of nonlinear anisotropy in 20 simulating the UGB and to improve the accuracy of simulation models. Pore-water 21 pressure can be treated as confinement stress for the resilient modulus of the UGB. 22 23 As the saturation of each layer changes, the resilient modulus of the UGB layer also changes and reaches its maximum when the layer is fully saturated. 24
- Based on the SMAE simulation of the stress distribution of the FPP under heavy
   loading conditions, it is found that the influence of water on the stress state increases

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as the applied load is increased. This insight can be used to optimize the design of

2 the FPP.

Overall, in the present research, an effective evaluation and prediction method is proposed 3 for a permeable pavement structure based on the novel PUPM. The impact of shear forces 4 induced by the wheel loading was not considered in this study. In permeable pavement struc-5 tures, shear forces can lead to an expansive phenomenon that creates fluid suction into the 6 7 granular skeleton, followed by an excess of pore-pressure during the skeleton's elastic recovery. Dilation and erosion may occur in dense granular soils subjected to high shear forces, with void 8 9 ratios below a critical value. In this case, further research on the structural material in FPP based on plastic deformation theory is necessary. 10

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