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Research paper

A multi-step calibration strategy for reliable parameter determination of salt rock mechanics constitutive models

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ABSTRACT

The storage of renewable hydrogen in salt caverns requires fast injection and production rates to cope with the imbalance between energy production and consumption. This raises concerns about the mechanical stability of salt caverns under such operational conditions. The use of appropriate constitutive models for salt mechanics is an important step in investigating this issue, therefore many constitutive models with several parameters have been presented in the literature. However, a robust calibration strategy to reliably determine which model and parameter set represents the given rock, based on stress-strain data sets, remains an unsolved challenge. In this paper, for the first time in the community, we present a multi-step strategy to determine a single parameter set based on many deformation data sets for salt rocks. Towards this end, we first develop a comprehensive constitutive model able to capture all relevant nonlinear deformation physics of transient, reverse, and steady-state creep. The determination of the single set of representative material parameters is then achieved by framing the calibration process as an optimization problem, for which the global Particle Swarm Optimization algorithm is employed. To allow for dynamic data integration, a multi-step calibration strategy is developed for a situation where experiments are included one at a time, as they become available. Additionally, due to the existing mild heterogeneity in the experimental rock samples, our optimization strategy is made flexible to allow for this slight heterogeneity. The devised optimization strategy, based on the multi-physics comprehensive constitutive modeling framework, results in a single set of representative material properties of all the deformation data sets. As a rigorous mathematical analysis for the presented method and the lack of relevant experimental data sets, we consider a wide range of synthetic experimental data sets, inspired by the existing sparse relevant data in the literature. The results of our performance analyses show that the proposed calibration strategy is robust. Moreover, the results become increasingly more accurate as more data sets become available.

1. Introduction

Solution-mined salt caverns have been used for storage of hydrocarbons,^{1–4} compressed air,⁵ and even feed-stock hydrogen mainly for chemical industry.^{6,7} More recently, salt caverns are being considered as viable options for large-scale (e.g., in the orders of TWh) storage of renewable hydrogen to support energy transition.⁸ However, due to the intermittent nature of renewable sources and variable consumption rates, injection and production of renewable hydrogen is expected to occur at much more unpredictable patterns and higher frequency than the current feed-stock-based storage systems. This can result in fast pressure fluctuations inside the caverns, which naturally increases the associated uncertainties related to the mechanical stability of the caverns. To perform stability analyses,

selecting an appropriate constitutive model is the first crucial step. The constitutive model, used in the numerical simulation framework, is expected to allow for accurate prediction of the mechanical behavior of salt rock.⁹ However, if the model is not well calibrated, the simulation results can compromise the stability analysis for the cavern, thus posing threats to the storage operation. Therefore, model calibration is the second crucial step for ensuring a reliable safety assessment. The calibration process must be performed against experiments relevant to the specific application. For this reason, instead of constant load creep tests, experiments in salt samples under high-frequency cyclic loading conditions are more representative of the situation expected for renewable hydrogen storage. Under these conditions, transient creep is

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International Journal of Rock Mechanics and Mining Sciences expected to be important, therefore, it is required to be included in the constitutive model. As a result, the number of material parameters often increases significantly, hence many laboratory experiments are necessary for their proper calibration. Additionally, since these experiments are performed on different salt samples, it is not possible to ensure that they have exactly the same mechanical properties. In fact, even samples taken from the same region and with similar appearance might have slightly different properties due to mild heterogeneities in the salt formation. Therefore, the model calibration should be able to provide a set of material parameters that is representative of all experiments considered. The main focus of this work is to propose a strategy that allows for including new experiments in the calibration and provides a representative set of material parameters that fits an ensemble of experiments.

Salt rocks entail a complex mechanical behavior, with different yet co-existing time-dependent deformation mechanisms.¹⁰ Capturing all these complexities in a single constitutive model is not a trivial task. In this category, the Hou/Lux¹¹ and Composite Dilatancy Model (CDM)¹² models are developed for both transient and steady-state creep. In addition, they are also developed for tertiary creep in the dilatancy zone and damage healing in the compressibility zone. Conversely, other models disregard the compressibility/dilatancy regions and focus on specific deformation mechanisms, such as transient, steady-state, and tertiary creep.^{13–19} However, as pointed out in the literature,²⁰ full constitutive models are not always necessary depending on the specific application and the stress regimes. For instance, transient creep might be disregarded for disposal operations, since internal pressure is expected to be fairly stable. However, this is not the case for hydrogen storage operations, where fast cyclic injections and productions are expected to take place. Although some researchers consider transient creep as a viscoelastic process,^{13,14,17} others develop constitutive models that assume time-dependent inelastic deformations.^{11,21–23} When rapid pressure swings are expected to occur, some studies in the literature also include reverse creep in their modeling framework.9,24

The complexity of salt rock mechanics is often reflected in the constitutive models, which tend to depend on many material parameters. As an example, the viscoplastic part of the Hou/Lux-ODS (Ohne Direkte Schädigung) and Hou/Lux-MDS (Mit Direkter Schädigung)^{11,25} models depend on 11 and 18 material parameters, respectively. This makes the calibration strategy a very challenging task, which also requires many experimental data sets to characterize the material behavior. The viscoplastic model of Desai, for instance, requires a set of at least six experiments to determine all material parameters.²¹ An additional challenge appears by recognizing the potential inherent differences between samples and difficulties in experimental controls.²⁶ In other words, different material parameters might be found for the same batch of samples, thus requiring many sets of experiments for an ideal calibration procedure. In this case, a set of material parameters that is representative of all experiments should be pursued through the calibration process. Moreover, it should be noted that performing creep experiments in salt rocks is a time-consuming task,²⁷⁻²⁹ which means that the size of the dataset increases at a low pace. Therefore, it would be convenient to perform partial calibrations with the experimental data currently available and include new experiments as they become available. During this process, the quality of the model results should increase as more experiments are used for calibration, and it should stabilize when a sufficient number of experiments is reached.

There are different approaches for determining the material parameters of a constitutive model, some of which are complementary. As pointed out in Ref. 30, some material parameters, such as Young's modulus and Poisson's ratio, can be determined by well-defined procedures, while others are obtained either by manual (trial and error) or automated procedures, with the latter being preferred in face of a large number of parameters. A common approach for automated calibration consists of defining an appropriate objective function to be minimized in an optimization process. This is called direct calibration.³¹ Although gradient-based algorithms have been used in the literature,³⁰ metaheuristic optimization approaches^{26,32} seem to be more common as they are more likely to avoid local minima. The direct calibration approach treats the constitutive model as a black-box, so the optimization process is agnostic to the field of application. Nevertheless, such an approach is not found in the literature for constitutive models related to salt rocks. Furthermore, a procedure for incrementally including new experiments in the calibration process is also not reported in the literature.

In this context, the present work proposes a calibration strategy for a salt rock constitutive model that includes deformation mechanisms relevant to cyclic operations in salt caverns, such as transient, steady-state, and reverse creep. The calibration of the material parameters related to each deformation mechanism is presented. A multi-step direct calibration procedure is developed to include one experiment at a time by properly adjusting the objective (loss) function and solving it as a multiobjective function optimization problem. Moreover, a regularization term is added to the loss function to roughly favor the same fitting quality for all experiments. The Particle Swarm Optimization (PSO) algorithm is employed for solving the optimization problems. Moreover, we investigate a situation where each experiment is performed on salt samples with slightly different material properties. As discussed before, the goal is to obtain a single set of representative material parameters. For this purpose, synthetic experiments are employed, such that quality assessment of the proposed calibration strategy is possible. Finally, a sensibility analysis is carried out to investigate the influence of some material parameters and to clarify the possible difficulties when performing the optimization process.

The remainder of this paper is organized as follows. Section 2 presents experimental results obtained from a triaxial test on a salt rock. The experimental results serve as a guide for the choice of our constitutive model, which is presented in Section 3. Once the model is defined, the calibration strategy adopted in this work is discussed in Section 4. In Section 5, the model validation against an experimental result is presented, and the calibration strategy is tested and investigated in different situations. Finally, Section 7 closes our presentation.

2. Experimental methodology and results

To give additional insights into the mechanical behavior of salt rock and to provide a benchmark for the constitutive model employed in this work, we briefly discuss in this section a triaxial test performed on a salt rock. The experiment was performed on the Z3 Leine rock salt provided by the Institut fur Gebrismechanik GMBH (IFG), Germany. The Z3 Leine rock salt originated from the Bernburg mine in Germany, it is very homogeneous (>98% NaCl), colorless, and no obvious layering is visible. The grain size is less than 10 mm and the core sample was prepared as a 1-in. diameter and 2-in. long cylindrical shape. Additionally, the sample was stored inside an airtight bag and kept in a watertight container.

We show here the methods and results of a cyclic loading test on the Z3 Leine rock salt. The experimental data is generated as testing data to assess the ability of our constitutive computer model to describe salt behavior under cyclic loading conditions. The experiment was carried out in a standard triaxial cell operating at room temperature (21 °C). The choice for room temperature testing was made to keep the experiment as simple as possible. The triaxial cell was built inhouse (Energy Transition Campus Amsterdam, ETCA) with an axial and radial stress limit of 95 MPa. The axial and radial displacements were measured during the test. We first loaded the cylindrical sample isostatically to 12.9 MPa and let the samples consolidate until the measured axial and radial strain equilibrated. After equilibrium, the radial stress was kept at 12.9 MPa for the duration of the experiment, whereas the axial stress was increased to 23.5 MPa (at 2.0 MPa/h) and kept at this stress for 4 days and thereafter, decreased back down to 12.9 MPa (at 2.0 MPa/h) followed by a consolidation for another 2



Fig. 1. Experimental results obtained from a triaxial test performed on the Z3 Leine salt rock sample. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

days. The 4 days of high axial stress and 2 days of low axial stress were repeated for other four axial stress steps, namely, 26.0/12.9 MPa, 27.5/12.9 MPa, 31.0/12.9 MPa, 33.5/12.9 MPa (see Fig. 1). Fig. 1 also shows axial and radial strains, both measured during the experiment, and volumetric strain (calculated) versus time. In this case, all five differential stress steps show axial shortening and volumetric shrinkage, whereas the radial strain shows dilation in all differential stress steps.

A closer look at this experiment can provide valuable insights into the modeling of salt mechanics. For this purpose, the left graph of Fig. 2 shows a zoomed view of the last loading stage (i.e. from 12.9 to 33.5 MPa). Notice that the black dashed line indicates the previous maximum stress of 31.0 MPa. When the axial stress goes from point A to point B, the corresponding strain goes from point A' to B', as indicated by the dashed red curve. As can be seen, the strain increment is relatively small along the stress path A-B. However, when the axial stress exceeds the maximum stress ever applied to the sample during the experiment, which at this point is 31.0 MPa, an abrupt increase in strain is observed from point B' to C'. This suggests that an additional inelastic strain has been triggered during the stress path B-C. This can be also concluded from the right graph of Fig. 2, which shows the corresponding stress-strain relation during the loading path A-B-C. To facilitate the visualization, notice that the light and dark gray areas in the two graphs of Fig. 2 correspond. The right graph shows that from point A'' to B'', the salt sample behaves as a (visco)elastic material. However, from point B'' to C'' there is a large increase in strain for a relatively small stress increment. This is a characteristic of plastic (or viscoplastic) deformation, and it can be observed in every unloading/reloading cycle during the experiment.

Finally, the right graph of Fig. 2 shows a hysteretic effect during the unloading/reloading path. The unload path goes from point B" to point A" and the load path goes from point A" back to B". The hysteresis refers to the fact that these two paths are not the same, and this is a manifestation of the well-known reverse transient creep.³³

3. Model formulation

The constitutive model adopted in this work is specifically designed to capture the deformation mechanisms observed in the experimental results presented in Section 2. The main conclusions from the experimental results are that (i) transient creep occurs when the stress exceeds a certain threshold, which characterizes a viscoplastic behavior, (ii) the material shows reverse transient creep deformation during unloading/reloading steps, which is characteristic of viscoelastic materials. Additionally, because the stress levels are much higher than 5 MPa, pressure solution creep effects can be neglected. Finally, the volumetric strain curve shown in Fig. 1 is always positive, meaning that the stress state lies in the compressibility region so tertiary creep is not present. Based on this discussion, and assuming infinitesimal deformations, the total strain can be decomposed into four independent contributions. The first one accounts for the instantaneous elastic response. Reverse transient creep, which is observed after an unloading step, is interpreted as a time-dependent recoverable strain (i.e. viscoelastic) and is described by a Kelvin-Voigt element.²⁴ Transient creep, on the other hand, is regarded as a time-dependent inelastic deformation (i.e., viscoplastic).²³ Finally, steady-state dislocation creep is captured by a dashpot element following a power-law function. In this manner, the total strain can be written as

$$\epsilon = \epsilon_e + \epsilon_{ve} + \epsilon_{vp} + \epsilon_{cr},\tag{1}$$

where ϵ_e , ϵ_{ve} , ϵ_{vp} and ϵ_{cr} denote the elastic, viscoelastic, viscoplastic and steady-state creep strain tensors, respectively. Next, the specific models for each of these contributions are described.

3.1. Elastic strain

For convenience, we define a function of Poisson's ratio, ν , as $\mathbb{C} = \mathbb{C}(\nu)$, such that $\mathbb{C} : \mathbb{R} \to \mathbb{R}^{3 \times 3 \times 3}$ is a 4th-order tensor with elements given by

$$\mathbb{C}_{ijkl}(\nu) = \frac{\nu}{(1+\nu)(1-2\nu)} \delta_{ij} \delta_{kl} + \frac{1}{2(1+\nu)} (\delta_{ik} \delta_{jl} + \delta_{il} \delta_{jk}).$$
(2)

with δ_{ii} denoting the Kronecker delta function.

The elastic strain tensor at any time t_i can be calculated with the linear elasticity, assuming isotropic properties, i.e.,

$$\boldsymbol{\varepsilon}_{e}(t_{i}) = \mathbb{C}_{1}^{-1} : \boldsymbol{\sigma}(t_{i}), \tag{3}$$

where \mathbb{C}_1 is the constitutive 4th-order tensor, defined as

$$\mathbb{C}_1 = E_1 \mathbb{C}(\nu_1). \tag{4}$$

Here, E_1 and v_1 denote the Young's modulus and Poisson's ratio associated to the elastic deformation, respectively.

3.2. Viscoelastic strain

The solution for the time-dependent elastic (i.e. viscoelastic) strain, represented by a Kelvin-Voigt element, for continuous stress functions, has been studied in the literature.³⁴ However, experimental data sets



Fig. 2. Zoomed-in view of a reloading step of the experiment that allows for identification of both viscoplastic and viscoelastic deformations.

are discrete, not continuous. Therefore, in this work, we present a solution strategy for discrete stress conditions. Towards this end, consider a discrete stress path represented as $(\sigma_0, \sigma_1, \dots, \sigma_i, \dots, \sigma_{n-1}, \sigma_n)$ with corresponding times $(t_0, t_1, \dots, t_i, \dots, t_{n-1}, t_n)$. The viscoelastic strain (i.e., for the Kelvin-Voigt element) subjected to this discrete stress condition reads

$$\epsilon_{\nu e}(t_i) = \mathbb{C}_2^{-1}(t_i) : \sigma_0 + \sum_{j=0}^{i-1} \mathbb{C}_2^{-1}(t_i - t_j) : \Delta \sigma_{j+1},$$
(5)

where $\Delta \sigma_{j+1} = \sigma_{j+1} - \sigma_j$,

$$\mathbb{C}_{2}^{-1}(t) = \frac{1}{E_{2}} \left(1 - e^{-\frac{E_{2}}{\eta_{2}}t} \right) \mathbb{C}^{-1}(\nu_{2}), \tag{6}$$

and $\mathbb{C}(v_2)$ is defined by Eq. (2). Moreover, E_2 and v_2 denote the Young's modulus and Poisson's ratio of the spring in the Kelvin-Voigt element, and η_2 is the dashpot viscosity of the same element.

3.3. Viscoplastic strain

Following Perzyna's theory, 21,23 the viscoplastic strain rate is expressed as

$$\dot{\epsilon}_{vp} = \mu_1 \left\langle \frac{F_{vp}}{F_0} \right\rangle^{N_1} \frac{\partial Q_{vp}}{\partial \sigma},\tag{7}$$

where μ_1 and N_1 are material parameters, F_0 is a reference value, and the operator $\langle \cdot \rangle$ denotes the ramp function. The yield function²¹ is given by

$$F_{vp}(\alpha, \sigma) = J_2 - (-\alpha I_1^{n_1} + \gamma I_1^2) \left[\exp(\beta_1 I_1) + \beta \frac{\sqrt{27} J_3}{2\sqrt{J_2^3}} \right]^m$$
(8)

in which n_1 , γ , β_1 , β and *m* are material parameters. In addition, an associative viscoplastic deformation mechanism is considered, implying that the potential function Q_{vp} in Eq. (7) is equal to the yield function F_{vp} of Eq. (8).

Moreover, denoting the deviatoric stress tensor as s, the stress invariants in Eq. (8) can be written as

$$I_1 = \operatorname{tr}(\sigma) + \sigma_t, \quad J_2 = \frac{1}{2}\mathbf{s} : \mathbf{s}, \quad \text{and} \quad J_3 = \operatorname{det}(\sigma),$$
 (9)

where σ_t is the tensile strength of the rock.

The hardening parameter in Eq. (8) characterizes the behavior of the yield function. The hardening rule adopted in this work is

$$\alpha = \frac{a_1}{\left[\left(\frac{a_1}{\alpha_0}\right)^{\frac{1}{\eta}} + \xi\right]^{\eta}},\tag{10}$$

where η , a_1 , α_0 are material parameters. In particular, α_0 denotes the initial configuration of the yield surface. Additionally, ξ is the accumulated viscoplastic strain, which is given by

$$\xi = \int_{t_0}^t \sqrt{\dot{\epsilon}_{vp} : \dot{\epsilon}_{vp}} \mathrm{d}t. \tag{11}$$

Note that, before any viscoplastic deformation takes place, Eq. (11) results in $\xi = 0$ and Eq. (10) leads to $\alpha = \alpha_0$, as expected. Furthermore, the yield surface ($F_{vp}(\alpha, \sigma) = 0$) expands as α increases. In the limiting case, if $\xi \to \infty$, then $\alpha \to 0$ and the yield surface coincides with the short-term failure boundary.

Once the viscoplastic strain rate is obtained, the viscoplastic strain at time t_i is obtained by performing a time integration and using backward Euler scheme, i.e.,

$$\boldsymbol{\varepsilon}_{vp}(t_i) = \boldsymbol{\varepsilon}_{vp}(t_{i-1}) + \Delta t \dot{\boldsymbol{\varepsilon}}_{vp}(t_i), \tag{12}$$

in which $\Delta t = t_i - t_{i-1}$. Note that the viscoplastic strain rate is also computed at t_i due to the implicit formulation.

3.4. Dislocation creep strain

In this study, we neglect pressure solution creep and consider dislocation creep only, as most of the available data in the literature are conducted under deviatoric stresses exceeding 5 MPa.³⁵ Dislocation creep is often modeled as using a power law,³⁶ which reads

$$\dot{\epsilon}_{cr} = A \exp\left(-\frac{Q}{RT}\right) q^{n-1} \mathbf{s},\tag{13}$$

where *A* and *n* are material parameters, *Q* is the activation energy, *T* is temperature and *R* is the universal gas constant ($R = 8.32 \text{ J K}^{-1} \text{ mol}^{-1}$). Similar to the viscoplastic strain, the creep strain at time t_i is obtained by

$$\boldsymbol{\varepsilon}_{cr}(t_i) = \boldsymbol{\varepsilon}_{cr}(t_{i-1}) + \Delta t \dot{\boldsymbol{\varepsilon}}_{cr}(t_i), \tag{14}$$

where implicit time integration is also employed.

4. The model calibration strategy based on ensemble of data sets

In this section, we present the developed calibration strategy adopted to determine the material parameters of the multi-physics constitutive model. As summarized in Table 1, the multi-physics model entails 19 material parameters^c in total. Any manual strategy to fit them would be certainly inapplicable. Moreover, performing optimization in

^c The variable α_0 defines the initial position of the yield surface. Therefore, it is not strictly a material parameter but rather an initial condition. Nevertheless, for the purposes of this work, α_0 is also regarded as a material parameter.



Fig. 3. (a) Steady-state creep rates (slopes) represented by the magenta lines, and (b) features (ϕ, Ψ and D) observed when adjusting the elastic and viscoelastic parameters.

Table 1 Material parameters to be calibrated.

Group	Model	Parameters
1	Dislocation creep	A, n
2	Elastic Viscoelastic	E_1, v_1 E_2, v_2, η_2
3	Viscoplastic	$\mu_1, \eta, N_1, n_1, \beta, m$ $a_1, \beta_1, \gamma, \alpha_0, k, \sigma_t$

Table 2

Material parameters for Group 1.	
Parameter	Value

Parameter	Value	Unit
n	3.0	-
A	1.1×10^{-21}	$Pa^{-n} s^{-1}$

a 19th-dimensional space is cumbersome and prone to suffer from the local optimum traps or too many possibilities to match the given data set. As a remedy to this significant challenge, in this study, we propose a strategy to adjust the material parameters separately in three different groups as follows. The first group, i.e., group 1, comprises the parameters associated with the dislocation creep model. The second group, i.e., group 2, is the union of the material parameters representing both elastic and viscoelastic models. Finally, the parameters related to the viscoplastic model are considered in the third group, i.e., group 3. The sequence of calibration goes from group 1 to 3. A brief discussion of the calibration steps of each group is provided below.

4.1. Group 1: Dislocation creep model

As expressed in Eq. (13), the creep model depends on 2 material parameters: A and n. Typical values of n for dislocation creep range between 3 to 7.37 Based on this information, we adjust parameters A and n such that the slopes of the creep strain curve match those from the experimental data. For example, Fig. 3-a shows the axial strain measured from the experimental results and the target slopes (stationary creep strain rates) represented by the magenta lines. For this step, only the solution provided by Eq. (14) is necessary, since only the slopes of the curves are required.

The material parameters found for the dislocation creep model are summarized in Table 2.

4.2. Group 2: Elastic and viscoelastic models

For the elastic model, the material parameters are the Young modulus and Poisson's ratio. The latter can be determined by the ratio between radial and axial strains. Additionally, is it assumed that the Poisson's ratio for elastic and viscoelastic elements are the same,

Material parameters for Group 2.	
Table 3	

Parameter	Value	Unit
E_1	102	GPa
v_1	0.32	-
E_2	42	GPa
v ₂	0.32	-
η_2	2.5×10^{5}	GPa s

i.e., $v_1 = v_2$. The Young's modulus, E_1 , can be obtained by the slope Ψ of the unloading/reloading path, as illustrated in Fig. 3-b. Finally, the values of E_2 and η_2 are adjusted all together to match the distance D and the angle ϕ of the average unloading/loading slope.

For the elastic and viscoelastic contributions of the constitutive model, the material parameters obtained based on the above-described procedure are shown in Table 3.

4.3. Group 3: Viscoplastic model

As summarized in Table 1, the viscoplastic model requires the definition of 12 parameters. Although different types of salt rocks and the presence of impurities may produce different values for these material properties, typical values for salt rocks can be found in the literature.^{21,23} The parameter γ is associated with the short-term failure boundary, whereas β , β_1 and *m* account for the influence of Lode's angle. The position of the dilatancy boundary can be adjusted mainly through parameters β_1 and n_1 . Also, F_0 is a reference value and k is regarded as zero, meaning that an associative flow rule is adopted in this work. These parameters are summarized in Table 4.

The remaining parameters μ_1 and N_1 relate to the rate-dependent behavior of the salt rock and should be calibrated for specific samples. Similarly, the hardening rule described by Eq. (10) depends on a_1 and η , which should also be calibrated. Additionally, the initial position of the yield surface is defined by the parameter α_0 , which depends on the stress history of the rock sample. The definition of α_0 is very important for the accuracy of the predictions, in the presence of viscoplasticity.

Based on the above discussion, from the 12 material parameters associated with the viscoplastic model, only μ_1 , N_1 , a_1 , η and α_0 are to be determined. The remaining parameters are taken from typical values found in the literature. Next, the strategy developed in this work for obtaining these sets of parameters is described.

4.4. Optimization strategy

As shown in the previous subsections, the constitutive model depends on 19 material parameters. Let us denote the entire set of material parameters as $\mathbf{m} \in \mathbb{R}^{d \times 1}$, where d = 19. Furthermore, for the purpose of the optimization procedure, let us split **m** in two subsets: $\mathbf{w} \in$

Table 4

Fixed material parameters for the viscoplastic element.

Parameter	Value	Unit
	3	-
β_1	4.8×10^{-3}	MPa ⁻¹
β	0.995	-
m	-0.5	-
γ	0.095	-
F_0	1.0	MPa ²
k	0.0	-

 $\mathbb{R}^{w \times 1}$, denoting the material parameters to be optimized; and $\mathbf{k} \in \mathbb{R}^{k \times 1}$ comprising the material parameters that are fixed. Mathematically, $\mathbf{m} = \mathbf{w} \cup \mathbf{k}$, which implies that w + k = d. As discussed before, the material parameters to be optimized are

$$\mathbf{w} = \begin{bmatrix} \mu_1 & N_1 & a_1 & \eta & \alpha_0 \end{bmatrix}^T, \tag{15}$$

whereas \mathbf{k} comprises all the remaining material parameters, which are fixed (Table 4). Note that the set of material parameters to be optimized (w) belong exclusively to the viscoplastic contribution of the constitutive model.

The strain tensor for a certain experiment *i* is then obtained by

$$\boldsymbol{\varepsilon}_{i}(\mathbf{w},t) = f(\mathbf{w},\mathbf{k},\boldsymbol{\sigma}_{i}(t)) \quad \text{for } i \in [1,\dots,N], \tag{16}$$

where N is the number of experiments and $\sigma_i(t)$ is the specific stress condition applied to experiment number *i*.

For each experiment *i*, we define a loss function $F_i(\mathbf{w})$ by taking the Mean Absolute Percentage Error (MAPE) of the axial (ε_a) and radial (ε_r) strains, i.e.,

$$F_{i}(\mathbf{w}) = \frac{1}{N_{t}} \sum_{j=1}^{N_{t}} \left(\left\| \frac{\varepsilon_{a,i}(\mathbf{w}, t_{j}) - \varepsilon_{a}^{*}(t_{j})}{\varepsilon_{a}^{*}(t_{j})} \right\| + \left\| \frac{\varepsilon_{r,i}(\mathbf{w}, t_{j}) - \varepsilon_{r}^{*}(t_{j})}{\varepsilon_{r}^{*}(t_{j})} \right\| \right),$$
(17)

where $\|\cdot\|$ represents the absolute value, N_t is the number of time steps in experiment *i*, and $\epsilon^*(t_j)$ is the true deformation measured at time t_j . The MAPE metric represents an average of the percentage error at each time t_i . By considering the percentage error, the same importance is given to the errors in both the beginning and the end of the experiment.

When more than one experiment is considered, say *i* experiments, the loss functions associated with each experiment are combined by taking the Mean Squared Error (MSE) plus a regularization term, i.e.,

$$L_i(\mathbf{w}) = \frac{1}{i} \sum_{j=1}^i F_j^2(\mathbf{w}) + \phi \sigma^2,$$
(18)

in which ϕ is the regularization factor and σ^2 is the variance of the errors in all *i* experiments. The incorporation of a regularization term is designed to mitigate the risk of the optimization process becoming overly specialized to a single experiment, thereby compromising its generalizability to other experiments. This is further discussed in Section 4.4.2.

Every time a new experiment is added, an optimization problem is solved to obtain the best set of material properties for that particular experiment only. For a given experiment $\#_i$, for example, this is achieved by minimizing the corresponding loss function F_i . In other words, the set of material parameters resulting from this process is defined as

$$\mathbf{w}_i^F \approx \operatorname{argmin} F_i(\mathbf{w}) \quad \forall \ \mathbf{w} \in \mathbb{P},\tag{19}$$

where $\mathbb{P} \subset \mathbb{R}^{w \times n}$ is the initial population distribution, with *n* denoting the initial population (swarm) size. The approximate sign " \approx " is used in Eq. (19) to admit the possibility of obtaining sub-optimal or, at least, approximate solutions.

Once the single experiment optimization has been performed for experiment $\#_i$, the set of parameters \mathbf{w}_i^F is added to the population of the next full optimization, which considers all experiments from 1 to *i*, i.e.,

$$\mathbf{w}_i^L \approx \operatorname{argmin} L_i(\mathbf{w}) \quad \forall \ \mathbf{w} \in \mathbb{P} \cup \mathbb{F}_i \cup \mathbb{L}_i.$$
(20)

Here, \mathbb{F}_i and \mathbb{L}_i represent the union of the solutions obtained from optimizing Eqs. (19) and (20), respectively. In other words,

$$\mathbb{F}_i = \bigcup_{j=1}^i \mathbf{w}_j^F \quad \text{and} \quad \mathbb{L}_i = \bigcup_{j=1}^{i-1} \mathbf{w}_j^L.$$
(21)

Notice that the full optimization (Eq. (20)) is performed with the initial population plus the individuals contained in sets \mathbb{F}_i and \mathbb{L}_i . This means that the set of parameters obtained from the previous full optimizations is also considered for the current full optimization. In this manner, the calibrations of subsequent experiments do not start from scratch, as they consider the results from previous calibrations.

The complete procedure is described in Algorithm 1. Notice that \mathbb{F} and \mathbb{L} are initially empty sets. Moreover, when only one experiment is available (i = 1), there is no full optimization, so \mathbb{L} remains empty. After the second experiment has been added, full optimizations are performed and \bar{w}_i^L are added to \mathbb{L} . The algorithm loops over N experiments, including them one by one to the calibration process.

Algorithm 1 Strategy for simultaneous calibration of a set of experiments.

Aperimenta.
$\mathbb{F} = \emptyset$
$\mathbb{L} = \emptyset$
for $i \leftarrow 1 \cdots N$ do
$\mathbf{w}_i^F \approx \operatorname{argmin} F_i(\mathbf{w}) \forall \ \mathbf{w} \in \mathbb{P}$
$\mathbb{F} \leftarrow \mathbb{F} \cup \mathbf{w}_i^F$
if $i > 1$ then
$\bar{\mathbf{w}}_i^L \approx \operatorname{argmin} L_i(\mathbf{w}) \forall \ \mathbf{w} \in \mathbb{P} \cup \mathbb{F} \cup \mathbb{L}$
$\mathbb{L} \leftarrow \mathbb{L} \cup \mathbf{w}_i^L$
end if
end for

The procedure described above has been specifically designed for experimental sets performed on samples with mild heterogeneous properties. In real situations, each experiment is performed on a different salt sample. Even if the samples present a similar appearance and are taken from the same region, they are likely to have slightly different mechanical properties. In this case, it is impossible to find a single set of material parameters that produces a perfect fit for all experiments (even in the hypothetical case of no model uncertainty). In other words, there is no ground-truth (exact) solution. Instead, there is a range of solutions (parameter sets) that will produce acceptable errors. Therefore, the goal of the presented strategy is to find one of those acceptable solutions. The way this is ensured is by performing single optimizations in each new experiment (i.e., optimization of F_i) before including it in the full optimization problems (i.e., minimization of L_i). When F_i is minimized, a locally optimal solution is obtained, which is added to the initial population for minimizing the full problem L_i . Additionally, a regularization term L_i is added to prevent the solution from specializing in one single experiment (see Section 4.4.2). The importance of the regularization term and an example showing how the proposed strategy handles this heterogeneity is shown in Section 6.4. It should be stressed that, if the material heterogeneity is severe among the samples, they shall be considered different materials for which different optimum parameter sets shall be found. Only in the presence of minor heterogeneity, we can argue the samples share comparable parameter sets.

4.4.1. Optimization algorithm

The optimization problems faced in this work present two important characteristics that drive the choice of the optimization algorithm. First, the loss functions $F_i(\mathbf{w})$ and $L_i(\mathbf{w})$, respectively defined in Eqs. (17) and (18), are non-convex functions with many local minima, since the viscoplastic model admits different combinations of material parameters that produce similar results. Second, the computation of gradients, especially for $L_i(\mathbf{w})$, is expensive. In this context, population-based



Fig. 4. (a) Multi-objective optimization and Pareto front (experiments #1 and #2 in this figure are only meant for illustration purposes), and (b) high and (c) low variance of F_i.

algorithms appear to be more attractive over gradient-based methods as they are less likely to be trapped in local minima and are independent of gradients. For this reason, we adopt the Particle Swarm Optimization (PSO) algorithm^{38,39} for solving the optimization problems of Eqs. (19) and (20). In this method, an initial population is created within the search space, and each member of the population represents a possible solution. Each individual is assigned an initial velocity so they can move through the search space. For each time step (iteration), the velocity of a certain particle *i* is computed as

$$\mathbf{v}_i^{t+1} = \omega \mathbf{v}_i^t + c_1 \mathbf{r}_1 \left(\mathbf{p}_i^t - \mathbf{x}_i^t \right) + c_2 \mathbf{r}_2 \left(\mathbf{g}_i^t - \mathbf{x}_i^t \right), \tag{22}$$

where ω , c_1 and c_2 are weights given to the previous velocity (inertia), particle's best position (\mathbf{p}_i^t) and swarm's best position (\mathbf{g}_i^t), respectively. The choice of these hyperparameters allows for balancing between exploration and exploitation. Appropriate values can be manually defined by performing initial tests, and they do not need to be redefined when new experiments are included in the calibration. In this study, the values used are $\omega = 0.7$, $c_1 = 0.7$ and $c_2 = 0.5$. Moreover, \mathbf{r}_1 and \mathbf{r}_2 are random vectors between 0 and 1. With this new velocity, the position of particle *i* is updated by

$$\mathbf{x}_{i}^{t+1} = \mathbf{x}_{i}^{t} + \mathbf{v}_{i}^{t+1}.$$
(23)

Once all particles have their positions updated, the algorithm proceeds to the next iteration. This process is repeated until a stop criterion is reached.

4.4.2. Multi-objective function optimization

Solving an optimization problem for multiple experiments simultaneously (Eq. (20)) consists of multi-objective function optimization, since the goal is to minimize the loss functions F_i for all experiments. This type of problem admits an infinite number of solutions that are not dominated by other feasible solutions, which means that they are all acceptable solutions to the minimization problem. This set of solutions is called the Pareto optimal front and is illustrated in Fig. 4 for a situation where only two experiments are considered.

Although all solutions along the Pareto front are admissible, we notice that the solution at point A provides a good fit for experiment #1 and a sub-optimal solution for experiment #2. Similarly, point C provides a better fit for experiment #2 than for #1. On the other hand, point B provides a solution that is equally good for both experiments, since $F_1 \approx F_2$, and therefore should be preferred.

To "encourage" the solution to stay along the dashed line of Fig. 4 we penalize the loss function L_i when $F_1 \cdots F_N$ are too different from each other, that is, high variance (see Fig. 4-c). The loss function is

then composed of a mean squared error (MSE) part and a regularization (Reg.) part. Mathematically, this can be written as

$$L_{i}(\mathbf{w}) = \frac{1}{i} \sum_{j=1}^{i} F_{j}^{2}(\mathbf{w}) + \phi \underbrace{\frac{1}{i} \sum_{j=1}^{i} \left[F_{j}(\mathbf{w}) - \tilde{F}(\mathbf{w})\right]}_{\sigma^{2}} = \underbrace{\frac{1}{i} \sum_{j=1}^{i} F_{j}^{2}(\mathbf{w}) + \underbrace{\phi\sigma^{2}}_{\text{Reg.}}}_{\text{MSE}},$$
(24)

where $\tilde{F}(\mathbf{w})$ is the average error of all experiments, as indicated in Fig. 4, and ϕ is an arbitrary regularization factor. When variance is high (Fig. 4-b), the regularization term is large, thus penalizing the loss function L_i . When variance is close to zero (Fig. 4-c), which means that the fit quality for all experiments is about the same, the regularization term tends to vanish from Eq. (24).

5. Results

In the first part of this section, we investigate the capabilities of the proposed constitutive model in describing the mechanical behavior of salt rocks observed in the laboratory. In the sequence, the optimization procedure proposed for the model calibration is explored. We first start by presenting the synthetic data employed throughout our analysis. Sensitivity analysis is performed to identify the impact of each material parameter on the model behavior. The PSO algorithm is first employed to calibrate each synthetic experiment individually. Then, the calibration strategy is tested for fitting the entire set of experiments as they become available, as described in Algorithm 1.

5.1. Model validation

The primary purpose of this subsection is to show that the constitutive model presented in Section 3 is able to accurately capture the time-dependent behavior of salt rocks operating in the compressibility zone (i.e., no tertiary creep) and under cyclic loading conditions. Additionally, we intend to highlight the importance of each term considered in the proposed constitutive model. Of particular interest is the description of transient creep, as it is permanently present during cyclic operations. For this purpose, we use three different models to describe the experimental results discussed in Section 2. These models are summarized in Table 5, and they differ from each other by how the transient creep is described. In Model 1, the transient creep is described by the Kelvin-Voigt element presented in Section 3.2, thus assuming that transient creep deformations are fully recoverable (elastic). On the other extreme, the hypothesis that all the deformation observed



Fig. 5. Total strain curves obtained with three different models.

 Table 5

 Models with different assumptions regarding the transient creep.

Model	Total strain	Transient creep
1	$\boldsymbol{\varepsilon} = \boldsymbol{\varepsilon}_e + \boldsymbol{\varepsilon}_{cr} + \boldsymbol{\varepsilon}_{ve}$	Fully elastic ($\boldsymbol{\epsilon}_{ve}$)
2	$\boldsymbol{\varepsilon} = \boldsymbol{\varepsilon}_e + \boldsymbol{\varepsilon}_{cr} + \boldsymbol{\varepsilon}_{ve} + \boldsymbol{\varepsilon}_{vp}$	Hybrid ($\boldsymbol{\epsilon}_{ve} + \boldsymbol{\epsilon}_{vp}$)
3	$\boldsymbol{\varepsilon} = \boldsymbol{\varepsilon}_e + \boldsymbol{\varepsilon}_{cr} + \boldsymbol{\varepsilon}_{vp}$	Fully inelastic ($\boldsymbol{\epsilon}_{vp}$)

during the primary stage of creep is fully inelastic is assumed by Model 3, in which the viscoplastic model presented in Section 3.3 is employed. Finally, a combination of both hypotheses is assumed by Model 2, where the viscoelastic (Kelvin-Voigt) element is combined with the viscoplastic element. It should be stressed that the terminologies "fully-elastic", "hybrid" and "fully-inelastic", employed in Table 5 to designate these models, refer exclusively to the underlying assumption of each model regarding the transient creep stage. For instance, Model 1 is not fully elastic as a whole, because of steady-state creep (ϵ_{cr}), but the transient creep stage is regarded as such.

The models presented in Table 5 are now used to fit laboratory experimental data. The experimental setup and salt rock details are presented in Section 2. It can be verified from Fig. 5 that Model 1 can be calibrated to properly describe the transient creep during the first step load. However, the assumption that transient creep strains are fully recoverable implies that most of the deformation should be reversed when the load is removed. This is precisely what we observe in the zoomed-in graph on the left of Fig. 5, where the unloading takes place at around 100 h. As expected, the total strain obtained with Model 1 is almost fully recovered after unloading, but this is not observed in the experimental results. In fact, only a small strain decrease is observed when the load is removed. Furthermore, the stress–strain graph in Fig. 6 shows that Model 1 provides a completely wrong behavior. This shows that transient creep is not fully elastic, and therefore cannot be described by a simple Kelvin-Voigt element.

It can be verified in Fig. 6 that Models 2 and 3 provide almost identical results, and both of them are able to describe the experimental data. Despite that, the zoomed-in graph in Fig. 6 clearly shows that Model 3 is unable to capture the reverse creep (hysteretic effect) observed during the unloading/reloading step. By contrast, the Kelvin-Voigt element of Model 2 can be tuned to properly describe reverse creep. These results reveal that transient creep (including reverse transient creep) can only be described by a combination of viscoplastic and viscoelastic models.

6. Calibration procedure

In this section, we investigate the calibration procedure described in Section 4. A set of synthetic experiments is designed to test the proposed strategy. The idea is to simulate a situation in which the experiments are provided one at a time, and the number of experiments available is not sufficient for a proper model calibration. In this context of high uncertainty, the goal is to perform a model calibration as good as possible with the experiments available and also to quantify the associated uncertainties.

6.1. Synthetic experiments

When a constitutive model is chosen to represent the mechanical behavior of a certain material, there are two sources of uncertainties. The first one is related to the uncertainties associated with measuring the material properties of that specific model. The second source of uncertainties is that the model itself is not perfect, in the sense that it is only a representation of reality, thus inaccurate. In addition to overcoming the lack of available laboratory experimental data, by using synthetic data generated from the same model we intend to calibrate, model uncertainty is also eliminated. In this manner, the effects of parameter uncertainties are isolated, allowing to better study the properties of the proposed calibration strategy. Moreover, it should be emphasized that synthetic data do not substitute real experimental data by any means. If the constitutive model is intended to be used in a real application, the calibration must be performed against laboratory (real) experimental data. Nevertheless, to ensure the synthetic data is as close as possible to a real situation, cyclic loading conditions are chosen such that they are similar to those used in the experimental results presented in Section 2.

In this work we consider 6 synthetic experiments in which the correct model parameters are known, thus providing the possibility of quantifying the calibration accuracy. The idea is to simulate a situation, where the experiments are made available one at a time, and the calibration takes place with the available data. This means that the calibration is first performed on Exp. #1. Then, Exp. #2 is made available and calibration is performed considering experiments #1 and #2. This is repeated until all six synthetic experiments are available.

The synthetic experiments are shown in Fig. 7. The stress conditions were chosen as shown in the left column of the figure. The graphs in the middle column show the stress path of each experiment with the colors representing the time. The stresses on the left and middle columns correspond to each other. To make the association easier to visualize, we marked specific points on the graphs of the left and middle columns that correspond to each other. In these same graphs, the initial yield surface of the viscoplastic model is also plotted for reference, according to Eq. (8). Finally, the corresponding strain responses are shown in the right column of Fig. 7. In all stress conditions shown in Fig. 7, the axial load is larger than the confining pressure, which means that the same Lode angle ($\theta = 60^{\circ}$) was considered in all experiments.

All experiments shown in Fig. 7 use the same set of material properties. The dislocation creep (Group 1) and viscoelastic (Group



Fig. 6. Stress-strain curves showing the unloading/loading step (reverse creep).

Table 6

Material properties for the synthetic experiments.				
Unit				
s ⁻¹				
-				
MPa ²⁻ⁿ				
-				
-				

Table 7

Ranges of variation of each material property for the uniform distributions.

$\log \alpha_0$
-1.9
-2.8

2) parameters are shown in Tables 2 and 3, respectively. For the viscoplastic element, the material parameters that are fixed (i.e., not obtained by calibration) are shown in Table 4. Finally, Table 6 presents the material parameters meant to be obtained through the calibration process. Even though these values are known, they are regarded as unknown so that we can test the optimization procedure.

6.2. Global sensitivity analysis (GSA)

Before proceeding with the model calibration, we investigate how the material parameters presented in Table 6 affect the model results. For this purpose, we perform global sensitivity analysis (GSA), where all parameters are varied at the same time so that we can identify not just how each parameter affects the results individually, but also the interactions between them.⁴⁰

The strategy consists of generating a large population (~40 thousand) of material parameter sets. We build random uniform distributions for each material parameter within specified ranges, as shown in Table 7. For each set of parameters, we compute a loss function by comparing the resulting strains with a base solution. The loss function is computed as in Eq. (17), with the set of parameters summarized in Table 6 regarded as the base solution. In this manner, we can analyze how the changes in the material parameters affect the values of the loss function. It is important to emphasize that Table 7 presents very wide variations with the exclusive purpose of better capturing the correlations between all material parameters. Samples with such large variations should be grouped in different batches according to their similarity, and each batch be calibrated separately. Fig. 12 (from the revised manuscript) shows much narrower ranges of variation and the corresponding effect on the mechanical response, illustrating what could be expected from similar (yet heterogeneous) samples.

There are many ways GSA can be performed. One of them is computing statistical correlations between the material parameters and the

Table 8							
Table of correlation	of each	material	parameter	with	the	loss	function.

	μ_1	N_1	a_1	η	α_0
Spearman	0.1	0.1	0.5	0.4	0.6
Pearson	0.02	0.03	0.3	0.2	0.2
Mutual Info.	0.03	0.03	0.7	0.4	1.0
F-test	0.04	0.03	1.0	0.5	0.9

loss function.^d The Pearson and Spearman correlations are commonly applied to identify linear and non-linear relationships, respectively, between variables.⁴¹ Additionally, univariate F-test is also able to capture linear relations, whereas mutual information can capture any type of dependency. It is important to stress that both Pearson's correlation and F-test assume normal distributions, which is not the case here. Nevertheless, the four methodologies are employed to identify relationships between the material parameters and the loss function. According to these methodologies, Table 8 reveals a strong relationship between the loss function and parameters a_1 , η and α_0 , the first two related to the hardening rule, and the last one defining the initial yield surface. All four methodologies point to a weak dependency on the rate-dependent parameters μ_1 and N_1 . These results are also confirmed by analyzing feature importance through a machine learning model and column permutation, as presented in Appendix.

The dataset is created by choosing random values within the ranges specified in Table 7. As a consequence, the correlation between the material parameters is strictly zero. When the simulations are performed on the dataset, the resulting probability distribution of loss function values is shown in the left graph of Fig. 8. We can see that there is a high probability of loss function values between 0.1 and 1.0, which suggests the existence of local minima. To further investigate this issue, we filter the loss function values larger than 0.1 out of our dataset and compute Spearman's correlations between all material parameters. In this manner, we only consider parameter sets that produce reasonably good results (loss function values smaller than 0.1). These correlations are shown in the right graph of Fig. 8, where a strong relationship between a_1 and η is identified. Weaker dependencies are also revealed between μ_1 , N_1 and α_0 . This shows that certain combinations between these variables can produce relatively good results.

A better way to visualize this effect is by computing Spearman's coefficient as we continuously filter out the loss function values from 10^5 down to 10^{-2} . This is shown in Fig. 9, which clearly shows a significant increment of dependency between a_1 and η for loss function values smaller than 1.0. To a lesser degree, similar behavior can be verified for the pairs $\mu_1 - N_1$ and $\mu_1 - \alpha_0$, as already revealed by the right

 $^{^{\}rm d}$ We actually use the logarithm of the loss function as it spans many different orders of magnitude.



Fig. 7. Synthetic experiments. Graphs on the left show the axial and radial stresses for each experiment. The middle column shows the corresponding stress path in the $I_1 - \sqrt{J_2}$ plane, and the initial yield surface is also indicated according to Eq. (8) for $\alpha = \alpha_0$. The right column presents the resulting deformations of the synthetic sample. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

graph of Fig. 8. It is important to emphasize that all combinations of material parameters were obtained by random sampling, thus ensuring zero correlation between them. What the results of Figs. 8 and 9 reveal is that all sets of parameters that produce a relatively good solution present a certain (still unknown) correlation between a_1 and η . The sets of material parameters that do not present this correlation do not produce good results compared to the base case.

To understand the origin of the correlation between a_1 and η , the hardening rule expressed by Eq. (10) is used. In this equation, $\alpha_0 = 0.02$, $\eta^* = 0.82$ and $a_1^* = 1.8 \times 10^{-5}$ hold, where the values η^* and a_1^* denote a pair P^* . By varying the accumulated viscoplastic strain (ξ) from 0 to 0.0075, which are typical values, the curve S^* can be plotted, shown in black in the left graph of Fig. 10. This curve is regarded as a base case. Then different pairs $P_i = (\eta_i, a_{1,i})$ are chosen to generate different curves S_i , which are compared with S^* using the

mean absolute percentage error (MAPE). The colormap in the right graph of Fig. 10 shows the MAPE values for each pair P_i . It is possible to identify a very low error region, denoted in blueish colors, meaning that all points (i.e., combinations of η and a_1) produce curves similar to S^* . The point P^* is naturally in this region. For illustration, six points are picked along this region and the corresponding S_i curves are plotted on the left graph of Fig. 10, showing that they indeed approximate the original curve S^* quite well. The existence of this blue region explains the correlation between a_1 and η in the right graph of Figs. 8 and 9. More importantly, they exemplify the presence of local minima in loss functions.

The results obtained from the global sensitivity analysis, particularly the ones in Fig. 10, give an idea about the behavior of the loss functions for the optimization procedure. These results show the presence of many local minima in which the optimization algorithm





Fig. 8. (Left) Loss function distribution. (Right) Spearman correlations for loss function values lesser than 0.1.



Fig. 9. Spearman's correlation with filter out loss values.

might be trapped, which allows the possibility of obtaining sub-optimal solutions.

6.3. Single calibrations

The goal of this subsection is to test the Particle Swarm Optimization (PSO) algorithm for finding the true material parameters of the synthetic experiments presented in Section 6.1 (Fig. 7). The idea is to run individual optimizations for each synthetic experiment and check whether the calibration process can indeed find the global solution, which is shown in Table 6. The hyperparameters used in the PSO algorithm (Eq. (22)) are $\omega = 0.8$, $c_1 = 0.8$ and $c_2 = 0.4$, the algorithm is set to perform 100 iterations, and the population size is 1280. To maximize coverage of the search domain, Latin Hypercube Sampling (LHS) is adopted and the ranges of each material property are those presented in Table 7.

The calibration outcomes obtained for each synthetic experiment are shown in Fig. 11. The left column of this figure shows a cobweb representation of the material properties. The gray lines represent the initial population, the red line denotes the set of properties obtained from the optimization process, and the true values are plotted in blue for comparison. The rightmost vertical bar in the cobwebs represents the loss function F_i (MAPE), according to Eq. (17), and its corresponding values for the best solution are also indicated. The right column shows the total strains obtained with the calibrated properties for each experiment, and they all agree very well with the (synthetic) experimental results. For experiments #3 and #5 the values of a_1 and N_1 obtained from optimization differ from the true values. However, as revealed by the GSA, these two parameters have a secondary importance compared to the others, so these disparities do not have much impact on the behavior of the constitutive model. The values obtained from the calibrations of each experiment are summarized in Table 9, along with the corresponding errors.

Table 9				
Material para	meters obtained	l from the	calibration	process.

	$\log \mu_1$	N_1	$\log a_1$	η	$\log \alpha_0$	Loss (F_i)
Reference	-11.1613	3.0000	-4.7447	0.8200	-2.6990	0.0
Exp. #1	-11.1414	2.9815	-4.7450	0.8201	-2.6991	6.02×10^{-8}
Exp. #2	-11.3425	3.1648	-4.8521	0.8772	-2.6993	1.47×10^{-5}
Exp. #3	-11.9118	3.9593	-4.7436	0.8202	-2.6951	2.39×10^{-4}
Exp. #4	-11.1942	2.9800	-4.7543	0.8256	-2.6987	7.13×10^{-6}
Exp. #5	-11.6245	3.4175	-4.8789	0.8925	-2.6972	7.54×10^{-5}
Exp. #6	-11.2350	3.0760	-4.6827	0.7875	-2.6978	1.33×10^{-6}

6.4. Full calibrations

In this test case, we aim to test the proposed calibration strategy in a more realistic scenario. In laboratory conditions, even if the rock samples are taken from the same region with a similar appearance, it is not possible to guarantee they will present exactly the same mechanical properties. Additionally, in general, the experiments are performed sequentially, meaning that they are not all available simultaneously. Considering that each creep experiment takes at least 20 to 30 days, approximately, it would be convenient to have partially calibrated models with the experiments at hand and include new experiments to the calibration as they become available.

To reproduce such a scenario, we take the reference values presented in Table 6 and randomly disturb the material properties of each rock sample. In this manner, all experiments are performed with rock samples with slightly different material properties. The levels of perturbations are $\pm 5\%$ for $\log \mu_1$ and N_1 , $\pm 2\%$ for $\log a_1$ and η , and $\pm 1\%$ for $\log \alpha_0$. The material properties for the rock samples of each experiment are presented in Fig. 12. The graphs in this same figure show the total strains obtained with the reference properties (i.e. those of Table 6) and the modified properties. It can be verified by visual comparison that the strain curves do not differ much from the reference case, but those small property variations do cause noticeable differences. Since the material properties of each experiment are different from each other, it is impossible to perfectly fit all experiments. Nevertheless, the goal of the calibration is to find a single set of material properties that fits the experiments as good as possible. Additionally, the calibration is performed in steps, including one new experiment at a time, according to Algorithm 1.

The result of the calibration procedure is presented in Fig. 13. The first line of this figure represents step 1, in which only experiment #1 is available for calibration. Once the model is calibrated against experiment #1, the model is used to predict the behaviors of the other experiments.^e Above each graph is indicated the F_i error, as in Eq. (17),

^e Even though this would never be possible in real life, we use the remaining experiments for prediction in order to check predictability.



Fig. 10. The left graph presents the behavior of α as a function of ξ for different values of η and a_1 . The right graph shows the MAPE for each pair $\eta - a_1$ compared to the true value P^* . (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Table 10

Population	sets	₽,	\mathbb{F}	and	\mathbb{L}	during	the	calibration	steps
------------	------	----	--------------	-----	--------------	--------	-----	-------------	-------

Step	Initial population	\mathbb{F}	L	Output
#1	\mathbb{P}	ø	ø	\mathbf{w}_1^F
#2	\mathbb{P}	\mathbf{w}_1^F	ø	\mathbf{w}_2^F , \mathbf{w}_2^L
#3	\mathbb{P}	\mathbf{w}_1^F , \mathbf{w}_2^F	\mathbf{w}_2^L	\mathbf{w}_3^F , \mathbf{w}_3^L
#4	\mathbb{P}	\mathbf{w}_1^F , \mathbf{w}_2^F , \mathbf{w}_3^F	\mathbf{w}_2^L , \mathbf{w}_3^L	\mathbf{w}_4^F , \mathbf{w}_4^L
#5	\mathbb{P}	\mathbf{w}_1^F , \mathbf{w}_2^F , \mathbf{w}_3^F , \mathbf{w}_4^F	\mathbf{w}_2^L , \mathbf{w}_3^L , \mathbf{w}_4^L	\mathbf{w}_5^F , \mathbf{w}_5^L
#6	\mathbb{P}	\mathbf{w}_1^F , \mathbf{w}_2^F , \mathbf{w}_3^F , \mathbf{w}_4^F , \mathbf{w}_5^F	\mathbf{w}_2^L , \mathbf{w}_3^L , \mathbf{w}_4^L , \mathbf{w}_5^L	\mathbf{w}_6^F , \mathbf{w}_6^L

for each experiment. The loss function values L_i , given by Eq. (18), are presented on the left for the calibrated (blue) and predicted (red) experiments. In the first step, only experiment #1 is available, so a single optimization (Eq. (19)) is performed using the initial population \mathbb{P} to obtain \mathbf{w}_1^F . When experiment #2 is available in the second step, another single optimization, with \mathbb{P} as the initial population, is performed on it, which provides the set of parameters \mathbf{w}_2^F . Still on the second step, a combined optimization (Eq. (20)) is performed upon experiments #1 and #2 including \mathbf{w}_1^F and \mathbf{w}_2^F among the initial population \mathbb{P} . The combined optimization between experiments #1 and #2 provides \mathbf{w}_2^L , which should be included in the combined optimization of the subsequent steps as well. This whole process is summarized in Table 10 for all calibration steps.

It can be verified from Fig. 13 that the combined loss function for the calibrated experiments, L_{cal} , substantially increases as more experiments are included in the calibration procedure. At the same time, the L_{pred} is observed to decrease, which suggests that the predictability of the calibrated constitutive model improves by adding new experiments. Fig. 14 plots these two quantities by the number of experiments available for calibration. On the left graph of this figure, we see that the loss function indeed increases in the beginning but it remains more or less constant as more experiments are added to the calibration. The reason for this is, as mentioned before, it is impossible to simultaneously fit all experiments since they have different material properties, so after a certain point the error is expected to stabilize at a constant level. On the left graph, however, we see that the more experiments we consider for calibration, the better the predictions of the constitutive model.

Eq. (18) includes the parameter ϕ as a regularization in the loss function for the combined optimization. The results presented in Fig. 13 were obtained with a regularization factor of $\phi = 10$. To investigate how the regularization term affects the calibration process, the same test case is run considering $\phi = 0$, $\phi = 10$ and $\phi = 100$. The loss function values L_i are shown in Fig. 14 as a function of the number of experiments considered for calibration. The graph of Fig. 14-a shows the results of the calibration experiments, where the loss function

(Eq. (24)) increases until the inclusion of the third experiment and stabilizes at approximately constant values. As expected, the larger the ϕ the larger the L_i , since the regularization term becomes larger. The graph in Fig. 14-b shows the loss function values for the experiments left for prediction. It can be seen that the loss function values decrease as more experiments are considered for calibration. In other words, it shows that the constitutive model can make better predictions when more experiments are considered during calibration. Additionally, it can be verified that for 5 experiments considered during calibration, the prediction of the 6th experiment is better when $\phi = 10$. Since it might be difficult to compare the loss function values with different values of ϕ , the graphs in Fig. 14-c and -d show the same results, but without the regularization term in the loss function. In other words, the graphs in Fig. 14-c and -d only show the mean squared errors (MSE) part of the loss function. In this case, the comparisons are unambiguously and we can see from the right graph that indeed better predictions are obtained with $\phi = 10$.

As explained before, the sets of properties chosen for each experiment were obtained by randomly disturbing the reference properties of Table 6. Therefore, it would be reasonable to expect that the reference properties themselves would also provide good performance in fitting all six experiments as well. In Fig. 15 we compare the total strains for all experiments considering the calibrated (red curves) and the reference (blue curves) set of material properties. The curves in black represent the true values of the synthetic experiments. It can be verified that experiments #2, #3 and #4 are better fitted by the calibrated parameters, whereas the reference properties perform slightly better for experiments #1, #5 and #6. However, the mean squared errors (MSE) shown at the bottom of this figure reveal that the calibrated material parameters present an overall better fit.

The calibrated results presented in Fig. 15 are obtained with a regularization parameter of $\phi = 100$. Different regularization parameters, however, may lead to different calibrated material properties. The obtained values for ϕ equals to 0, 10 and 100 are summarized in Table 11, along with the reference properties for comparison. As shown in this table, the MSE values of the calibrated properties are always smaller than the reference properties. Interestingly, the material properties obtained through the calibration process are significantly different from each other and the reference values. Apart from α_0 , the other material properties even lie outside the limits of the perturbed properties, as it can be verified in Fig. 12. This can be attributed to the non-linearity of the viscoplastic model.

The fact that Table 11 presents different material parameter sets for each choice of the regularization term, ϕ , might raise the question of which set is the "correct" one. Or even if the obtained parameter sets would be the same if the order in which the experiments are added was shuffled. In this context, it is important to note that each synthetic experiment was obtained with a different set of material parameters,



Fig. 11. Synthetic experiments. (Left) Cobweb representation of the material parameters. (Right) Comparison between the true synthetic experiments and the calibrated model. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Table 11

Calibrated material properties obtained with different values of ϕ , and the reference properties from Table 6 for comparison. The last line shows the mean squared error (MSE) for each set of properties.

	$\phi = 0$	$\phi = 10$	$\phi = 100$	Reference
μ_1	4.51×10^{-12}	1.83×10^{-12}	9.77×10^{-12}	6.89×10^{-12}
N_1	2.98	3.99	3.47	3.00
a_1	4.33×10^{-5}	3.12×10^{-6}	2.19×10^{-5}	1.80×10^{-5}
η	0.60	1.19	0.74	0.82
α_0	0.00207	0.00205	0.00202	0.0020
MSE	0.0615	0.0635	0.0609	0.5167

which has a few implications. First, the minimum error cannot be zero, since the calibrated model can never perfectly fit all experiments. Second, it is not possible to ensure the existence of a global minimum error. In other words, there might be many sets of material parameters that produce the minimum error, or very close to it. Therefore, in the absence of a ground truth, any set of material parameters that minimizes the fitting error should be accepted. Moreover, shuffling the order in which the experiments are included can indeed change the final results, but they should be equally acceptable, as discussed above.

A discussion regarding the acceptable ranges of material property variations is also worthy to be carried out. Considering the extreme case where all samples present the same material properties, the optimization problem has a global minimum, and the error is zero at a single set of material parameters. Nevertheless, the problem is still non-convex,



Fig. 12. The black curves (Ref.) are obtained with the reference properties of Table 6, whereas the blue curves (Mod.) are created by perturbing (modifying) the reference properties. The modified material parameters are indicated below each graph. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



Fig. 13. Calibration process including one experiment at a time. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



Fig. 14. Loss function comparison for calibrations and predictions.



Fig. 15. Constitutive model results obtained with the material properties obtained from calibration and the reference values from Table 6. The overbar refers to the quantities related to the reference parameters. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

meaning that the cost function has (possibly lots of) local minima. Although challenging, the PSO should be able to find the global minimum by calibrating the model against one single experiment, provided that a large enough population is employed to avoid all local minima. If the material properties are slightly different for each sample, the presence of a global minimum is not guaranteed anymore. In this case, there is a narrow set of possible material parameters that produce the best results. In other words, instead of one single solution, a narrow range of solutions should be acceptable. Further proceeding to the other extreme case, when the variance among the material properties is high, a wide range of material parameters could produce the best results. From this perspective, the higher the variance of properties, the wider the range of acceptable solutions, and the easier for the PSO to find one of the possible solutions. However, the best results in this case would certainly not be good, thus compromising the validity of calibrating one single model for a set of samples with such different mechanical behaviors.

7. Conclusion

Geomechanics of salt caverns for safe cyclic hydrogen storage requires a detailed investigation of the associated creep mechanisms. For this purpose, we assemble a constitutive model able to capture transient creep, reverse creep and steady-state dislocation creep. This is achieved by including elastic, viscoelastic, viscoplastic, and power-law contributions to the constitutive model. The viscoelastic contribution can capture the hysteretic effect that appears during the unloading/reloading stages, also known as reverse creep. Moreover, it is shown that the viscoelastic element alone is not able to appropriately describe transient creep, for which a viscoplastic model is indispensable. With this constitutive model, the experimental results presented in this paper can be successfully described.

An important step in devising and deploying a constitutive model relates to model calibration. Due to the time scales involved in creep deformations, laboratory experiments in salt rocks are usually very time-consuming (approximately one month long or even more). Additionally, it takes a lot of experiments to properly calibrate a constitutive model. There is also the possibility that mechanical properties might vary from sample to sample, making the calibration process more challenging. In this context, the main contribution of this paper is to devise a multi-step calibration strategy that takes place on the fly, in the sense that the constitutive model is calibrated against experiments as they are made available. Determination of the material parameters corresponding to the elastic, viscoelastic, and dislocation creep can be done independently because the presented procedure is general and flexible. Another significant contribution of the present study is on the calibration of the viscoplastic material parameters, which have to be all tuned simultaneously. Moreover, the choice of the material parameters to be calibrated is discussed, and a systematic analysis for the impact of these parameters on the constitutive model behavior is also presented. The calibration strategy consists of sequentially solving multi-objective optimization problems as new experiments are included.

It is shown that the proposed strategy provides increasingly better results as more experiments are incorporated into the calibration process. In this manner, calibrated constitutive models are provided much more efficiently and reliably than the existing procedures in the literature. Additionally, it is shown that including a regularization term into the loss function is beneficial to promote equal quality fit of the constitutive model against all experimental data sets. The proposed methodology can be applied to any constitutive model, and it provides representative material parameters for salt rocks. As such, this work contributes to improving the accuracy of constructing a suitable constitutive model with reliable material parameter sets to study the mechanics of salt caverns under cyclic operations. Future studies will incorporate this characterization procedure in field-scale 3D cavern simulations.

Table A.12

Feature importance according to the column permutation method.							
Feature name	μ_1	N_1	<i>a</i> ₁	η	α ₀		
Importance	0.050916	0.054642	0.814813	0.543760	0.872997		

CRediT authorship contribution statement

Hermínio T. Honório: Writing – original draft, Visualization, Validation, Software, Methodology, Formal analysis, Conceptualization. Maartje Houben: Writing – review & editing, Investigation, Conceptualization. Kevin Bisdom: Writing – review & editing, Conceptualization. Arjan van der Linden: Investigation. Karin de Borst: Conceptualization, Writing – review & editing. Lambertus J. Sluys: Writing – review & editing, Methodology, Conceptualization. Hadi Hajibeygi: Writing – review & editing, Methodology, Conceptualization.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available on request.

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Appendix. Feature importance for sensitivity analysis

Another interesting strategy to measure the influence of each material parameter on the model behavior is through feature importance, as usually performed in machine learning (ML) applications. Some ML models, such as linear regression and decision trees, naturally provide feature importance rankings. A more general approach can be achieved by column permutation. This strategy consists of training a ML model to predict the target variable (in our case, the loss function). After the training step, the model performance is evaluated according to a certain metric (e.g. MSE). This establishes a base metric for the ML model. Then, we shuffle the values of a certain feature (i.e., material parameter), rerun the model without retraining, and check the new metric. Based on how much the new metric is reduced compared to the base metric we can infer the importance of that feature. A great reduction means the ML model heavily relies on that feature. Conversely, if the metric barely changes, it means the ML model does not find that feature very useful. This procedure is performed using the Random Forest algorithm and the results are shown in Table A.12. We can see that parameters μ_1 and N_1 are of less importance compared to a_1 , η and α_0 . This is in complete agreement with the correlations found in Table 8.

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References

- Lux K-H. Design of salt caverns for the storage of natural gas, crude oil and compressed air: Geomechanical aspects of construction, operation and abandonment. *Geol Soc Lond Spec Publ.* 2009;313(1):93–128. http://dx.doi.org/10.1144/SP313.7.
- Tarkowski R, Uliasz-Misiak B, Tarkowski P. Storage of hydrogen, natural gas, and carbon dioxide–Geological and legal conditions. Int J Hydrog Energy. 2021;46(38):20010–20022. http://dx.doi.org/10.1016/j.ijhydene.2021.03.131.
- Allen K. Eminence dome-natural-gas storage in salt comes of age. J Pet Technol. 1972;24(11):1299–1301. http://dx.doi.org/10.2118/3433-PA.
- Gentry H. Storage of high pressure natural gas in underground salt or rock caverns. In: Symposium on Salt. 1963:604–608.
- Crotogino F, Mohmeyer K-U, Scharf R. Huntorf CAES: More than 20 Years of Successful Operation. Orlando, Florida, USA: 2001.
- Caglayan DG, Weber N, Heinrichs HU, Linßen J, Robinius M, Kukla PA, Stolten D. Technical potential of salt caverns for hydrogen storage in europe. *Int J Hydrog Energy*. 2020;45(11):6793–6805. http://dx.doi.org/10.1016/j.ijhydene.2019. 12.161.
- Tarkowski R. Underground hydrogen storage: Characteristics and prospects. Renew Sustain Energy Rev. 2019;105:86–94. http://dx.doi.org/10.1016/j.rser.2019.01.051.
- Hashemi L, Blunt M, Hajibeygi H. Pore-scale modelling and sensitivity analyses of hydrogen-brine multiphase flow in geological porous media. *Sci Rep.* 2021;11(1):8348. http://dx.doi.org/10.1038/s41598-021-87490-7.
- Aubertin M, Julien MR, Servant S, Gill DE. A rate-dependent model for the ductile behavior of salt rocks. *Can Geotech J.* 1999;36(4):660–674. http://dx.doi.org/10. 1139/t99-033.
- Cristescu N, Hunsche U. Wiley New York; 1998. Time Effects in Rock Mechanics; vol. 350, http://dx.doi.org/10.1023/A:1007566002890.
- Hou Z. Mechanical and hydraulic behavior of rock salt in the excavation disturbed zone around underground facilities. *Int J Rock Mech Min Sci.* 2003;40(5):725–738. http://dx.doi.org/10.1016/S1365-1609(03)00064-9.
- Hampel A. The CDM constitutive model for the mechanical behavior of rock salt: Recent developments and extensions. In: *Proceedings of the 7th Conference* on Mechanical Behaviour of Salt, Paris. 2012:16–19. http://dx.doi.org/10.1201/ b12041.
- Heusermann S, Rolfs O, Schmidt U. Nonlinear finite-element analysis of solution mined storage caverns in rock salt using the LUBBY2 constitutive model. *Comput Struct.* 2003;81(8–11):629–638. http://dx.doi.org/10.1016/S0045-7949(02) 00415-7.
- Zhou H, Wang C, Han B, Duan Z. A creep constitutive model for salt rock based on fractional derivatives. *Int J Rock Mech Min Sci.* 2011;48(1):116–121. http://dx.doi.org/10.1016/j.ijrmms.2010.11.004.
- Jiang Q, Qi Y, Wang Z, Zhou C. An extended Nishihara model for the description of three stages of sandstone creep. *Geophys J Int.* 2013;193(2):841–854. http: //dx.doi.org/10.1093/gji/ggt028.
- Ma L-j, Liu X-y, Fang Q, Xu H-f, Xia H-m, Li E-b, Yang S-g, Li W-p. A new elasto-viscoplastic damage model combined with the generalized hoek–brown failure criterion for bedded rock salt and its application. *Rock Mech Rock Eng.* 2013;46:53–66. http://dx.doi.org/10.1007/s00603-012-0256-8.
- Deng J, Liu Y, Yang Q, Cui W, Zhu Y, Liu Y, Li B. A viscoelastic, viscoplastic, and viscodamage constitutive model of salt rock for underground energy storage cavern. *Comput Geotech*. 2020;119:103288. http://dx.doi.org/10.1016/j.compgeo. 2019.103288.
- Firme PA, Brandao NB, Roehl D, Romanel C. Enhanced double-mechanism creep laws for salt rocks. Acta Geotech. 2018;13:1329–1340. http://dx.doi.org/10.1007/ s11440-018-0689-7.
- Firme PA, Roehl D, Romanel C. Salt caverns history and geomechanics towards future natural gas strategic storage in Brazil. J Natl Gas Sci Eng. 2019;72:103006. http://dx.doi.org/10.1016/j.jngse.2019.103006.
- Dusseault M, Bachu S, Rothenburg L. Sequestration of CO2 in salt caverns. J Can Pet Technol. 2004;43(11). http://dx.doi.org/10.2118/04-11-04.
- Desai C, Varadarajan A. A constitutive model for quasi-static behavior of rock salt. J Geophys Res: Solid Earth. 1987;92(B11):11445–11456. http://dx.doi.org/10. 1029/JB092iB11p11445.

- Jin J, Cristescu N. An elastic/viscoplastic model for transient creep of rock salt. Int J Plast. 1998;14(1–3):85–107. http://dx.doi.org/10.1016/S0749-6419(97)00042-9.
- Khaledi K, Mahmoudi E, Datcheva M, Schanz T. Stability and serviceability of underground energy storage caverns in rock salt subjected to mechanical cyclic loading. *Int J Rock Mech Min Sci.* 2016;86:115–131. http://dx.doi.org/10.1016/j. ijrmms.2016.04.010.
- Munson DE, DeVries KL, Fossum AF, Callahan GD. Extension of the MD Model for Treating Stress Drops in Salt. Tech. Rep. sand–93-0377C; Sandia National Labs.; 1993.
- Hou Z, Wang Q, Xie L, Liu J, Zhang R. The hou's short-and long-term strength model, the Hou/Lux constitutive model for rock salt as well as their applications in storage cavern design. In: Underground Storage of CO2 and Energy. Balkema, Leiden: CRC Press; 2010:95–103. http://dx.doi.org/10.1201/b11592-20.
- Robson JD, Armstrong D, Cordell J, Pope D, Flint TF. Calibration of constitutive models using genetic algorithms. *Mech Mater.* 2024;189:104881. http://dx.doi. org/10.1016/j.mechmat.2023.104881.
- Yang C, Daemen J, Yin J-H. Experimental investigation of creep behavior of salt rock. Int J Rock Mech Min Sci. 1999;36(2):233–242. http://dx.doi.org/10.1016/ \$0148-9062(98)00187-9.
- Özşen H, Özkan İ, Şensöğüt C. Measurement and mathematical modelling of the creep behaviour of Tuzköy rock salt. Int J Rock Mech Min Sci. 2014;66:128–135. http://dx.doi.org/10.1016/j.ijrmms.2014.01.005.
- Bérest P, Béraud J, Gharbi H, Brouard B, DeVries K. A very slow creep test on an Avery Island salt sample. Rock Mech Rock Eng. 2015;48:2591–2602. http: //dx.doi.org/10.1007/s00603-015-0850-7.
- Anandarajah A, Agarwal D. Computer-aided calibration of a soil plasticity model. Int J Numer Anal Methods Geomech. 1991;15(12):835–856. http://dx.doi.org/10. 1002/nag.1610151202.
- Tolk A, Fowler J, Shao G, Yücesan E. Advances in Modeling and Simulation. Springer International Publishing; 2017 10, http://dx.doi.org/10.1007/978-3-319-64182-9, 978–973, Epub ahead of print.
- Schulte R, Karca C, Ostwald R, Menzel A. Machine learning-assisted parameter identification for constitutive models based on concatenated loading path sequences. *Eur J Mech A Solids*. 2023;98:104854. http://dx.doi.org/10.1016/j. euromechsol.2022.104854.
- 33. Bérest P, Brouard B, Gharbi H. Rheological and geometrical reverse creep in salt caverns. In: Mechanical Behavior of Salt VIII: Proceedings of the Conference on Mechanical Behavior of Salt. SALTMECH VIII, Leiden, the Netherlands: CRC Press/balkema; 2015:199–208. http://dx.doi.org/10.1201/b18393-27.
- Argyris J, Doltsinis IS, et al Constitutive modelling and computation of nonlinear viscoelastic solids. Part I: Rheological models and numerical integration techniques. *Comput Methods Appl Mech Engrg.* 1991;88(2):135–163. http://dx.doi. org/10.1016/0045-7825(91)90252-2.
- Kumar KR, Hajibeygi H. Influence of pressure solution and evaporate heterogeneity on the geo-mechanical behavior of salt caverns. *The Mechanical Behavior of Salt X*. 2022:407–420. http://dx.doi.org/10.1201/9781003295808.
- Ramesh Kumar K, Makhmutov A, Spiers CJ, Hajibeygi H. Geomechanical simulation of energy storage in salt formations. *Sci Rep.* 2021;11(1):19640. http: //dx.doi.org/10.1038/s41598-021-99161-8.
- Hunfeld L, Breunese J, Wassing B. The influence of a threshold stress for pressure solution creep on cavern convergence and subsidence behavior–An FEM study. In: *The Mechanical Behavior of Salt X.* CRC Press; 2022:577–589. http://dx.doi.org/ 10.1201/9781003295808.
- Eberhart R, Kennedy J. A new optimizer using particle swarm theory. In: MHS'95. Proceedings of the Sixth International Symposium on Micro Machine and Human Science. Ieee; 1995:39–43. http://dx.doi.org/10.1109/MHS.1995.494215.
- Gad AG. Particle swarm optimization algorithm and its applications: a systematic review. Arch Comput Methods Eng. 2022;29(5):2531–2561. http://dx.doi.org/10. 1007/s11831-021-09694-4.
- Pianosi F, Beven K, Freer J, Hall JW, Rougier J, Stephenson DB, Wagener T. Sensitivity analysis of environmental models: A systematic review with practical workflow. *Environ Model Softw.* 2016;79:214–232. http://dx.doi.org/10.1016/j. envsoft.2016.02.008.
- Rovetta A. Raiders of the lost correlation: a guide on using pearson and Spearman coefficients to detect hidden correlations in medical sciences. *Cureus*. 2020;12(11). http://dx.doi.org/10.7759/cureus.11794.