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DOI [10.1016/j.electacta.2024.144258](https://doi.org/10.1016/j.electacta.2024.144258)

Publication date  $2024$ 

Document Version Final published version

Published in Electrochimica Acta

## Citation (APA)

Phadke, S. A., de Jong, W., & Haverkort, J. W. (2024). An experimentally validated model for anodic H<sub>.</sub> O<br>production in alkaline water electrolysis and its implications for scaled-up operation. *Electrochimica Acta*, <sup>2</sup> 491, Article 144258. <https://doi.org/10.1016/j.electacta.2024.144258>

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Electrochimica Acta

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# An experimentally validated model for anodic  $H_2O_2$  production in alkaline water electrolysis and its implications for scaled-up operation



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## ARTICLE INFO

*Keywords:* Alkaline water electrolysis Anodic hydrogen peroxide Electrochemical reactor model Hydrogen Mole balance

## A B S T R A C T

The anodic co-production of hydrogen peroxide  $(H_2O_2)$  during alkaline water electrolysis has gained interest as a sustainable alternative for anthraquinone oxidation. However, electrochemical  $H_2O_2$  production is often studied with idealized laboratory setups to determine the  $H_2O_2$  formation kinetics. In this work, we perform the reaction with industrially relevant operating principles using a flow cell with separately recirculating anolyte and catholyte. We then fit the data to an analytical model that we derive based on mole balances that accounts for anodic generation, anodic oxidation, and bulk disproportionation of  $H_2O_2$ , as well as electrolyte volumes and electrode surface area. We performed experiments at 100, 200, and 300 mA cm-2 to derive values for the reaction system. At 200 mA cm<sup>-2</sup>, we found a generation rate of 0.037 mmol min<sup>-1</sup> cm<sup>-2</sup> (FE<sub>H<sub>2</sub>O<sub>2</sub> = 59%) and</sub> an anodic decomposition rate constant of 0.304 cm min-1, with a bulk disproportionation rate constant of 1.85  $\times$  10<sup>-3</sup> min<sup>-1</sup>. We successfully applied our model to two sources in literature to derive values for their systems as well. In all cases, the contribution of anodic oxidation of  $H_2O_2$  was found to be the larger loss mechanism in comparison to bulk disproportionation. Using the analytical model, we show that decreasing the reservoir volume is a simple way to increase the  $H_2O_2$  concentration over time. Further refinement of the model can be achieved through the use of mass transfer relationships based on electrolyzer geometries to describe the anodic oxidation of  $H_2O_2$  in the mole balance equations.

## **1. Introduction**

The use of electrochemistry, when powered by renewable energy resources, offers a promising pathway for the sustainable production of chemicals. One of these chemicals that requires a more sustainable pathway is hydrogen peroxide (H $_2$ O $_2$ ), which is used as a green oxidant in industries such as paper milling and textile bleaching [[1](#page-9-0)[,2\]](#page-9-1). However, it is currently produced by the anthraquinone oxidation process, which has a large energy demand of 17.6 kWh  $kg^{-1}$  due to high solvent use and separation requirements [[3](#page-9-2)[–5\]](#page-9-3). A more sustainable route would be via alkaline water electrolysis. During alkaline water electrolysis, we typically produce hydrogen gas  $(H_2)$  at the cathode and oxygen gas  $(O_2)$  at the anode [[6](#page-9-4)]. While research into the cathodic co-production of  $H_2O_2$  via oxygen reduction reaction is more commonly investigated, cathodically produced  $H_2O_2$  has some notable drawbacks. One drawback is that in order to effectively deliver oxygen to the cathode, a more complex gas-diffusion electron must be used, which can lead to mass transfer limitations. The other issue is that in cathodic  $H_2O_2$ production, the valuable  $H_2$  product is replaced, and the anode still produces low-value O $_{\rm 2}$  [\[7\]](#page-9-5). A more attractive alternative is to instead electrochemically produce  $H_2O_2$  at the anode by carefully selecting the

anode material and electrolyte [[8\]](#page-9-6). This form of paired electrolysis makes use of both the cathode, by producing a valuable, carbon-free energy carrier in  $H_2$ , and of the anode, by producing a high-value commodity chemical in  $H_2O_2$  alongside  $O_2$ .

The main difficulty of anodic  $H_2O_2$  production is that the potential required to produce  $H_2O_2$  is higher than that required to produce  $O_2$ . The thermodynamic half cell potential to produce  $H_2O_2$  under alkaline conditions as per Eq.  $(1)$  $(1)$  $(1)$  is 1.76 V versus the Reversible Hydrogen Electrode (RHE). Because the thermodynamic half cell potential to produce  $O_2$  $O_2$  is only 1.23 V versus RHE as per Eq. (2), the generation of  $H_2O_2$  at the anode is always in competition with the formation of O2 . While different anode materials may display different selectivities towards  $H_2O_2$  generation over  $O_2$  evolution, there is still no reported material with 100% Faradaic efficiency to  $H_2O_2$ .

Much of the research into anodic  $H_2O_2$  production focuses on finding more selective anode materials or on elucidating the reaction mechanism [\[9–](#page-9-7)[13\]](#page-9-8). In either case, experiments are typically performed in a one-compartment cell or in a separated H-cell configuration to study the fundamental anode performance over time [\[14](#page-9-9)[–16](#page-9-10)]. Experiments are also often performed with refreshed anolyte, or single-pass

<https://doi.org/10.1016/j.electacta.2024.144258>

Available online 9 April 2024 Received 30 November 2023; Received in revised form 16 March 2024; Accepted 8 April 2024

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anolyte in the case of flow cells, to avoid the effect of  $\rm H_2O_2$  loss mechanisms [\[17](#page-9-11)[,18](#page-9-12)]. A cation exchange membrane such as Nafion 117 is also frequently used, presumably to prevent  $H_2O_2$  crossover to the catholyte. However, this would be inadvisable for an alkaline electrolyzer system as it inhibits the transport of hydroxide (OH<sup>-</sup>) anions, which allow the reaction to proceed. In order to scale up a system for industrial electrochemical  $H_2O_2$  production, we must examine how the system behaves with more relevant industrial operating conditions, which include separately recirculating electrolyte flows, a porous separator material, and constant pH and temperature throughout the reaction.

For example, operating a flow cell with single-pass anolyte using high flow rates yields an anolyte product stream with very low  $H_2O_2$ concentration. This low concentration results in a more difficult downstream separation to extract the product. One could feed anolyte at lower flow rates to achieve a higher concentration, but the total  $H_2O_2$ production rate would then be lower. Such lower flow rates come with the drawback of the unavoidable loss mechanisms, namely the anodic oxidation of  $H_2O_2$  as per Eq. [\(3\)](#page-2-2) at 0.67 V versus RHE, and the disproportionation of  $H_2O_2$  in bulk electrolyte as per Eq. ([4](#page-2-3)). One solution would be recirculating the anolyte at high flow rates for some time before the separation stage, thus increasing  $H_2O_2$  concentration over time, easing downstream separation, and lowering cost. However, recirculating anolyte comes with the same unavoidable loss mechanisms. As  $\rm H_2O_2$ -charged anolyte recirculates past the anode, the chance for anodic oxidation of the  $\rm H_2O_2$  increases. Additionally, the increased time for recirculation increases the time for bulk disproportionation to occur in the anolyte reservoir, further decreasing the achieved  $H_2O_2$ concentration. Therefore, we must study how the network of reactions behaves in the relevant case. This network of reactions is shown schematically in [Fig.](#page-2-4) [1](#page-2-4).



 $H_2O_2 + 2 OH^- \rightarrow 2 H_2O + O_2 + 2 e^ E^{\circ} = 0.67$  V versus RHE (3)  $2 H_2O_2 \rightarrow 2 H_2O + O_2$ (4)



<span id="page-2-4"></span>Fig. 1. A simplified schematic of the reactions detailed in Eqs. [\(1\)](#page-2-0)–([4\)](#page-2-3) occurring in the anode chamber of the electrolyzer, with the anode wall on the left.

In this work, we study an industrially relevant electrolyzer system that separately recirculates anolyte and catholyte, and includes the standard porous separator material used in alkaline water electrolysis, Zirfon Perl UTP 500. We formulate a system of transient mole balance equations for the process and perform experiments to derive individual terms of the mole balance equations. The terms we derive experimentally are the generation rate of  $H_2O_2$  and the rate constant

**Table 1**

<span id="page-2-5"></span>



of bulk disproportionation of  $H_2O_2$  in the electrolyte. We then fit our experimental data to the analytical solution of the mole balance equations, which provides the rate constant for the oxidation of  $H_2O_2$ at the anode. We repeat this analysis using data from two references in literature that perform the reaction in a similar manner. Lastly, we simulate a change in design parameters to inform our recommendations on reactor and system design.

## **2. Analytical model**

## <span id="page-2-0"></span>*2.1. List of symbols*

<span id="page-2-1"></span>[Table](#page-2-5) [1](#page-2-5) lists the variables used in this work and their accompanying units.

## <span id="page-2-3"></span><span id="page-2-2"></span>*2.2. Mole balance equations*

We follow the analysis method outlined by Pickett involving two separate mole balances, one over the electrolyzer, and the other over the electrolyte reservoir [\[19](#page-9-13)]. In our analysis, we interchangeably use the terms ''electrolyzer'' and ''electrolyzer volume'' to denote the anode chamber and the volume of the anode chamber, because they are the system under investigation. A simplified diagram of the system is shown in [Fig.](#page-3-0) [2](#page-3-0). The mole balance over the electrolyzer is written in Eq. [\(5\)](#page-2-6),

<span id="page-2-6"></span>
$$
V_E \frac{dc_{out}}{dt} = \dot{Q}c_{in} - \dot{Q}c_{out} + SA - k_a Ac_{out} - k_b V_E c_{out}
$$
\n<sup>(5)</sup>

where  $V_E/L$  is the volume of the anode chamber,  $c_{out}(t)/mM$  is the concentration of H<sub>2</sub>O<sub>2</sub> out of the electrolyzer,  $t/m$ in is time,  $\dot{Q}/L$  min<sup>-1</sup> is the volumetric flow rate of electrolyte,  $c_{in}(t)/mM$  is the concentration of H<sub>2</sub>O<sub>2</sub> going into the electrolyzer,  $S/mmol$  min<sup>-1</sup> cm<sup>-2</sup> is the constant anodic generation rate of  $H_2O_2$ ,  $A/cm^2$  is the geometric anode surface area,  $k_a$ /cm min<sup>-1</sup> is the rate constant for anodic oxidation of H<sub>2</sub>O<sub>2</sub> as per Eq. ([3](#page-2-2)), and  $k_b / \text{min}^{-1}$  is the rate constant for bulk disproportionation as per Eq. [\(4\)](#page-2-3). Note that these units require the anodic oxidation term,  $k_a A$ , to be multiplied by a conversion factor of 0.001 L cm<sup>-3</sup>, which carries throughout.

A similar mole balance is expressed in Eq. ([6\)](#page-2-7) for the change in concentration across the electrolyte reservoir,

<span id="page-2-7"></span>
$$
V_R \frac{dc_{in}}{dt} = \dot{Q}c_{out} - \dot{Q}c_{in} - k_b V_R c_{in}
$$
\n<sup>(6)</sup>

where  $V_R/L$  is the reservoir volume. The total anolyte volume,  $V_A/L$ , is equal to  $V_E + V_R$ . This definition treats the small volume of electrolyte in the tubing between electrolyzer and reservoir as belonging to the reservoir, and is addressed in Section [3.1.](#page-3-1) The terms involving S and  $k_a$ appear only in the electrolyzer mole balance, while the term involving  $k<sub>h</sub>$  appears in both balances, as bulk disproportionation can occur everywhere.



<span id="page-3-0"></span>**Fig. 2.** A simplified diagram of the overall system. The dashed boxes indicate the boundaries of the mole balance equations.

## *2.3. Assumptions*

We assume a perfectly mixed anode chamber due to bubble mixing and flow such that the outlet concentration of the electrolyzer,  $c_{out}(t)$ , is the concentration everywhere in the anode chamber, including the anode surface. This assumption is acceptable for systems with low single-pass conversion rates, which for our system was between 0.9% and 3.0%, validating the assumption. We similarly assume a perfectly mixed anolyte reservoir, which we achieve experimentally via magnetic stirring. We also assume that  $V_A$ ,  $V_E$ ,  $V_R$ , and  $\dot{Q}$  are constant.

In Eq. ([5](#page-2-6)), we express the anodic oxidation of  $H_2O_2$  as a surface reaction described by a first order rate equation using a homogeneous  $H<sub>2</sub>O<sub>2</sub>$  concentration in the electrolyzer. This is a simplifying assumption for a surface concentration that would actually involve a mass transfer term, [[6](#page-9-4)] but it allows us to more easily express the reaction term without involving more complex mass transfer relationships for various electrolyzer geometries. Incidentally, a mass transfer limited reaction would also be expected to be a first order reaction, so this generalized form may cover more than one possible situation.

We assume that only the reactions in Eqs.  $(1)$  $(1)$  $(1)$ – $(3)$  take place at the anode. We further assume that  $S$  is constant, although in reality there will be a ratio of how much current goes towards  $H_2O_2$  generation versus  $H_2O_2$  oxidation,  $O_2$  evolution, or any other side reactions at the anode. Finally, we assume that there is no loss of  $H_2O_2$  due to crossover into the catholyte. This was observed experimentally and further examined in Section [4.4.](#page-6-0)

#### *2.4. Solutions*

<span id="page-3-7"></span>Eq. ([6](#page-2-7)) can be rearranged to solve for  $c_{out}(t)$  as a function of  $c_{in}(t)$ , and then differentiated to find an expression for  $dc_{out}(t)/dt$  as a function of  $c_{in}(t)$ . These expressions can be used to eliminate  $c_{out}$  from Eq. ([5](#page-2-6)), leading to the second order, non-homogeneous differential equation in Eq. [\(7\)](#page-3-2),

$$
\frac{d^2c}{dt^2}+\left(\frac{\dot{Q}}{V_E}+\frac{\dot{Q}}{V_R}+\frac{k_aA}{V_E}+2k_b\right)\frac{dc}{dt}+\left(\dot{Q}\left(\frac{k_aA}{V_EV_R}+\frac{k_b}{V_R}+\frac{k_b}{V_E}\right)\right.
$$

<span id="page-3-4"></span><span id="page-3-3"></span><span id="page-3-2"></span>*Electrochimica Acta 491 (2024) 144258*

$$
+\frac{k_a A k_b}{V_E} + k_b^2\bigg)c = \frac{SA\dot{Q}}{V_E V_R} \tag{7}
$$

where we have dropped the subscript of  $c_{in}(t)$  and examine simply  $c(t)/mM$ , the concentration of  $H_2O_2$  in the anolyte reservoir over time.

We make a final simplification of Eq. [\(7\)](#page-3-2) for the case that the flow rate,  $\dot{Q}$ , is very large. The full solution to Eq. [\(7\)](#page-3-2) and the justification of the high flow rate assumption are shown in [Appendices](#page-8-0) [A](#page-8-0) and [B.](#page-9-14) In the case of large  $\dot{Q}$ , the  $\dot{Q}$  term cancels out and we obtain the first order differential equation in Eq. [\(8\)](#page-3-3).

$$
\frac{dc}{dt} = \frac{SA}{V_E + V_R} - \frac{k_a A}{V_E + V_R}c - k_b c
$$
\n(8)

Using the initial condition that  $c(t) = 0$  at  $t = 0$ , we reach the final result in Eq. ([9\)](#page-3-4).

$$
c = \frac{SA}{k_a A + k_b (V_E + V_R)} \left( 1 - \exp \left( - \left( \frac{k_a A}{V_E + V_R} + k_b \right) t \right) \right)
$$
(9)

As  $t$  approaches  $\infty$ , we find the expected steady state concentration in Eq. ([10\)](#page-3-5), which takes the form of the  $H_2O_2$  generation term over a weighted sum of the  $H_2O_2$  decomposition terms.

<span id="page-3-5"></span>
$$
c_{\text{Steady State}} = \frac{SA}{k_a A + k_b (V_E + V_R)}\tag{10}
$$

We can also define an extent of reaction,  $0 \le \xi < 1$ , such that  $\xi c(t)$ is the fraction of the steady state concentration reached in the anolyte. Using this definition and solving for  $t_{\xi}$ , the time it takes to reach  $\xi$ fraction of the steady state concentration, we arrive at Eq. ([11\)](#page-3-6).

<span id="page-3-6"></span>
$$
t_{\xi} = \frac{-\ln(1-\xi)}{\left(\frac{k_a A}{V_E + V_R} + k_b\right)}\tag{11}
$$

#### **3. Methods**

#### *3.1. Materials*

<span id="page-3-1"></span>Experiments were performed using a flow cell constructed of lasercut PMMA sheets with silicone and EPDM gaskets layered in between, compressed together with bolts. Titanium plates were used as current collectors, and the electrodes were kept at a distance of 0.7 cm to the separator. The anode and cathode chamber dimensions were 3 cm wide by 4 cm tall by 0.7 cm deep ( $V_E$  = 0.0084 L). The cathode was nickel fiber felt (12 cm<sup>2</sup>, geometric) from Hebei Aegis Metal Materials Co., Ltd, 0.4 mm thickness, with 40 μm fiber diameter and 60% porosity. The anode was boron-doped diamond (2.5 cm  $\times$  4 cm = 10 cm<sup>2</sup>, geometric) from NeoCoat on a niobium substrate, with 5 μm thick, pdoped, 2500 ppm boron doping, polycrystalline coating. The separator used was the porous diaphragm, Zirfon Perl UTP 500 (Agfa) with a thickness of 500  $\mu$ m. The electrolyte used was 1 M Na<sub>2</sub>CO<sub>3</sub> (Merck-Sigma, ACS Reagent,  $\geq$  99.5%, powder or granules) plus 11 g L<sup>-1</sup> (approximately 90 mM)  $Na<sub>2</sub>SiO<sub>3</sub>$  (Merck-Sigma, SKU 307815). Flow was maintained at 0.1 L min-1 using a Longer BT100-3J peristaltic pump with DG15-24 two-channel pump head, with the anolyte and catholyte recirculated separately. The tubing for anolyte held a volume of 8.04  $\text{cm}^3$ , which was negligible compared to the anolyte volume of  $V_A$  = 0.4 L. The anolyte reservoir was magnetically stirred to ensure good mixing.

Because  $S$ ,  $k_a$ , and  $k_b$  are expected to vary based on temperature, pH, electrolyte composition, presence of a stabilizer, etc., these parameters were kept constant across all experiments. The anolyte pH was maintained between 13.25 and 13.10, just above the base electrolyte pH of 13.10, by manual monitoring and addition of aliquots of 5 M NaOH (Merck-Sigma, ACS Reagent,  $\geq$  97.0%) solution. The high NaOH concentration served to lower the amount of anolyte volume change upon NaOH addition. The overall combination of reaction, sampling, NaOH addition, and any possible liquid flux through the porous separator resulted in overall volume changes of *<* 10% over 7 h across all experiments. The temperature was controlled to be just



<span id="page-4-0"></span>**Fig. 3.** (a) Photo of the experimental setup with (1) power supply (2) two-channel peristaltic pump (3) pH and temperature sensors (4) Anolyte reservoir with magnetic stirring and external container for cold water bath (5) electrochemical flow cell with cathode compartment near and anode compartment away (6) catholyte reservoir. (b) Plot of the maintained pH and temperature of the anolyte reservoir for a typical experiment with recirculating flows. The vertical spikes in pH were the moments of NaOH solution addition, and are required less frequently as the pH of the catholyte slowly increases during the experiment.

under room temperature, at approximately  $16 \pm 1$  °C, by immersing the anolyte reservoir in a cold water bath. The anolyte pH and temperature were measured using a Prominent PHEP-H 314 SE sensor and a Prominent Pt 100-SE sensor, respectively. Catholyte was recirculated for all experiments, with no maintenance of pH or temperature. Fixed current (galvanostatic operation) was supplied at 1.0, 2.0, or 3.0 A in twoelectrode operation using an OWON SPE6103 power supply. [Fig.](#page-4-0) [3\(](#page-4-0)a) shows a photo of the experimental setup and [Fig.](#page-4-0) [3\(](#page-4-0)b) shows the typical curves for pH and temperature in the anolyte reservoir over time during an experiment with recirculating flows.

#### *3.2. H2O<sup>2</sup> quantification*

<span id="page-4-5"></span>The  $H_2O_2$  concentration was quantified using the potassium per-manganate (KMnO<sub>4</sub>) titration method as outlined by Gill et al. [[20\]](#page-9-15). In short, the method comprises of taking a sample of electrolyte (typically 2.5 mL) and immediately acidifying with equal volume of a 1:5 dilution of H2SO<sup>4</sup> (Merck-Sigma, 95%–98%, ACS Reagent) in milli-Q water (Merck-Millipore, resistivity = 18.2 M $\Omega$  cm). Electrolyte samples from both anolyte and catholyte were taken from the reservoirs at regular intervals. For single-pass experiments, electrolyte was sampled directly from the reactor outflow. The titrant used was a 2 mM solution of KMnO<sup>4</sup> , diluted ten-fold from stock solution (Merck-Sigma, 0.02 M, standardized against oxalate, Titripur). To start, three drops of 2 mM KMnO<sup>4</sup> solution were added to the magnetically stirred, acidified sample until the pink color disappeared (starting the reaction). These three drops defined the limit of quantification for a 2.5 mL sample to be 0.3 mM. The titrant was further added drop-wise until a light-pink color remained in the sample, indicating the titration endpoint.

#### *3.3. Determination of*

<span id="page-4-3"></span>The majority of literature shows that for fresh electrolyte passed across the anode, the generation of  $H_2O_2$  tends to be constant over time for a fixed operating potential  $[17,18]$  $[17,18]$  $[17,18]$  $[17,18]$ . This observation could also be reasoned for an electrode that is very stable over time, such as boron-doped diamond. So for a corresponding fixed current density, this formation rate can be expressed as,

<span id="page-4-2"></span>
$$
S = \frac{\dot{Q}c_{SinglePass}}{A} = \frac{j}{n\mathcal{F}} \text{FE}_{\text{H}_2\text{O}_2} \tag{12}
$$

where  $c_{SinglePass}$  is the  $H_2O_2$  concentration achieved in electrolyte flown in single-pass over the anode,  $j$  is the current density,  $n=2$  is the ratio of moles of electrons to moles of  $H_2O_2$ ,  $\mathcal F$  is Faraday's constant, and  $FE_{H_2O_2}$  is the Faradaic efficiency towards  $H_2O_2$ . The generation rate,  $S$ , for a single current density can be experimentally quantified by flowing electrolyte in single-pass at a high flow rate and measuring the outlet  $H_2O_2$  concentration immediately. The high flow rate and quick measurement ensure that the residence time for anodic oxidation and the time for bulk disproportionation are low enough to be negligible. [Fig.](#page-4-1) [4](#page-4-1) shows the schematic of the flow setups of the experiments. The first expression in Eq.  $(12)$  $(12)$  can be used to find a value for S from the experiment, while the second can be used to calculate the Faradaic efficiency.

#### *3.4. Determination of*

<span id="page-4-4"></span>The experimental determination of the rate constant for bulk disproportionation,  $k_b$ , required first running the electrolyzer with recirculating flow in order to charge the anolyte with  $H_2O_2$ . After two hours of operation with pH and temperature maintained, the electrolyzer



<span id="page-4-1"></span>Fig. 4. Diagram of the different flow configurations (not to scale). The solid arrow leaving the anode chamber and returning to the anolyte reservoir represents recirculating flow, while the dashed arrow leaving the anode chamber towards a separate collection vessel represents single-pass flow. For experiments using recirculating flow, anolyte is sampled from the reservoir. For experiments using single-pass flow, anolyte is sampled directly from the outlet of the anode chamber, not the collection vessel.

contents were drained into the reservoirs, and samples of anolyte were periodically taken for  $H_2O_2$  quantification. This procedure was performed for three different current densities in order to compare concentration curves with different initial concentration values.

## *3.5. Numerical fitting of*

Because the anodic oxidation of  $\rm H_2O_2$  is an electrochemical reaction,  $k_a$  is expected to increase as the cell potential increases. However, due to its lower thermodynamic half cell potential of  $E^{\circ} = 0.67$  V versus RHE compared to the generation of  $H_2O_2$  at 1.76 V versus RHE, these two reactions are in direct competition. As such,  $k_a$  cannot be independently measured. Instead, after experimentally deriving values for  $S$  and  $k_h$  as described in Sections [3.3](#page-4-3) and [3.4,](#page-4-4) the electrolyzer is run for seven hours with recirculating flow. Samples of electrolyte are taken for  $H_2O_2$  quantification as described in Section [3.2.](#page-4-5) With the known values of  $V_E$  and  $V_R$ , the data points of  $c(t)$  for a given current density are fitted to Eq. ([9](#page-3-4)) in Python using the 'curvefit' function from the SciPy module. This function runs a non-linear least squares regression to find the best fit. Fitted parameters were given no constraints and only supplied with an initial guess to ease computation.

#### **4. Results and discussion**

#### *4.1. H2O<sup>2</sup> generation*

The results of the single-pass flow experiments are shown in [Fig.](#page-5-0) [5\(](#page-5-0)a). Using the average concentrations at each of the three current densities, we use Eq. ([12\)](#page-4-2) to calculate  $S = 0.017, 0.037,$  and 0.054 mmol min<sup>-1</sup> cm<sup>-2</sup> at 100, 200, and 300 mA cm<sup>-2</sup>, respectively. The calculated Faradaic efficiencies at each of the three current densities were similar, with values of 54%, 59%, and 58% for 100, 200, and 300 mA cm<sup>-2</sup>, respectively. These constant  $H_2O_2$  generation rates and the calculated Faradaic efficiencies are consistent with the literature report of boron-doped diamond materials by Mavrikis et al. using refreshed electrolyte [\[17](#page-9-11)]. At the same current densities in 1 M carbonate/bicarbonate electrolyte, they report  $H_2O_2$  generation rates between 0.016 and 0.076 mmol  $min^{-1}$  cm<sup>-2</sup> and Faradaic efficiencies between 50% and 70% for a set of boron-doped diamond anodes.

## *4.2. H2O<sup>2</sup> loss via bulk disproportionation*

The results of the experiments for  $k<sub>b</sub>$  quantification are shown in [Fig.](#page-5-0) [5](#page-5-0)(b). Each of the curves represent a batch of anolyte that was charged with  $H_2O_2$  for two hours at 100, 200, or 300 mA cm<sup>-2</sup> with separately recirculating flows. The power supply was then switched off, its contents drained, and the anolyte concentration was measured over time. Literature indicates that the disproportionation of  $H_2O_2$  should be a first order decomposition reaction [[21](#page-9-16)]. Examining the data, we see a constant slope on a semi-log plot for all three data sets, indicating a first order decomposition reaction with an average rate constant of 1.85  $\times$  10<sup>-3</sup> min<sup>-1</sup>. This value is consistent with the value for bulk disproportionation found by Li et al. who used an electrolyte of  $2 \text{ M KHCO}_3$ at room temperature, and Lee et al. who studied  $H_2O_2$  decomposition for a range of electrolytes including  $\text{Na}_2\text{CO}_3$  with  $\text{Na}_2\text{SiO}_3$  stabilizer [[21](#page-9-16)[,22](#page-9-17)].

#### *4.3. Full system - Fitting*

<span id="page-5-1"></span>After deriving  $S$  and  $k_b$ , we now perform seven hour experiments with separately recirculating electrolyte, a porous Zirfon separator, and with anolyte pH and temperature maintained. [Fig.](#page-6-1) [6](#page-6-1) shows the accumulation of  $H_2O_2$  over time in the system, along with the fit of Eq. ([9](#page-3-4)). The fitted values of  $k_a$  are 0.136, 0.304, and 0.349 cm min<sup>-1</sup> at 100, 200, and 300 mA cm-2, respectively. The modified anodic decomposition term as it appears in Eq. ([8](#page-3-3)),  $(k_a A)/(V_E + V_R)$ , was calculated to be 3.40  $\times$  10<sup>-3</sup>, 7.59  $\times$  10<sup>-3</sup>, and 8.73  $\times$  10<sup>-3</sup> min<sup>-1</sup>, in order of increasing current density. These values are all greater than  $k_b = 1.85 \times 10^{-3}$  min<sup>-1</sup>, indicating that the anodic oxidation of H<sub>2</sub>O<sub>2</sub> in the anolyte was the dominant loss mechanism in our system. The fit appears to match the experimental results well, though there is a slight underprediction of the concentration at  $t < 240$  min and a slight overprediction of the steady state concentration at  $t > 360$  min. This likely originates from our definition of the constant generation of  $\rm H_2O_2$ . In the case of a competing surface reaction,  $S$  would no longer be constant, but be expected to decrease over time as  $c(t)$  increased over time, due to the increased rate of anodic oxidation. Nevertheless, the fit is good and displays the expected trend of increasing  $k_a$  with increasing current density.



<span id="page-5-0"></span>Fig. 5. (a) The constant generation of H<sub>2</sub>O<sub>2</sub> under single-pass flow for a given current density. The dashed lines indicate the average measured concentrations over one hour of 1.68, 3.65, and 5.40 mM at 100, 200, and 300 mA cm<sup>-2</sup>, respectively. These average concentrations are used to calculate  $S = 0.017$ , 0.037, and 0.054 mmol min<sup>-1</sup> cm<sup>-2</sup>, in order of increasing current density. (b) Comparison in semi-log scale of the homogeneous decomposition of  $H_2O_2$  in anolyte from different starting concentrations without applied current. These starting concentrations were achieved by operating the electrolyzer with recirculating electrolyte flow for two hours at different current densities. Dashed lines are linear regressions of the data sets. These data sets share a constant slope, indicating a first order bulk disproportionation reaction with an average rate constant of  $k_b = 1.85 \times 10^{-10}$  $10^{-3}$  min<sup>-1</sup>.



<span id="page-6-1"></span>Fig. 6. Seven-hour experiments for the anodic production of  $H_2O_2$  with recirculating anolyte. The dashed lines show Eq. ([9](#page-3-4)) using fitted  $k_a$  values of 0.136, 0.304, and 0.349 cm  $min^{-1}$  for 100, 200, and 300 mA  $cm^{-2}$ , respectively.

## *4.4. Exclusion of crossover effects*

<span id="page-6-0"></span>It was observed that the  $H_2O_2$  concentration in the catholyte was always at or below the limit of quantification (0.3 mM as mentioned in Section [3.2\)](#page-4-5). This indicated that either the decomposition of  $H_2O_2$ in the catholyte far outpaced the diffusive flux through the Zirfon separator, or that the diffusive flux itself was negligible. At pH greater than the pKa of  $H_2O_2$  (11.7), the  $H_2O_2$  exists primarily in its deprotonated form as  $HO_2^-$ . This anion experiences a force of electric migration towards the anode, which is in the opposite direction of the diffusive flux. We therefore reason, as we operate at pH *>* 13, that nearly all of the anodically produced  $\rm H_2O_2$  is retained in the anolyte. To confirm this, we modify Eq. [\(5\)](#page-2-6) to add a term to account for  $H_2O_2$  crossover,  $-k_c A_{sep} c_{out}(t)$ , where  $A_{sep}$  is the separator surface area. The  $k_c$  term can be calculated by analogy to Fick's law for diffusion across the separator, assuming a concentration of zero on the cathode side, as per Eq. ([13\)](#page-6-2),

$$
k_c = \frac{\mathcal{D}}{L_{sep}}\tag{13}
$$

where  $k_c$ /cm min<sup>-1</sup> is the rate constant for crossover,  $\mathcal D$  is the effective diffusion coefficient, and  $L_{sep}$  is the thickness of the separator. Using the values of our setup ( $A_{sep}$  = 12 cm<sup>2</sup> and  $L_{sep}$  = 0.05 cm) and assuming a typical liquid diffusion coefficient at ambient temperature of  $\mathcal{D} = 1 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$ , we find  $k_c = 2.0 \times 10^{-4} \text{ cm min}^{-1}$ . The modified crossover term as it would appear in Eq. [\(8\)](#page-3-3),  $(k_c A_{sep})/(V_E + V_R)$ , was calculated to be  $3.60 \times 10^{-4}$  min<sup>-1</sup>. Comparing this value to the anodic decomposition terms that we found in Section [4.3](#page-5-1) (all  $> 3.40 \times 10^{-3}$ )  $min<sup>-1</sup>$ , we see that any effect of crossover is negligible in comparison to the anodic oxidation in the anode chamber. The modified crossover term is also negligible in comparison to the bulk decomposition rate constant of  $1.85 \times 10^{-3}$  min<sup>-1</sup>.

## *4.5. Extension to literature data*

One of the strengths of the outlined analytical model is that knowledge of the precise details of the system are not required. Neither the specific reaction mechanism for  $H_2O_2$  generation, the particular electrolyte composition, nor the electrolyzer geometry have to be taken into consideration. The only relevant parameters are the physical dimensions (A,  $V_E$ , and  $V_R$ ), the overall generation rate (S), and the rate constants ( $k_a$  and  $k_b$ ). As such, the model remains versatile. We demonstrate this versatility by examining two sources from literature, Pangotra et al. [\[23](#page-9-18)] and Li et al. [[22\]](#page-9-17), and use their data to calculate rate constants as per their experimental setups.

The setup of Pangotra et al. uses a  $10 \text{ cm}^2$  anode and an electrolyte flow rate of  $0.1$  L min<sup>-1</sup>, and is very similar to our own. The main difference is that they use Nafion 117 as a separator and keep their anolyte in an ice bath to maintain the temperature. Using their data, we found a  $k_b$  value of 5.70  $\times$  10<sup>-4</sup> min<sup>-1</sup> for 2 M K<sub>2</sub>CO<sub>3</sub> with 90 mM  $Na<sub>2</sub>SiO<sub>3</sub>$  electrolyte. This value is about three times lower than for our system, which is consistent with a lowered reaction rate due to lower temperatures. We fitted their data for both  $S$  and  $k_a$  at the same current densities as we use, and the fit is shown in [Fig.](#page-6-3) [7\(](#page-6-3)a). The fitted curve shows excellent agreement, likely due to the additional free parameter available for fitting,  $S$ . [Table](#page-7-0) [2](#page-7-0) lists the computed values for all of the experimental data sets analyzed. The values of  $S$  from Pangotra et al. are comparable to ours, but the  $k_a$  values are much higher, particularly at 300 mA cm-2. This leads to their overall lower steady state concentrations and their observed optimal current density of 200 mA cm-2 .

<span id="page-6-4"></span><span id="page-6-2"></span>The setup used by Li et al. was not a flow setup but rather a separated batch reactor system. The anolyte was magnetically stirred to ensure mixing. Li et al. operate their system potentiostatically, but observed a relatively constant current at each potential, allowing our analysis to continue. While they do not maintain pH or temperature, they operate at low currents of *<* 35 mA and observe a very small pH change from 8.31 to 8.68. We therefore assume that the temperature and pH have not changed significantly over the course of the experiment, such that the model can still be applied. The analytical model can be reformulated by simply setting  $V_R$  and  $\dot{Q}$  equal to zero, which causes Eq. [\(6\)](#page-2-7) to cancel out entirely. The resulting mole balance across the electrolyzer takes the following form.



<span id="page-6-3"></span>Fig. 7. Fits to data from literature sources, with open symbols to indicate data points not from our work. See [Table](#page-7-0) [2](#page-7-0) for a summary of parameter values. (a) Dashed lines showing the fit of Eq. [\(9\)](#page-3-4) to the data of Pangotra et al. [\[23\]](#page-9-18). Both S and  $k_a$  were fitted to this data using  $k_b$  from their data. (b) Dashed lines showing the fit of Eq. ([15](#page-7-1)) to the data of Li et al. [[22\]](#page-9-17). Only  $k_a$  was fitted to this data using  $S$  and  $k_b$  from their data.

The solution to Eq. [\(14](#page-6-4)), replacing  $c_{out}$  with c, is shown in Eq. [\(15](#page-7-1)),

$$
c = \frac{SA}{k_a A + k_b V_E} \left( 1 - \exp\left( -\left(\frac{k_a A}{V_E} + k_b\right)t \right) \right)
$$
(15)

where  $V_E$  = 0.06 L is the anolyte volume. Eq. ([15\)](#page-7-1) takes the same overall form as Eq. [\(9\)](#page-3-4), but setting  $V_R$  equal to 0. This is a result of all reactions taking place in the same batch reactor, without a separate reservoir. Li et al. [\[22](#page-9-17)] arrive at a similar expression to Eqs. ([9](#page-3-4)) and ([15\)](#page-7-1) and fit it successfully to their data. However, they combine their  $k_a$  and  $k_b$  terms into a single parameter and neglect the solution volume and electrode surface area. Our more versatile analytical model based on mole balances successfully accounts for these differences, and the fit of Eq. [\(15](#page-7-1)) to their data is shown in [Fig.](#page-6-3) [7\(](#page-6-3)b). Our fit matches well to the experimental data obtained by Li et al. However, the data sets do not continue until a very clear steady state, so we cannot comment on any underprediction or overprediction of the model with respect to time. Li et al. performed a similar experiment to quantify the contribution of bulk disproportionation as we did and found  $k<sub>b</sub>$  $= 1.83 \times 10^{-3}$  min<sup>-1</sup> [\[22](#page-9-17)]. This value is very close to the value for our system, despite using a different electrolyte of 2 M KHCO<sub>3</sub>. The values of  $S$  (calculated using data from Li et al.) are significantly lower than our values due to the lower total current of their experiments with a  $0.5 \text{ cm}^2$  anode, but follow the predicted trend of increasing with increasing current density (see [Table](#page-7-0) [2](#page-7-0)). However, the  $k_a$  values (fitted) are quite large, and are comparable to those of Pangotra et al. who operate at much higher current densities. These large anodic decomposition rate constant values may also have led to the lower concentrations seen in the experiments of Li et al. This result highlights the drawback of running such a system in batch reactor, as there is a large opportunity for any produced  $\rm H_2O_2$  to oxidize further. In contrast, a flow cell system has a lower residence time of  $\rm H_2O_2$  in the electrolyzer, thereby lowering the chance for anodic oxidation of  $H<sub>2</sub>O<sub>2</sub>$ .

### *4.6. Model validation and implications for scaled-up operation*

The scaled-up electrochemical process to produce  $H_2O_2$  with high flow rates faces the obstacle of low single-pass conversion. A low  $H_2O_2$ concentration makes later separation and purification more difficult, and low flow rates result in overall low product yield, thus necessitating anolyte recirculation to charge it with higher concentrations of  $\mathrm{H}_2\mathrm{O}_2$ . The objective of the process design should then be to maximize  $H_2O_2$ concentration in the anolyte stream in the minimum required time. While  $S$ ,  $k_a$ , and  $k_b$  are dependent on the electrode–electrolyte system chosen,  $A, V_E, V_R$ , and  $\dot{Q}$  can all be easily changed as desired to fit the requirements of a separation system or target production rate.

To validate our model's ability to predict the change in  $c(t)$  with varying  $V_E$  or  $V_R$ , we perform experiments at 200 mA cm<sup>-2</sup> and overlay the predicted curves using fixed parameter values of  $S$ ,  $k_a$ , and  $k_b$  for different  $V_E$  and  $V_R$ . The results of these experiments are shown in [Fig.](#page-7-2) [8.](#page-7-2) The model slightly underpredicts the effect of increasing the anolyte reservoir volume, and largely misses the effect of changing the electrolyzer volume. The data gathered with  $V_F = 0.0036$  L was obtained by assembling the electrolyzer using a thinner PMMA plate for the anode chamber, altering the cell geometry and bringing the anode closer to the separator. Eq. ([9](#page-3-4)) predicts that changing  $V_E$  while keeping  $V_A$  constant should have no change on the accumulated  $H_2O_2$ concentration. However, it appears that modeling the anodic oxidation of  $H_2O_2$  as a surface reaction using a homogeneous concentration value across the electrolyzer chamber was insufficient to model the system. It is likely that the effect of cell geometry is too significant to be captured by a first order expression using a homogeneous concentration. Future refinement of this model should instead use a mass transfer expression based on electrolyzer geometry to find a surface  $H_2O_2$  concentration value and examine different electrolyzer geometries and current densities to validate the expression.

**Table 2**

<span id="page-7-1"></span>Summary of parameter values from fitted data. Entries marked ''(fit)'' were fitted using Eq. ([9](#page-3-4)) or ([15\)](#page-7-1), while the others were derived from available data.  $E_{Cell}$  indicates the full cell potential.

<span id="page-7-0"></span>

This work	A/cm <sup>2</sup>	$V_R/L$	$V_F/L$	$Q/L$ min <sup>-1</sup>
	10	0.3916	0.0084	0.1
	$S/mmol$ min <sup>-1</sup> cm <sup>-2</sup>		$k_a$ (fit)/cm min <sup>-1</sup>	$k_{h}/\text{min}^{-1}$
100 mA $cm^{-2}$		0.017	0.136	$1.85 \times 10^{-3}$
$(E_{Cell} \sim 5.5 \text{ V})$				
$200 \text{ mA cm}^{-2}$		0.037	0.304	$1.85 \times 10^{-3}$
$(E_{cell} \sim 7.5 \text{ V})$				
300 mA $cm^{-2}$		0.054	0.349	$1.85 \times 10^{-3}$
$(E_{\text{Cell}} \sim 9.1 \text{ V})$				
Pangotra et al. [23]	A/cm <sup>2</sup>	$V_R/L$	$V_F/L$	$\dot{O}/L$ min <sup>-1</sup>
	10	0.191024	0.008976	0.1
	S (fit)/mmol min <sup>-1</sup> cm <sup>-2</sup>		$k_a$ (fit)/cm min <sup>-1</sup>	$k_{h}/\text{min}^{-1}$
100 mA $cm^{-2}$		0.016	0.423	$5.7 \times 10^{-4}$
$(E_{cell} \sim 4.4 \text{ V})$				
$200$ mA $cm^{-2}$		0.036	0.641	$5.7 \times 10^{-4}$
$(E_{Cell} \sim 5.9 V)$				
300 mA $cm^{-2}$		0.069	1.830	$5.7 \times 10^{-4}$
$(E_{\text{Cell}} \sim 6.7 \text{ V})$				
Li et al. [22]	A/cm <sup>2</sup>	$V_R/L$	$V_F/L$	$\dot{O}/L$ min <sup>-1</sup>
	0.5	$\mathbf 0$	0.06	$\Omega$
	$S/mmol$ min <sup>-1</sup> cm <sup>-2</sup>		$k_a$ (fit)/cm min <sup>-1</sup>	$k_{h}/\text{min}^{-1}$
2.3 V vs. RHE	$6.37 \times 10^{-3}$		0.456	$1.83 \times 10^{-3}$
$({\sim}25$ mA cm <sup>-2</sup> )				
2.5 V vs. RHE	$8.88 \times 10^{-3}$		0.707	$1.83 \times 10^{-3}$
$({\sim}42 \text{ mA cm}^{-2})$				
2.7 V vs. RHE		0.013	1.113	$1.83 \times 10^{-3}$
$({\sim}69 \text{ mA cm}^{-2})$				



<span id="page-7-2"></span>**Fig. 8.** Experimental validation of the model for different  $V_F$  and  $V_R$  at 200 mA cm-2. The lines show the predicted concentration curves for the given parameters. The predicted concentrations for the base case (black line) and the lowered  $V_E$  case (green line) overlap completely because the total anolyte volume,  $V_A$ , was not changed. The prediction for changing  $V_R$  underpredicts the experiment, and the prediction for changing  $V_E$  does not match.

Because the effect of changing  $V_R$  was predicted relatively well, we extend the predictions to other values of  $V_R$ , using a base case with  $V_E$  $= 0.0084$  L and  $V_R = 0.3916$  L as per our experimental setup. These predictions are shown in [Fig.](#page-8-1) [9](#page-8-1)(a). As expected by examination of Eq. [\(10](#page-3-5)), decreasing  $V_R$  leads to higher steady state concentrations. [Fig.](#page-8-1) [9\(](#page-8-1)a) also shows that decreasing  $V_R$  leads to higher concentrations of  $H_2O_2$ earlier in time as the anolyte is charged with  $H_2O_2$ . However, due to the large change in anolyte volume with  $V_R$ , the trend for the total number of moles is reversed. [Fig.](#page-8-1) [9\(](#page-8-1)b) shows the predicted accumulation of  $H_2O_2$  in moles, where a low  $V_R$  achieves a correspondingly low amount



<span id="page-8-1"></span>**Fig. [9](#page-3-4).** Simulated results using Eq. (9) at 200 mA cm<sup>-2</sup> with changing reservoir volume, with  $V_R = 0.3916$  L and  $V_F = 0.0084$  L. (a) The concentration of H<sub>2</sub>O<sub>2</sub> reaches a higher steady state value more quickly with decreasing  $V_R$ . As  $V_R$  approaches 0, the predicted curve approaches the case of a batch reactor. (b) Simulated results for the amount of H<sub>2</sub>O<sub>2</sub> in mmol at 200 mA cm<sup>-2</sup> with changing reservoir volume,  $V_R$ . Because the total electrolyte volume decreases strongly with decreasing  $V_R$ , the total number of moles produced also decreases

of  $H_2O_2$ , reversing the trend seen in [Fig.](#page-8-1) [9\(](#page-8-1)a). Therefore, the target H2O<sup>2</sup> production rate must be considered in tandem with the system geometry to find the optimal design parameters and recirculation time. This could be accomplished by setting a desired extent of reaction,  $\xi$ , or a desired reaction time,  $t_{\xi}$ , and then optimizing for the number of moles of  $H_2O_2$ .

## **5. Conclusions**

The large-scale electrochemical production of  $\rm H_2O_2$  is hampered by low single-pass conversion, and thus requires electrolyte recirculation to charge the anolyte with enough  $\mathrm{H}_2\mathrm{O}_2$  for further separation. Our work provides an analytical solution for how the concentration develops over time and a methodology to find individual reaction terms for a given system geometry. With simple experimentation, the individual rate constants for anodic generation and bulk disproportionation of  $H<sub>2</sub>O<sub>2</sub>$  can be quantified. A rate constant for anodic oxidation can then be numerically fitted, but this value is best taken as an estimation of the anodic oxidation for a particular electrolyzer geometry. We found for our system, as well as two others in literature, that the  $H_2O_2$ decomposition due to anodic oxidation was always greater than the decomposition due to bulk disproportionation. As a result of describing anodic oxidation using a homogeneous concentration across the electrolyzer chamber, our analytical model predicted that changing the volume of electrolyte in the anode chamber would have no effect on the achieved concentration of  $\rm H_2O_2$ . However, this description was found to be unsuitable for a differing electrolyzer geometry, and the model should be refined with a more generalized expression that accounts for electrolyzer geometry and mass transfer in order to extend the model using surface concentrations. We recommend that the anolyte reservoir volume,  $V_R$ , be selected to meet the target production rate at a desired reaction time, but further work can be done to find the optimal balance between these parameters and the overall cost of the scaled-up system.

## **CRediT authorship contribution statement**

**Sohan A. Phadke:** Conceptualization, Methodology, Investigation, Formal analysis, Writing – original draft, Writing – review & editing. **Wiebren de Jong:** Conceptualization, Writing – review & editing, Supervision, Funding acquisition. **J.W. Haverkort:** Conceptualization, Writing – review & editing, Supervision, Funding acquisition.

## **Declaration of competing interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

### **Data availability**

Data will be made available on request.

## **Acknowledgments**

This project received funding from the NWO-AES Crossover program, Netherlands under project number 17621 (RELEASE). We would like to thank Dr. J. G. Buijnsters for his knowledge and supply of boron-doped diamond electrodes and Mr. Antonius Waskito W. for his assistance with experiments. We would also like to thank Pangotra et al. and Li et al. for making their data readily available.

#### **Appendix A. Low flow rate solution to Eq. ([7\)](#page-3-2)**

<span id="page-8-0"></span>Starting with Eq. ([7](#page-3-2)), we make the following substitutions:

$$
\frac{d^2c}{dt^2} + \alpha \frac{dc}{dt} + \beta c = \gamma
$$
\n(A.1)\n
$$
\alpha = \frac{\dot{Q}}{dt} + \frac{\dot{Q}}{dt} + \beta c = \gamma
$$

$$
\alpha = \frac{\omega}{V_E} + \frac{\omega}{V_R} + \frac{a}{V_E} + 2k_b ;
$$
\n
$$
\beta = \dot{Q} \left( \frac{k_a A}{V_E V_R} + \frac{k_b}{V_R} + \frac{k_b}{V_E} \right) + \frac{k_a A k_b}{V_E} + k_b^2 ; \quad \gamma = \frac{SA\dot{Q}}{V_E V_R}
$$
\nThis leads to the general solution,

\n
$$
c = C_1 \exp \left( -\lambda_1 t \right) + C_2 \exp \left( -\lambda_2 t \right) + \frac{\gamma}{\beta}
$$
\n(A.2)

where  $C_1$  and  $C_2$  are constants, and

$$
\lambda_1 = \frac{\alpha - \sqrt{\alpha^2 - 4\beta}}{2} \quad ; \quad \lambda_2 = \frac{\alpha + \sqrt{\alpha^2 - 4\beta}}{2}
$$

Using the initial conditions that  $c(t) = 0$  at  $t = 0$  and  $\frac{dc(t)}{dt} =$  $(SA)/V_R$  at  $t = 0$ , we arrive at the complete solution in Eq. ([A.3\)](#page-8-2).

$$
c = \left(\frac{SA\beta - \gamma\lambda_2 V_R}{\beta V_R \left(\lambda_2 - \lambda_1\right)}\right) \exp\left(-\lambda_1 t\right) - \left(\frac{SA\beta - \gamma\lambda_1 V_R}{\beta V_R \left(\lambda_2 - \lambda_1\right)}\right) \exp\left(-\lambda_2 t\right) + \frac{\gamma}{\beta}
$$
\n(A.3)

<span id="page-8-2"></span>At  $t$  approaches  $\infty$ , the steady state concentration reached can be expressed as Eq. [\(A.4](#page-8-3)),

<span id="page-8-3"></span>
$$
c_{\text{Steady State}} = \frac{\gamma}{\beta} = \frac{SA}{k_a A + k_b \left(V_E + V_R\right) + \frac{k_a A k_b V_R}{\dot{Q}} + \frac{k_b^2 V_E V_R}{\dot{Q}}}
$$
(A.4)

which simplifies to Eq. ([10\)](#page-3-5) for large *̇* .

### **Appendix B. High flow rate justification**

<span id="page-9-14"></span>In Section [2.4](#page-3-7), we use a simplification of Eq.  $(7)$  $(7)$  in the case of large  $\dot{Q}$ . Here, we fix the values of *S*, *A*,  $k_a$ ,  $k_b$ ,  $V_E$ , and  $V_R$  using the values for our setup at 200 mA  $\text{cm}^{-2}$ , and vary  $\dot{Q}$  in Eq. [\(A.3](#page-8-2)) to confirm that our assumption is valid. Using a base case of  $\dot{Q} = 0.1$  L min<sup>-1</sup>, as used in our experiments, we show the predicted effect of changing  $\dot{O}$  using Eq.  $(A.3)$  $(A.3)$  in [Fig.](#page-9-19) [B.1](#page-9-19). The curves for the fastest three flow rates  $(2 \dot{Q},$  $\dot{Q}$ , and 0.5  $\dot{Q}$ ) overlap, indicating that our flow rate of  $\dot{Q} = 0.1$  L min<sup>-1</sup> was sufficiently fast to use Eq. ([9\)](#page-3-4) in our analysis.



<span id="page-9-19"></span>Fig. B.1. Simulated results for changing flow rate,  $\dot{Q}$ , where the highest three flow rates (corresponding to 0.2, 0.1, and 0.05 L min-1) overlap, indicating the validity of the high flow rate assumption at 0.1 L min-1 .

#### **References**

- <span id="page-9-0"></span>[1] [P. Bajpai, Biermann's Handbook of Pulp and Paper: Raw Material and Pulp](http://refhub.elsevier.com/S0013-4686(24)00500-0/sb1) [Making, Joseph P. Hayton, Radarweg 29, PO Box 211, 1000 AE Amsterdam,](http://refhub.elsevier.com/S0013-4686(24)00500-0/sb1) [Netherlands, 2018.](http://refhub.elsevier.com/S0013-4686(24)00500-0/sb1)
- <span id="page-9-1"></span>[2] J. Ferdush, K. Nahar, T. Akter, M.J. Ferdoush, N. Jahan, S.M.F. Iqbal, Effect of hydrogen peroxide concentration on 100% cotton knit fabric bleaching, Eur. Sci. J. 15 (2019) 254–263, [http://dx.doi.org/10.19044/esj.2019.v15n33p254.](http://dx.doi.org/10.19044/esj.2019.v15n33p254)
- <span id="page-9-2"></span>[3] Q. Chen, Toward cleaner production of hydrogen peroxide in China, J. Clean. Prod. 14 (2006) 708–712, [http://dx.doi.org/10.1016/j.jclepro.2005.03.025.](http://dx.doi.org/10.1016/j.jclepro.2005.03.025)
- [4] Q. Chen, Development of an anthraquinone process for the production of hydrogen peroxide in a trickle bed reactor–from bench scale to industrial scale, Chem. Eng. Process.: Process Intensif. 47 (2008) 787–792, [http://dx.doi.org/10.](http://dx.doi.org/10.1016/j.cep.2006.12.012) [1016/j.cep.2006.12.012.](http://dx.doi.org/10.1016/j.cep.2006.12.012)
- <span id="page-9-3"></span>[5] A.T. Murray, S. Voskian, M. Schreier, T.A. Hatton, Y. Surendranath, Electrosynthesis of hydrogen peroxide by phase-transfer catalysis, Joule 3 (2019) 2942–2954, [http://dx.doi.org/10.1016/j.joule.2019.09.019.](http://dx.doi.org/10.1016/j.joule.2019.09.019)
- <span id="page-9-4"></span>[6] A.J. Shih, M.C.O. Monteiro, F. Datilla, D. Pavesi, M. Philips, A.H.M. da Silva, R.E. Vos, K. Ojha, S. Park, O. van der Heijden, G. Marcandalli, A. Goyal, M. Villalba, X. Chen, G.T.K.K. Gunasooriya, I. McCrum, R. Mom, N. López, M.T.M. Koper, Water electrolysis, Nature Rev. Methods Prim. 2 (2022) 1–19, [http://dx.doi.org/10.1038/s43586-022-00164-0.](http://dx.doi.org/10.1038/s43586-022-00164-0)
- <span id="page-9-5"></span>[7] C. Qu, D.-w. Liang, Novel electrochemical advanced oxidation processes with H2O<sup>2</sup> generation cathode for water treatment: A review, J. Environ. Chem. Eng. 10 (2022) 107896, <http://dx.doi.org/10.1016/j.jece.2022.107896>.
- <span id="page-9-6"></span>[8] V. Viswanathan, H.A. Hansen, J.K. Nørskov, Selective electrochemical generation of hydrogen peroxide from water oxidation, J. Phys. Chem. Lett. 6 (2015) 4224–4228, [http://dx.doi.org/10.1021/acs.jpclett.5b02178.](http://dx.doi.org/10.1021/acs.jpclett.5b02178)
- <span id="page-9-7"></span>[9] S. Mavrikis, S.C. Perry, P.K. Leung, L. Wang, C. Ponce de León, Recent advances in electrochemical water oxidation to produce hydrogen peroxide: A mechanistic perspective, ACS Sustain. Chem. Eng. 9 (2021) 76–91, [http://dx.doi.org/10.](http://dx.doi.org/10.1021/acssuschemeng.0c07263) [1021/acssuschemeng.0c07263.](http://dx.doi.org/10.1021/acssuschemeng.0c07263)
- [10] T.M. Gill, L. Vallez, X. Zheng, The role of bicarbonate-based electrolytes in  $H_2O_2$ production through two-electron water oxidation, ACS Energy Lett. 6 (2021) 2854–2862, <http://dx.doi.org/10.1021/acsenergylett.1c01264>.
- [11] S. Siahrostami, G.-L. Li, V. Viswanathan, J.K. Nørskov, One- or two-electron water oxidation, hydroxyl radical, or  $H_2O_2$  evolution, J. Phys. Chem. Lett. 8 (2017) 1157–1160, [http://dx.doi.org/10.1021/acs.jpclett.6b02924.](http://dx.doi.org/10.1021/acs.jpclett.6b02924)
- [12] X. Shi, S. Siahrostami, G.-L. Li, Y. Zhang, P. Chakthranont, F. Studt, T.F. Jaramillo, X. Zheng, J.K. Nørskov, Understanding activity trends in electrochemical water oxidation to form hydrogen peroxide, Nature Commun. 8 (2017) 1–12, [http://dx.doi.org/10.1038/s41467-017-00585-6.](http://dx.doi.org/10.1038/s41467-017-00585-6)
- <span id="page-9-8"></span>[13] A. Venugopal, L.H.T. Egberts, J. Meeprasert, E.A. Pidko, B. Dam, T. Burdyny, V. Sinha, W.A. Smith, Polymer modification of surface electronic properties of electrocatalysts, ACS Energy Lett. 7 (2022) 1586–1593, [http://dx.doi.org/10.](http://dx.doi.org/10.1021/acsenergylett.2c00199) [1021/acsenergylett.2c00199.](http://dx.doi.org/10.1021/acsenergylett.2c00199)
- <span id="page-9-9"></span>[14] K. Fuku, Y. Miyase, Y. Miseki, T. Gunji, K. Sayama, Enhanced oxidative hydrogen peroxide production on conducting glass anodes modified with metal oxides, Chem. Select 1 (2016) 5721–5726, <http://dx.doi.org/10.1002/slct.201601469>.
- [15] Y. Miyase, S. Iguchi, Y. Miseki, T. Gunji, K. Sayama, Electrochemical  $H_2O_2$ production and accumulation from  $H_2O$  by composite effect of  $Al_2O_3$  and BiVO4, J. Electrochem. Soc. 166 (2019) H644–H649, [http://dx.doi.org/10.1149/](http://dx.doi.org/10.1149/2.0561913jes) [2.0561913jes.](http://dx.doi.org/10.1149/2.0561913jes)
- <span id="page-9-10"></span>[16] T. Kang, B. Li, Q. Hao, W. Gao, F. Bin, K.N. Hui, D. Fu, B. Dou, Efficient hydrogen peroxide ( $H_2O_2$ ) synthesis by CaSnO<sub>3</sub> via two-electron water oxidation reaction, ACS Sustain. Chem. Eng. 8 (2020) 15005–15012, [http://dx.doi.org/10.](http://dx.doi.org/10.1021/acssuschemeng.0c05449) [1021/acssuschemeng.0c05449.](http://dx.doi.org/10.1021/acssuschemeng.0c05449)
- <span id="page-9-11"></span>[17] S. Mavrikis, M. Göltz, S.C. Perry, F. Bogdan, P.K. Leung, S. Rosiwal, L. Wang, C. Ponce de León, Effective hydrogen peroxide production from electrochemical water oxidation, ACS Energy Lett. 6 (2021) 2369–2377, [http://dx.doi.org/10.](http://dx.doi.org/10.1021/acsenergylett.1c00904) [1021/acsenergylett.1c00904.](http://dx.doi.org/10.1021/acsenergylett.1c00904)
- <span id="page-9-12"></span>[18] C. Xia, S. Back, S. Ringe, K. Jiang, F. Chen, X. Sun, S. Siahrostami, K. Chan, H. Wang, Confined local oxygen gas promotes electrochemical water oxidation to hydrogen peroxide, Nat. Catal. 3 (2020) 125–134, [http://dx.doi.org/10.1038/](http://dx.doi.org/10.1038/s41929-019-0402-8) [s41929-019-0402-8](http://dx.doi.org/10.1038/s41929-019-0402-8).
- <span id="page-9-13"></span>[19] D. Pickett, The analysis of a batch electrochemical reactor with continuously recirculating electrolyte, Electrochim. Acta 18 (1973) 835–837, [http://dx.doi.](http://dx.doi.org/10.1016/0013-4686(73)85035-2) [org/10.1016/0013-4686\(73\)85035-2.](http://dx.doi.org/10.1016/0013-4686(73)85035-2)
- <span id="page-9-15"></span>[20] T.M. Gill, X. Zheng, Comparing methods for quantifying electrochemically accumulated  $H_2O_2$ , Chem. Mater. 32 (2020) 6285-6294, [http://dx.doi.org/10.](http://dx.doi.org/10.1021/acs.chemmater.0c02010) [1021/acs.chemmater.0c02010.](http://dx.doi.org/10.1021/acs.chemmater.0c02010)
- <span id="page-9-16"></span>[21] [H.H.B. Lee, A.-H. Park, C. Oloman, Stability of hydrogen peroxide in sodium](http://refhub.elsevier.com/S0013-4686(24)00500-0/sb21) [carbonate solutions, Tappi J. 83 \(2000\) 1–9.](http://refhub.elsevier.com/S0013-4686(24)00500-0/sb21)
- <span id="page-9-17"></span>[22] L. Li, Z. Hu, Y. Kang, S. Cao, L. Xu, L. Yu, L. Zhang, J.C. Yu, Electrochemical generation of hydrogen peroxide from a zinc gallium oxide anode with dual active sites, Nature Commun. 14 (2023) 1–12, [http://dx.doi.org/10.1038/s41467-](http://dx.doi.org/10.1038/s41467-023-37007-9) [023-37007-9.](http://dx.doi.org/10.1038/s41467-023-37007-9)
- <span id="page-9-18"></span>[23] D. Pangotra, L.-I. Csepei, A. Roth, V. Sieber, L. Vieira, Anodic generation of hydrogen peroxide in continuous flow, Green Chem. 24 (2022) 7931–7940, <http://dx.doi.org/10.1039/d2gc02575b>.