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# Magnetic Field Prediction in Cubic Spoke-Type Permanent-Magnet Machine Considering Magnetic Saturation

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**Abstract**—In this article, a nonlinear semianalytical model (SAM) is presented to predict the magnetic field distribution (MFD) and electromagnetic performances (EPs) in the cubic spoke-type permanent magnet (PM) machine. To model the rectangular PMs, the rectangular PM is simplified as a combination of fan-shaped regions with different arc angles. Then, the MFD and EPs of the cubic spoke-type machines can be obtained by the harmonic modeling technique. Particularly, the saturation of the magnetic bridges is considered by the nonlinear iterative algorithm. The proposed nonlinear SAM is studied on a 12-slot/8-pole cubic PM prototype, and the nonlinear finite element model and experiment verify its correctness. The main contribution of this article is to present a general analytical modeling method for cubic spoke-type PM machines and consider the magnetic saturation of magnetic bridges.

**Index Terms**—Cubic spoke-type permanent magnet (PM) machine, harmonic modeling (HM), magnetic saturation, nonlinear.

## NOMENCLATURE

PM	Permanent magnet.
FE model	Finite-element model.
SD	Subdomain.
HM	Harmonic modeling.
SAM	Semianalytical model.
MFD	Magnetic field distribution.
CFS	Complex Fourier series.

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$A$	Magnetic vector potential.
$B$	Magnetic flux density.
$H$	Magnetic field strength.
$\mu$	Permeability.
$M$	Magnetization.
$J$	Current density.

## I. INTRODUCTION

AS a typical topology of the interior permanent magnet (PM) machine, the tangentially magnetized spoke-type PM machine has a good flux concentrated effect, compared with other types of PM machines, which provides better performance [1], [2], [3]. Therefore, spoke-type PM machines have extensive application prospects in industrial and household appliances [4], [5]. It is crucial to develop a rapid and precise magnetic field distribution (MFD) calculation approach for its design and optimization.

Finite element (FE) analysis has obvious advantages in precisely predicting the magnetic field of complex structure motors as it can take into account the influence of nonlinear ferromagnetic material [6], [7], [8]. Nevertheless, the optimization of the spoke-type PM machine necessitates numerous geometrical dimension iterations, which takes a lot of time [9]. The alternative strategy is analytical or hybrid analysis, which can rapidly evaluate the motor's magnetic field [10]. Numerous analytical models have been developed over the years [11], [12], [13], [14]. However, most of the analytical models cannot consider the nonlinear effect of iron parts, that is, the saturation is ignored, which leads to the overestimation of the magnetic field [15]. To take the effect of the magnetic saturation into consideration, Dubas and Boughra proposed an exact SD model that considers material nonlinearity by superimposing the components of the magnetic field solution in each subdomain of  $r$ - and  $\theta$ -directions (or  $x$ - and  $y$ -directions) [16], [17]. Besides, the local saturation effect can be further considered by dividing the iron part into elementary subdomains [18]. The harmonic modeling (HM) approach presented in [19] and [20] directly embeds the permeability of ferromagnetic materials into the magnetostatic field solution, in contrast to the analytical models developed in [16] and [17]. HM technology is further developed by Djelloul-Khedda et al., which is used to compute the performances of

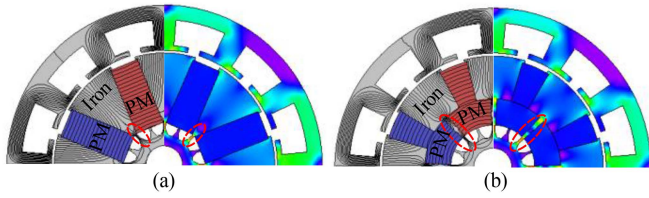


Fig. 1. Equivalent calculation method of a spoke-type PM machine. (a) Initial model. (b) Equivalent model.

the switched reluctance machine [21] and the iron-core loss of the flux-modulated PM machine [22]. Based on HM technology, Zhao et al. proposed a rapid optimization technique for coaxial magnetic gears that takes only around 80% as long to compute as the FE model takes [23]. Therefore, the nonlinear semianalytical model (SAM) based on HM technology is an effective approach to design and optimize the spoke-type PM machine.

The analytical modeling of spoke-type PM machines with regular forms in polar coordinates has attracted some academic attention, and it is relatively straightforward [13], [24], [25]. On the other hand, it is challenging to approximate cube spoke-type PMs as subdomains that are consistent in polar coordinates. To solve this problem, Meessen et al. [26] provided a reference solution for transforming an inconsistent domain into the consistent domain of the reference coordinate. On this basis, the rectangular PMs can be approximated by several fan-shaped subdomains [27], [28], [29], [30]. The rectangular PM is equivalent to two fan-shaped regions by Liang et al., and the exact SD model (the nonlinearity of ferromagnetic materials is ignored) is used to determine the MFD and electromagnetic performances of a spoke-type PM machine. However, as the majority of spoke-type PMs are designed with long depths and wide widths, it is not a generally accepted modeling technique to roughly transform a rectangular PM into two fan-shaped sections [28], [29], [30]. The MFD of the initial model and equivalent model of a spoke-type PM motor is evaluated using the FE model, as illustrated in Fig. 1, in accordance with the authors provided in [28], [29], and [30]. It is clear that the spoke-type PM motor's unique structure causes the magnetic flux leakage of the equivalent model to increase and the saturation of the rotor core to intensify. As a result, this method cannot be used to model the spoke-type PM motor analytically in general. On the other hand, because the traditional SD model disregards magnetic saturation, the magnetic flux density will be exaggerated. For analytical modeling, it is essential to determine the geometric parameters of each approximated fan-shaped region (such as the inner/outer radius, polar-arc angle, etc.) [27]. Therefore, it is necessary to propose a general modeling method for cubic spoke-type PM motors to quickly and accurately calculate their MFD and electromagnetic performances (EPs).

This article proposes an improved SAM for magnetic field prediction in cubic spoke-type PM motors based on HM technology to solve the aforementioned issues. The influence of local saturation of the magnetic bridge can be accurately taken into consideration by an iterative algorithm. The FE model and

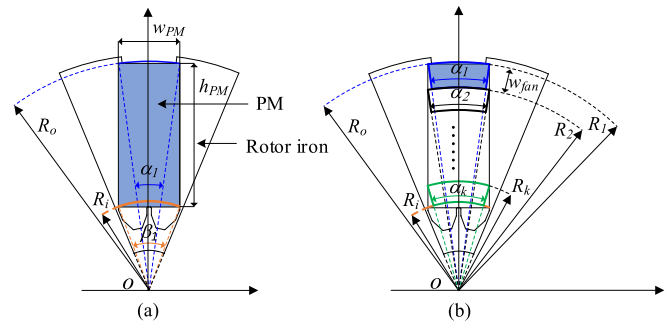


Fig. 2. Improved modeling method of rectangular PM. (a) Initial rectangular PM. (b) Equivalent fan-shaped region.

experiments are utilized to verify the validity of the proposed nonlinear SAM. The approach described in this article is applicable to all cubic spoke-type PM machines, has significant theoretical significance, and serves as an engineering reference for the design and optimization of such machines.

The rest of this article is organized as follows. The improved rectangular PM modeling approach and model simplification are introduced in Section II. Section III presents the spoke-type PM SAM in polar coordinates. In Section IV, the results of the proposed SAM are compared with those of the FE model. The prototype is then tested in Section V. Finally, Section VI concludes this article.

## II. MODEL SIMPLIFICATION

This section introduces the improved modeling approach for rectangular PM and simplifies the rotor and stator.

### A. Model of Rectangular PM

In polar coordinates, to satisfy partial differential equations and boundary conditions, the geometry of PM should be a regular region [27]. As a result, as shown in Fig. 2, the rectangular PM in this article is approximated by a superposition of fan-shaped regions with different pole-arc angles. The geometric parameters of each fan-shaped region can be determined by mathematical formulas as follows.

The width of each fan-shaped region  $w_{\text{fan}}$  is

$$w_{\text{fan}} = \frac{R_o - R_i}{K} \quad (1)$$

where  $K$  is the number of fan-shaped regions;  $R_o$  and  $R_i$  are the inner and outer radii of the rectangular PM, respectively.

The outer radius of the first fan-shaped region is  $R_1$  ( $R_1 = R_o$ ), and the  $k$ th outer radius is

$$R_o^k = R_1 - w_{\text{fan}}(k - 1). \quad (2)$$

Then, the polar-arc angle corresponding to each fan-shaped region can be calculated by

$$\alpha_k = 2 \cdot \arcsin \left( \frac{w_{\text{PM}}}{2 \cdot R_o^k} \right). \quad (3)$$





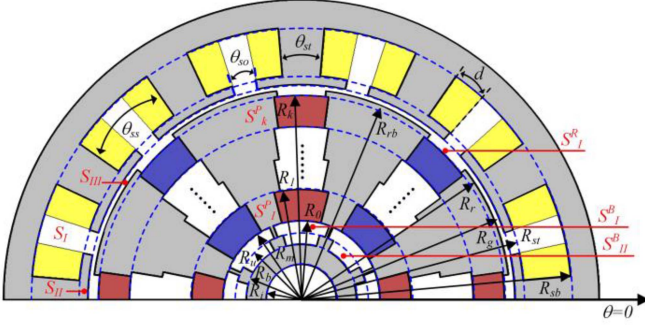


Fig. 5. 2-D analytical model.

The magnetic vector potential  $A_{SI}$  satisfies the following Poisson equation [21]:

$$\frac{\partial^2 A_{zI}^{SI}}{\partial r^2} + \frac{1}{r} \frac{\partial A_{zI}^{SI}}{\partial r} - \left( \frac{V_{SI}}{r} \right)^2 A_{zI}^{SI} = -\mu_{c,\theta}^{SI} J_z \quad (11)$$

where  $V_{SI} = [\mu_{c,\theta}^{SI} K_\theta (\mu_{c,r}^{SI})^{-1} K_\theta]^{1/2}$ .

The general solution of (11) is

$$A_{zI}^{SI}|_r = W_{SI} \left( \frac{r}{R_{sb}} \right)^{\lambda_{SI}} a_{SI} + W_{SI} \left( \frac{R_s}{r} \right)^{\lambda_{SI}} b_{SI} + r^2 F \quad (12)$$

where  $a_{SI}$  and  $b_{SI}$  are unknown coefficients.

The particular solution of (11) is  $r^2 F$ , and  $F$  is defined by

$$F = \left( [V_{SI}]^2 - 4I \right)^{-1} \mu_{c,\theta} J_z \quad (13)$$

where  $J_z$  is the complex Fourier series (CFS) coefficients of  $J$ , which can be obtained by

$$\hat{J}_{z,n} = \frac{1}{2\pi j n} \sum_{i=1}^{Q_s} \left[ J_{i,1} (e^{j n d} - 1) e^{-j n \frac{\theta_{ss}}{2}} + J_{i,2} (1 - e^{-j n d}) e^{j n \frac{\theta_{ss}}{2}} \right] e^{j n \alpha_i} \quad (14)$$

$$J_{i,1} = \frac{N_c}{S} C_1^T [i_A, i_B, i_C] \quad (15)$$

$$J_{i,2} = \frac{N_c}{S} C_2^T [i_A, i_B, i_C] \quad (16)$$

where  $N_c$  is the conductor number of slot coil,  $[i_A, i_B, i_C]$  are the armature currents,  $S$  is the surface of the stator slot coil,  $C_1^T$  and  $C_2^T$  are the transpose of the connecting matrix between the three-phase current and the stator slots, which represent the distribution of stator windings in the slots

$$J_z = [\hat{J}_{z,-N} \quad \cdots \quad \hat{J}_{z,N}]^T. \quad (17)$$

## B. PM Region

The magnetic vector potential in the PM region satisfies the following Poisson's equation [23]:

$$\begin{aligned} \frac{\partial^2 A_z^{SPk}}{\partial r^2} + \frac{1}{r} \frac{\partial A_z^{SPk}}{\partial r} - \left( \frac{V_{SPk}}{r} \right)^2 A_z^{SPk} \\ = -\frac{\mu_0}{r} (M_\theta^k + j K_\theta M_r^k) \end{aligned} \quad (18)$$

where  $M_r^k$  and  $M_\theta^k$  are the CFS coefficients of radial and tangential components of the magnetization vector  $M$

$$\hat{M}_{\theta,n}^k = \frac{2pB_{r,f}}{n\pi\mu_0} \sin\left(\frac{n\pi}{2p}\alpha_k\right) \quad (19)$$

$$\hat{M}_{r,n}^k = 0 \quad (20)$$

$$M_\theta^k = [\hat{M}_{r,-N}^k \quad \cdots \quad \hat{M}_{r,N}^k]^T. \quad (21)$$

The general solution of (18) is

$$A_z^{Pk}|_r = W_{Pk} \left( \frac{r}{R_k} \right)^{\lambda_{SI}} a_{Pk} + W_{Pk} \left( \frac{R_{k-1}}{r} \right)^{\lambda_{Pk}} b_{Pk} + rG. \quad (22)$$

The particular solution of (18) is  $rG$ , and  $G$  is defined by

$$G = \mu_0 (V_{Pk}^2 - I)^{-1} (M_\theta^k + j K_\theta M_r^k). \quad (23)$$

## C. Other Regions

The magnetic vector potential in the stator slot-opening region, air-gap region, rotor-slot opening region, and magnetic bridge region satisfies the following Laplace equation [20]:

$$\frac{\partial^2 A_z^{Sm}}{\partial r^2} + \frac{1}{r} \frac{\partial A_z^{Sm}}{\partial r} - \left( \frac{V_{Sm}}{r} \right)^2 A_z^{Sm} = 0. \quad (24)$$

The general solution of (24) is as follows, using the stator slot-opening region as an example

$$A_z^{SII}|_r = W_{SII} \left( \frac{r}{R_{st}} \right)^{\lambda_{SII}} a_{SII} + W_{SII} \left( \frac{R_g}{r} \right)^{\lambda_{SII}} b_{SII}. \quad (25)$$

In the air-gap region,  $\lambda_{SIII} = \sqrt{[K_\theta]^2} = |K_\theta|$ .

## D. Boundary Conditions

The interface continuity boundary conditions and Newman boundary conditions are collected in Table III based on the overall solutions of the aforementioned subdomains.

Finally, all boundary conditions are written in the following matrix form:

$$MX = Y \quad (26)$$

where  $M$ ,  $X$ , and  $Y$  represent the coefficient factors, the unknown coefficients, and the constant values in the boundary condition equations, respectively.

Then, the EPs (including cogging torque, back EMF, electromagnetic torque, etc.) can be further predicted [24]. The calculating formula is as follows:

The electromagnetic torque  $T_{em}$  can be computed by

$$T_{em} = \frac{L_{lef} R_g^2}{\mu_0} \int_0^{2\pi} B_r^{II}(R_g, \theta) B_\theta^{II}(R_g, \theta) d\theta. \quad (27)$$

The flux linkage of the  $i$ th stator slot coil can be computed by

$$\varphi_{1,i} = L_{lef} \frac{N_c}{S} \int_{\alpha_i - \frac{\theta_{ss}}{2}}^{\alpha_i + \frac{\theta_{ss}}{2} + d} \int_{R_{st}}^{R_{sb}} A_z^{IV}(r, \theta) dr d\theta \quad (28)$$

$$\varphi_{2,i} = L_{lef} \frac{N_c}{S} \int_{\alpha_i + \frac{\theta_{ss}}{2} - d}^{\alpha_i + \frac{\theta_{ss}}{2}} \int_{R_{st}}^{R_{sb}} A_z^{IV}(r, \theta) dr d\theta. \quad (29)$$

TABLE III  
BOUNDARY CONDITIONS

Description	Expressions
BCs between $S_I$ and $S_{II}$	$A_z^{S_I} \Big _{r=R_{st}} - A_z^{S_{II}} \Big _{r=R_{st}} = 0$
	$H_\theta^{S_I} \Big _{r=R_{st}} - H_\theta^{S_{II}} \Big _{r=R_{st}} = 0$
BCs between $S_{II}$ and $S_{III}$	$A_z^{S_{II}} \Big _{r=R_g} - A_z^{S_{III}} \Big _{r=R_g} = 0$
	$H_\theta^{S_{II}} \Big _{r=R_g} - H_\theta^{S_{III}} \Big _{r=R_g} = 0$
BCs between $S_{III}$ and $S_I^R$	$A_z^{S_{III}} \Big _{r=R_r} - A_z^{S_I^R} \Big _{r=R_r} = 0$
	$H_\theta^{S_{III}} \Big _{r=R_r} - H_\theta^{S_I^R} \Big _{r=R_r} = 0$
BCs between $S_I^R$ and $S_k^P$	$A_z^{S_I^R} \Big _{r=R_k} - A_z^{S_k^P} \Big _{r=R_k} = 0$
	$H_\theta^{S_I^R} \Big _{r=R_k} - H_\theta^{S_k^P} \Big _{r=R_k} = 0$
BCs between $S_k^P$ and $S_{k-1}^P$	$A_z^{S_k^P} \Big _{r=R_{k-1}} - A_z^{S_{k-1}^P} \Big _{r=R_{k-1}} = 0$
	$H_\theta^{S_k^P} \Big _{r=R_{k-1}} - H_\theta^{S_{k-1}^P} \Big _{r=R_{k-1}} = 0$
BCs between $S_k^P$ and $S_l^B$	$A_z^{S_k^P} \Big _{r=R_m} - A_z^{S_l^B} \Big _{r=R_m} = 0$
	$H_\theta^{S_k^P} \Big _{r=R_m} - H_\theta^{S_l^B} \Big _{r=R_m} = 0$
BCs between $S_l^B$ and $S_{II}^B$	$A_z^{S_l^B} \Big _{r=R_u} - A_z^{S_{II}^B} \Big _{r=R_u} = 0$
	$H_\theta^{S_l^B} \Big _{r=R_u} - H_\theta^{S_{II}^B} \Big _{r=R_u} = 0$
BCs at $r=R_{sb}$	$H_\theta^{S_I} \Big _{r=R_{sb}} = 0$
BCs at $r=R_b$	$H_\theta^{S_{II}^B} \Big _{r=R_b} = 0$

The total flux linkage for each phase can be obtained.

$$\begin{bmatrix} \Psi_a \\ \Psi_b \\ \Psi_c \end{bmatrix} = \begin{bmatrix} \Psi_{1,a} \\ \Psi_{1,b} \\ \Psi_{1,c} \end{bmatrix} + \begin{bmatrix} \Psi_{2,a} \\ \Psi_{2,b} \\ \Psi_{2,c} \end{bmatrix} \quad (30)$$

where

$$\begin{bmatrix} \Psi_{1,a} \\ \Psi_{1,b} \\ \Psi_{1,c} \end{bmatrix} = C_1 [\varphi_{1,1} \quad \varphi_{1,2} \quad \cdots \quad \varphi_{1,Q_s}]^T \quad (31)$$

$$\begin{bmatrix} \Psi_{2,a} \\ \Psi_{2,b} \\ \Psi_{2,c} \end{bmatrix} = C_2 [\varphi_{2,1} \quad \varphi_{2,2} \quad \cdots \quad \varphi_{2,Q_s}]^T. \quad (32)$$

Then, the back EMF for each phase can be derived as

$$\begin{bmatrix} E_a \\ E_b \\ E_c \end{bmatrix} = -\frac{d}{dt} \begin{bmatrix} \Psi_a \\ \Psi_b \\ \Psi_c \end{bmatrix}. \quad (33)$$

For phase A, the machine is fed only by phase A with  $i_a$ , and the self- and mutual inductances can be calculated as follows:

$$\begin{bmatrix} L_a \\ M_{ab} \\ M_{ac} \end{bmatrix} = [\Psi_a \quad \Psi_b \quad \Psi_c]^T / i_a. \quad (34)$$

### E. Nonlinear Solution Algorithm

As illustrated in Fig. 6, each part of the iron can be separated into  $C_T$  blocks along the  $\theta$ -direction and  $L$  layers along the

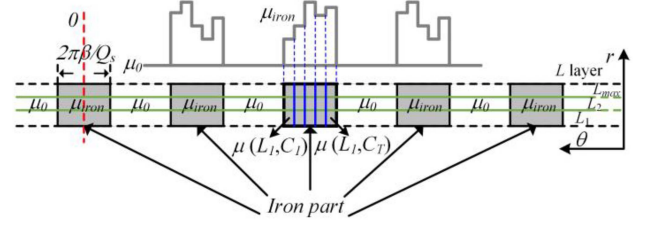


Fig. 6. Multilayer division of iron part.

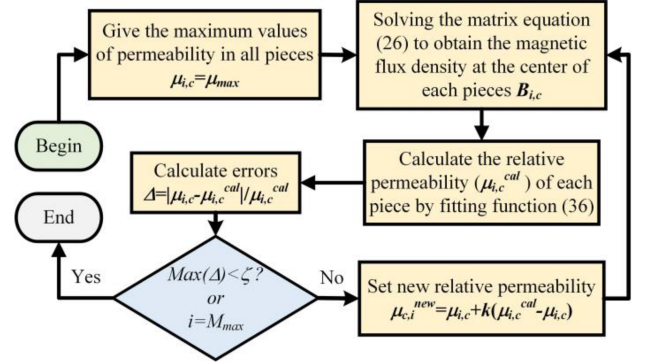


Fig. 7. Nonlinear iterative algorithm.

$r$ -direction. The Fourier coefficients of the  $l$ th layer of the stator slots/teeth region can be obtained by

$$\hat{\mu}_n^l = \begin{cases} (1 - \beta) \mu_0 + \frac{\beta}{Q_s C_T} \sum_{i=1}^{Q_s} \sum_{c=1}^{C_T} \mu_{i,c} & n = 0 \\ \sum_{i=1}^{Q_s} \frac{\mu_0}{2\pi j n} e^{jn\pi \frac{2(i-1)-\beta}{Q_s}} \left[ 1 - e^{jn\pi \frac{2(\beta-1)}{Q_s}} \right] & n \neq 0 \\ + \sum_{i=1}^{Q_s} \sum_{c=1}^{C_T} \frac{\mu_{i,c}}{2\pi j n} e^{\frac{\beta C_T - 2(i-1) C_T - 2\beta c}{Q_s C_T}} \left[ e^{jn\pi \frac{2\beta}{Q_s C_T}} - 1 \right] & n \neq 0 \end{cases} \quad (35)$$

where  $\mu_{i,c}$  is the permeability in the  $c$ th piece of the  $i$ th iron part.

The Fourier coefficients  $\hat{\mu}_n^{l,rec}$  can be obtained by replacing  $(\mu_0, \mu_{i,c})$  by  $(1/\mu_0, 1/\mu_{i,c})$  in (35).

$K$  in Fig. 7 is the correction factor ( $0 < k < 1$ ), and the empirical value is generally 0.2–0.3 [23]. The algorithm shown in Fig. 7 is utilized to estimate the saturation level in the soft-magnetic material through an iterative process. On the other hand, although the calculation accuracy can be improved by dividing the iron parts into more layers, it sacrifices the calculation time. In the Spoke-type PM motor studied in this article, the magnetic saturation of the rotor magnetic bridge is the most obvious. The effect of magnetic bridge saturation is considered by the iterative algorithm. When the error requirement  $\Delta$  is met or the maximum number of iterations  $M_{max}$  is reached, the calculation is completed.

The relative permeability can be obtained by the fitting equation [32]

$$\mu_r(B) = \left( \frac{B_o}{H_o \mu_0} \right) \left( \frac{1}{1 + (B/B_o)^v} \right) \quad (36)$$

where  $B_o$ ,  $H_o$ , and  $v$  are the constants.

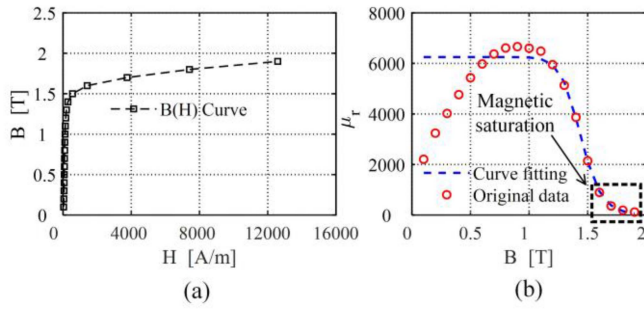


Fig. 8. Magnetic characteristic of 50CS470. (a)  $B$ - $H$ . (b)  $\mu_r$ - $B$ .

TABLE IV  
MAIN PARAMETERS OF THE STUDIED MACHINE

Items	Symbol	Value
Number of slots	$Q_s$	12
Number of pole pairs	$p$	4
Rated current	$I$	10 A
Number of turns	$N_c$	14
Active length	$L_{lef}$	14 mm
Remanence of PM	$B_r$	0.47 T

The ferromagnetic material adopted in this prototype is 50CS470, and its  $B$ - $H$  curve and  $B$ - $\mu_r$  curve are given in Fig. 8. The parameters  $B_o$ ,  $H_o$ , and  $v$  are 1.44, 133.3, and 17.42, respectively.

#### IV. FINITE ELEMENT MODEL VERIFICATION

To demonstrate the impact of the approximated fan-shaped PM fraction on the accuracy of the 2-D SAM, four cases are defined in this section. With one fan-shaped region in the first case, two in the second, three in the third, and four in the fourth, the rectangular PM is approximated by these cases, respectively. The FE model is established in the FE software JMAG, and the main parameters of the studied motor are listed in Table IV. Fig. 9(a) and (b) shows the MFD under no-load and load conditions, respectively. Matrix (26) is solved in MATLAB to obtain the MFD and EPs. In each case, the MFD and electromagnetic parameters obtained by the analytical model are compared with the FE model.

##### A. Comparison of Magnetic Field Distribution

In Figs. 10 and 11, the comparison of the air gap flux density components between the FE model and the proposed nonlinear SAM is given. The waveforms and harmonic spectrums show that the analytical results are closer to the FE model as the number of fan-shaped approximation PM pieces increases. When the number of approximated PM pieces is four, the above two calculation methods are very consistent.

Additionally, as shown in Fig. 12, the air gap flux density components under load conditions are compared when the phase current is 10 A. It is apparent that when the number of approximated blocks of PMs increases, the computation accuracy improves as well.

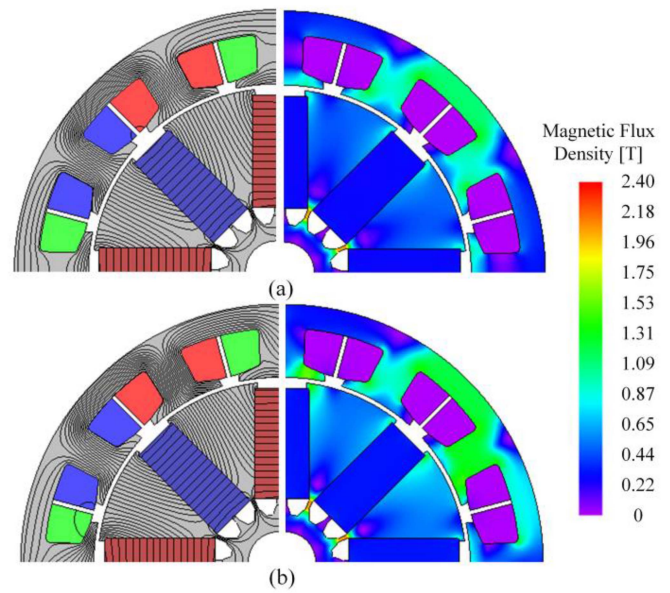


Fig. 9. FE models. (a) No-load condition. (b) On-load condition.

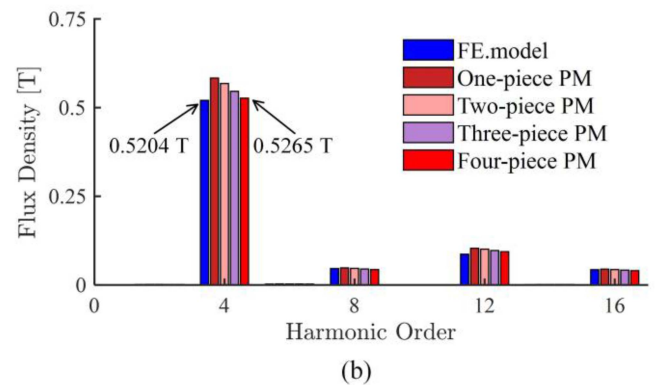
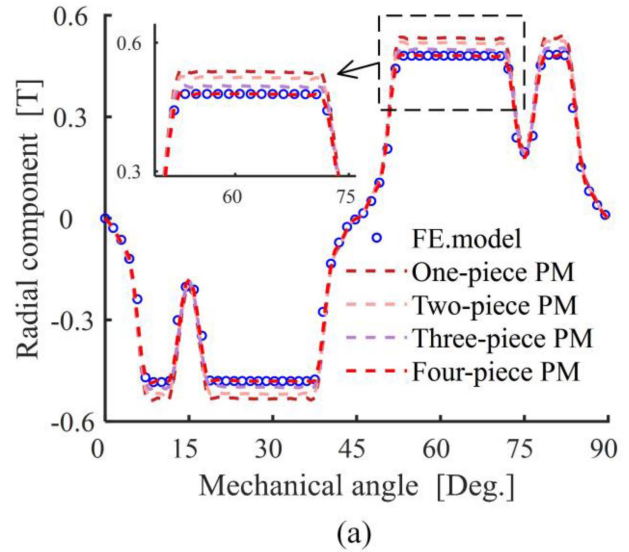


Fig. 10. Comparison of radial components of no-load flux density in the air gap. (a) Waveforms. (b) Harmonic spectrum.



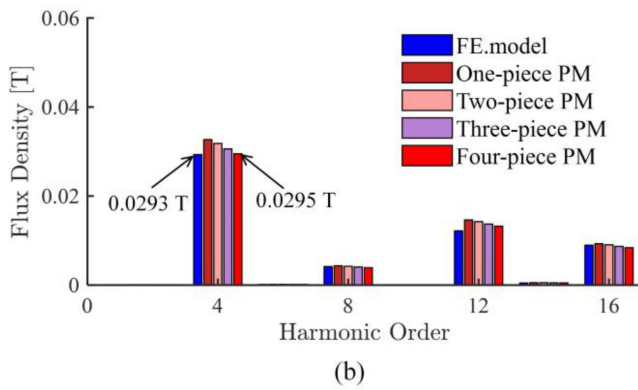
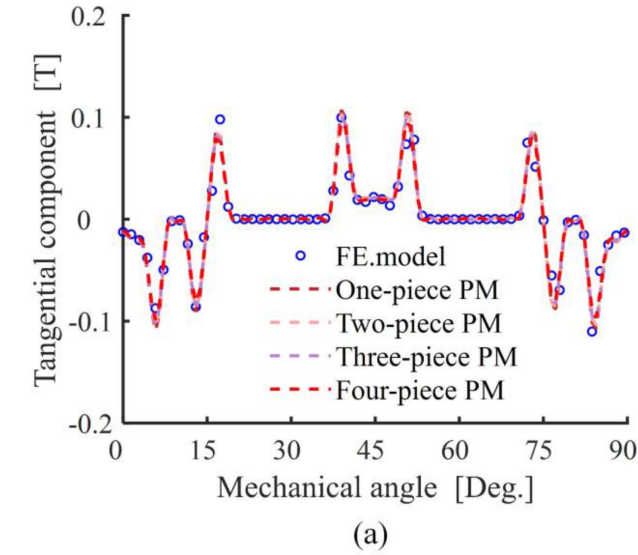


Fig. 11. Comparison of tangential components of no-load flux density in the air gap. (a) Waveforms. (b) Harmonic spectrum.

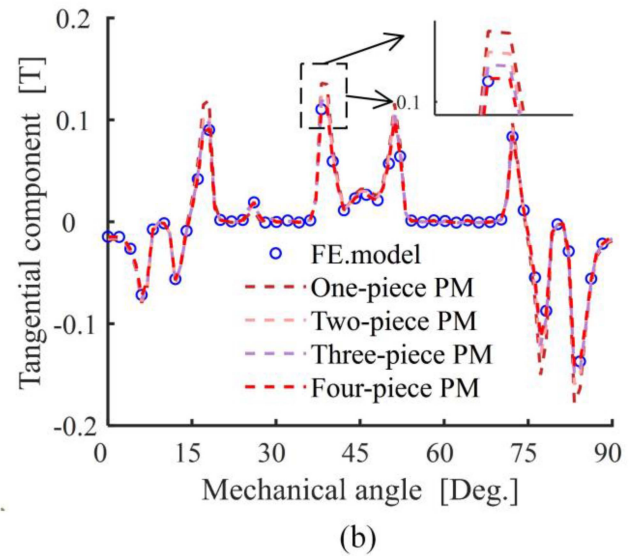
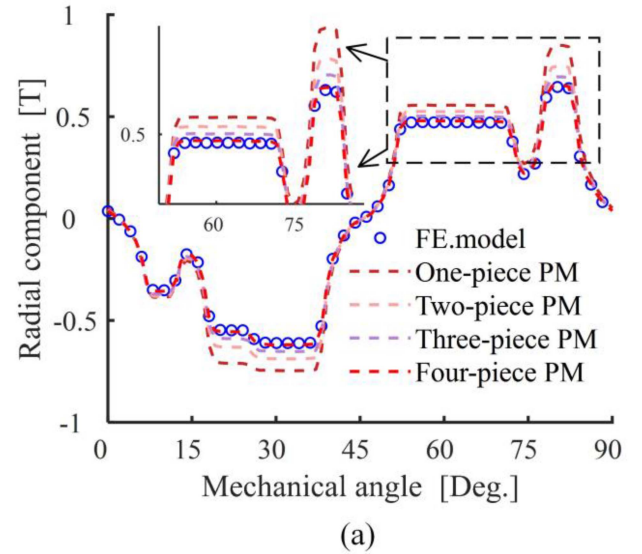


Fig. 12. Comparison of on-load air gap flux density components. (a) Radial component. (b) Tangential component.

### B. Comparison of Electromagnetic Performances

Figs. 13 and 14 compare the no-load EPs, namely cogging torque and back EMF. Even though there are calculation errors in the first to third cases, these errors get smaller as there are more approximations of PM regions. In the fourth case, the EPs predicted by the SAM are basically consistent with the FE model calculation results.

In particular, the self- and mutual inductances of phase A are calculated. Fig. 15 shows the comparison between the analytical model (four-piece PM) and the FE model for the variation of self- and mutual inductances with rotor position. Both results obtained from the SAM are in very good agreement with those obtained by the FE model. The maximum and minimal values of the self-inductance are, respectively,  $L_{a,\max} = 0.1813$  mH and  $L_{a,\min} = 0.1536$  mH for the SAM and  $L_{a,\max} = 0.1799$  mH and  $L_{a,\min} = 0.1545$  mH for the FE model.

Furthermore, the electromagnetic torque for each case is evaluated at rated current  $I = 10$  A, as illustrated in Fig. 16. It is clear that they have the same variation trends. To visual interpretation of the calculation accuracy, Table V lists the

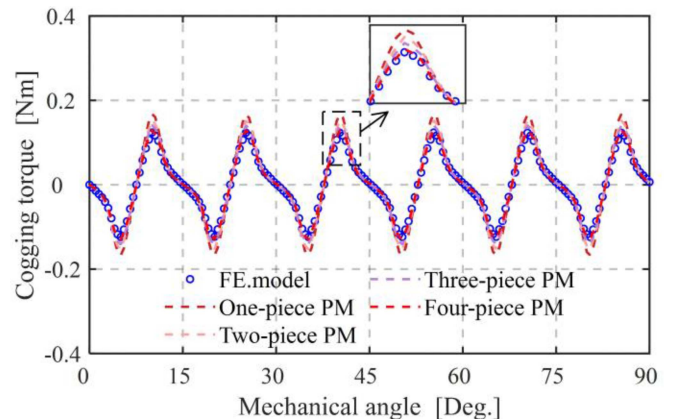


Fig. 13. Comparison of cogging torque.

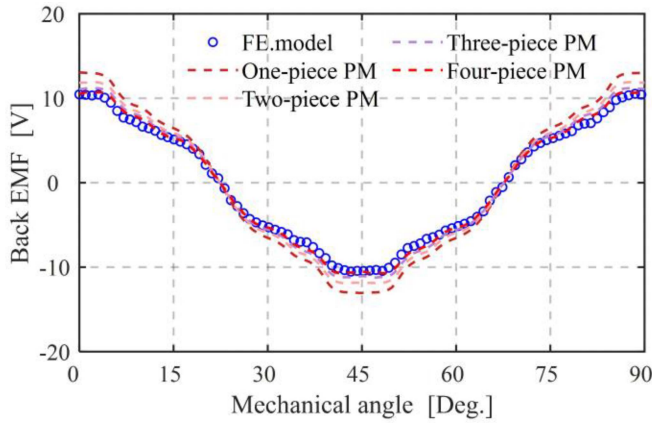


Fig. 14. Comparison of back EMFs at 3000 r/min.

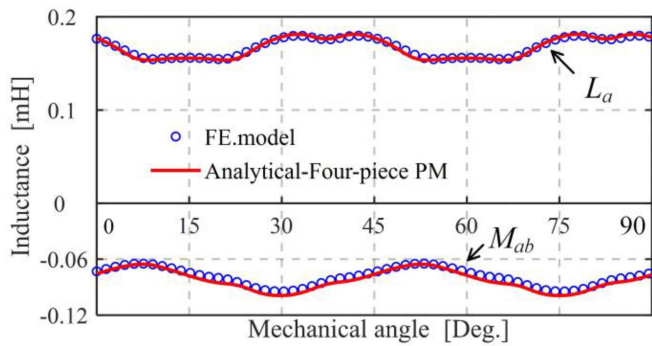
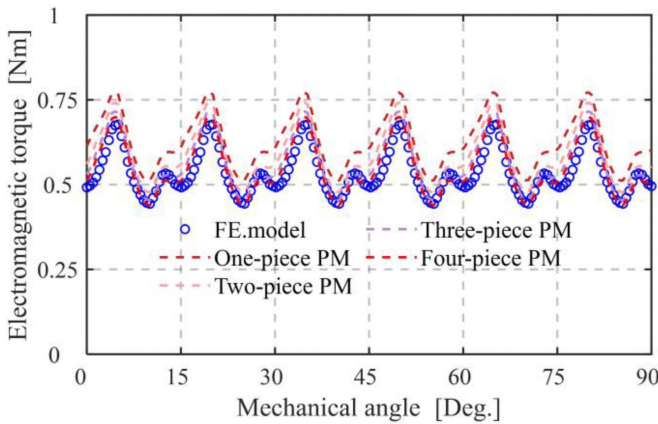
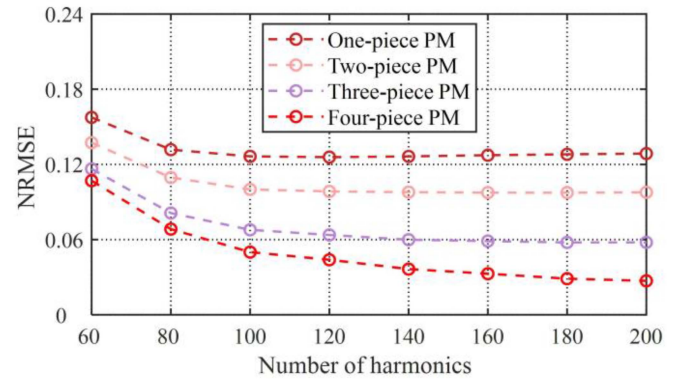
Fig. 15. Comparison of self/mutual inductance ( $L_a$  and  $M_{ab}$ ).

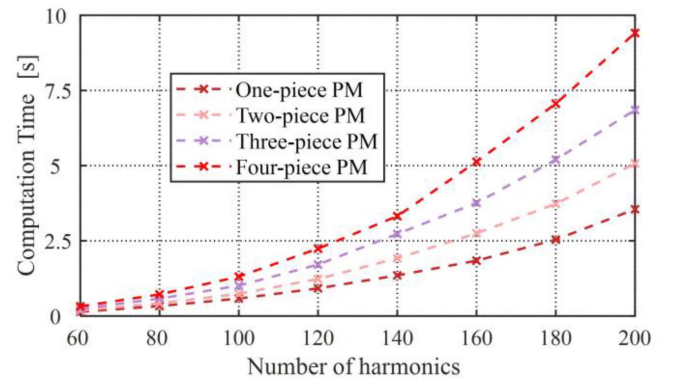
Fig. 16. Comparison of electromagnetic torque.

TABLE V  
COMPARISON OF ELECTROMAGNETIC TORQUE

Items	FE model	1-piece	2-piece	3-piece	4-piece
Average $T_{em}$	0.536Nm	0.628Nm	0.590Nm	0.565Nm	0.548Nm
Relative error	-	17.16%	10.07%	5.41%	2.23%



(a)



(b)

Fig. 17. Influence of the number of harmonics on (a) NRMSE of the radial magnetic flux density in the air-gap and (b) computation time.

average torque and relative error of the above calculation cases. As the number of approximate PMs increases, the calculation error of average electromagnetic torque decreases gradually. In particular, when the fan-shaped PMs are four, the relative error of the average electromagnetic torque is only 2.23%, and an acceptable agreement has been achieved.

### C. Computation Time

The number of calculation regions affects the computation time of the analytical model proposed in this article, but the selection of harmonic numbers also has a significant impact. The normalized root mean square of error (NRMSE) of the no-load magnetic density in each case is calculated as follows to visually illustrate the calculation accuracy

$$\text{NRMSE} = \sqrt{\frac{\sum_i^{N_{pc}} [B_{Ana}(i) - B_{FEM}(i)]^2}{\sum_i^{N_{pc}} B_{FEM}(i)^2}} \quad (37)$$

where  $B_{Ana}(i)$  and  $B_{FEM}(i)$  are values of the  $i$ th estimation of magnetic flux density, respectively, by SAM and FE model;  $N_{pc}$  is the number of test data.

In Fig. 17, the NRMSE of the radial magnetic flux density in the air-gap and calculation time of the SAM is shown as a function of the number of harmonics. All calculations are



TABLE VI  
COMPUTATION TIME COMPARISONS OF DIFFERENT CASES

	1-piece	2-piece	3-piece	4-piece
Linear SAM/s	1.16	1.60	2.14	2.86
Nonlinear SAM/s	8.59	14.31	18.77	24.52
Nonlinear FE model/s	30.58			

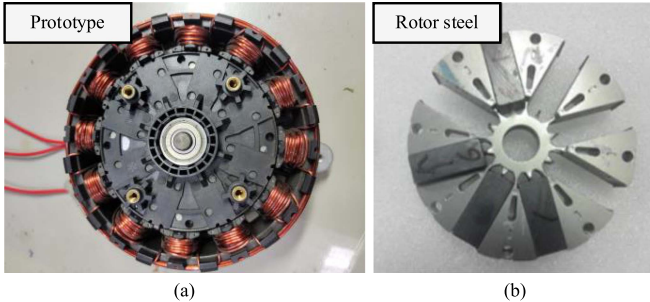


Fig. 18. Structure of the prototype. (a) Prototype. (b) Rotor steel.

performed at the center of air-gap for  $N_{pc} = 500$  different points along the circumference. It can be seen from Fig. 17(a) that the NRMSE of each case already starts to converge around  $N = 120$ . To make a compromise between calculating efficiency and accuracy, the maximum harmonic order  $N$  for computation in this article is set to 130. Both analytical models and FE models are run on a PC with Intel (R) Core (TM) i7-7700k CPU @ 4.20 GHz and 16 GB main memory under the WIN10 operating environment. The computation time of SAM (linear and nonlinear) and nonlinear FE model for single-step MFD is listed in Table VI. It can be seen that as the number of approximate PMs increases, the computational time of the SAM also increases. This is because for each additional calculation region,  $2 \times (2 \times N + 1)$  unknown coefficients are added. In addition, the computational time of the nonlinear SAM is several times that of the linear SAM. This is because the nonlinear SAM uses the iterative algorithm proposed in Section III to consider the nonlinearity of ferromagnetic materials, which is equivalent to several repetitions of the linear SAM. In the fourth case, a proper compromise between calculation time and accuracy is achieved. The calculation time of the nonlinear SAM is 80% of the nonlinear FE model, while the linear SAM is only 10%. The computational time of the nonlinear SAM depends on the convergence error  $\Delta$  and the maximum number of iterations  $M_{max}$ . Thanks to the efficient computational efficiency of the linear SAM model, it has important application prospects in the design and optimization of PM motors.

## V. EXPERIMENTAL VERIFICATION

In this section, the phase inductance, back EMF, and output torque experiments of a 12-slot/8-pole cubic spoke-type PM machine are carried out to verify the effectiveness of the nonlinear SAM proposed in this article. The structure of the prototype is shown in Fig. 18.

To verify the correctness of the proposed method, the phase inductance of different rotor positions is measured by LCR

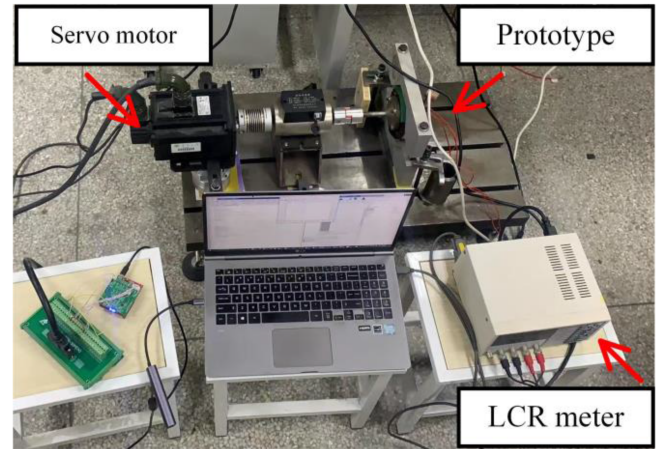


Fig. 19. Inductance measurement setup.

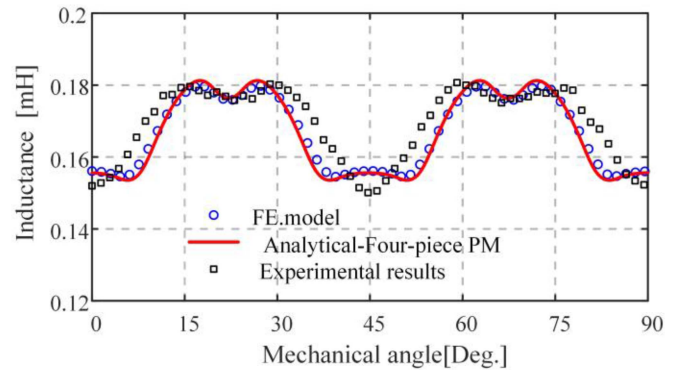


Fig. 20. Comparison of phase inductance.

meter, and the measurement setup is shown in Fig. 19. Fig. 20 shows the comparison between the measured and calculated phase inductances at different rotor positions. It can be found that the experimental waveform is slightly different from the analytical and FE results because the rotor structure is simplified in the analytical model and the FE model [i.e., the effect of the weight reduction hole is ignored, as can be seen in Fig. 18(b)]. The maximum values of the phase inductance  $L_{max}$  of the experiment and SAM are 0.1817 mH and 0.1813 mH, respectively; the minimum values of experimental and SAM are 0.1498 mH and 0.1536 mH, respectively, and the relative error is 2.54%.

To test the no-load back EMF of the prototype, the prototype is driven by a servo motor. Fig. 21 illustrates the experimental setup and devices. The servo motor is set to speed control mode and runs at 1200 r/min. The experimental results of back EMFs are shown in Fig. 22. As can be seen, the experimental results and the four-piece approximation model match well. The experimental result has an RMS value of 2.96 V, while the proposed nonlinear SAM computes a value of 3.04 V, and the relative error is only 2.7%. The predicted waveform shape by nonlinear SAM and the experimental waveform, however, differ slightly. It is primarily due to the analytical model neglecting the rotor chamfer's influence.

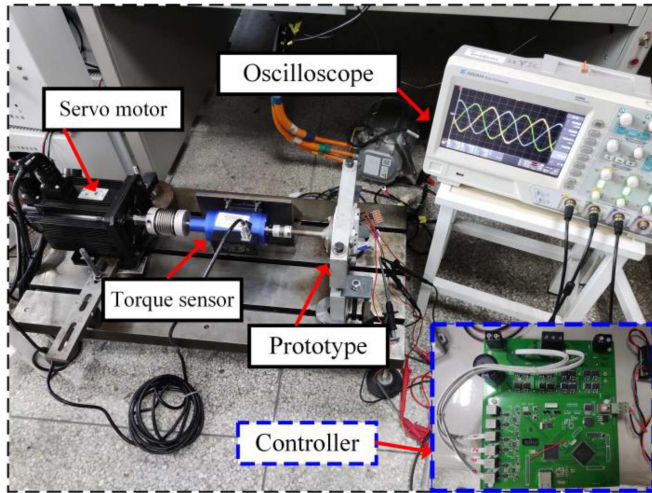
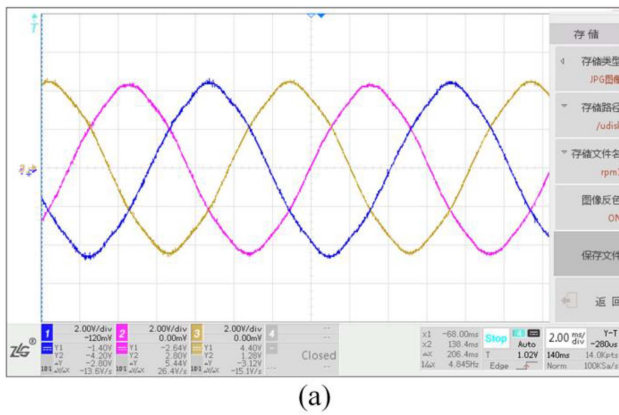
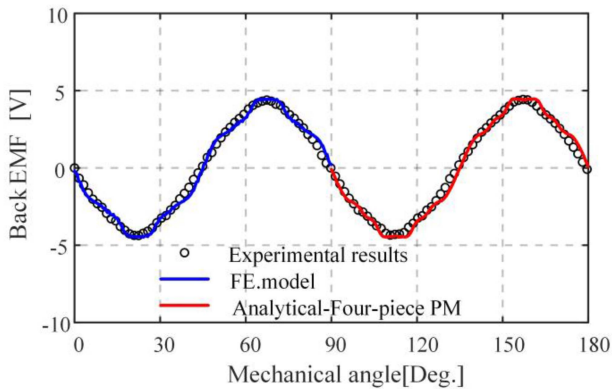


Fig. 21. Experimental setup.



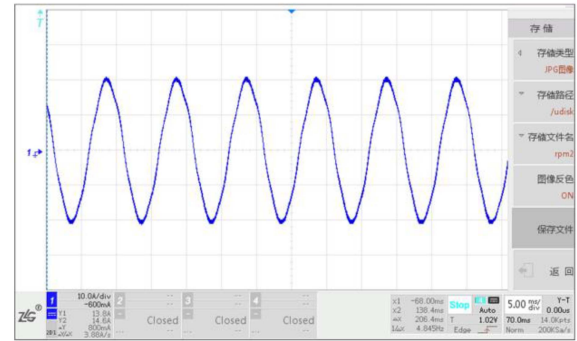
(a)



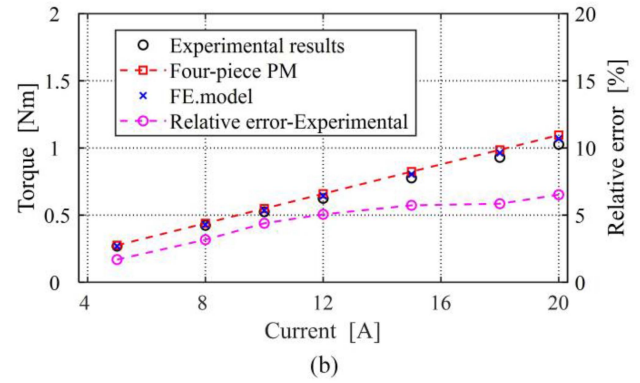
(b)

Fig. 22. Experimental result of back EMFs. (a) Experimental results. (b) Comparison of back EMF of phase A.

The output torque of the prototype is then tested. The prototype is controlled by position sensorless field-oriented control (FOC), and the servo motor runs as a generator. The output torque is measured with a high-precision torque sensor. The output torque was tested at 1500 r/min, and the amplitude of the phase current varied from 5 to 20 A. The current waveform at a phase current amplitude of 20 A is presented in Fig. 23(a), while the current in the analytical model and the FE model is



(a)



(b)

Fig. 23. Output torque. (a) 20 A phase current waveform. (b) Current versus torque curve.

TABLE VII  
CURRENT AND TORQUE DATA AT 1500 R/MIN

Current /A	5	8	10	12	15	18	20
Test /Nm	0.269	0.424	0.525	0.625	0.777	0.93	1.027
FE model /Nm	0.269	0.429	0.536	0.643	0.804	0.963	1.07
SAM /Nm	0.274	0.437	0.548	0.657	0.822	0.984	1.094

a completely sinusoidal current, which also causes errors in the output torque results. Fig. 23(b) shows the current versus torque curve. Table VII provides the specific information for the current and output torque at 1500 r/min. It can be seen that when the current is lower than 12 A, the relative error is less than 5%; on the other hand, as the current increases, the degree of magnetic saturation deepens. The relative error rises to 6.7% at 20 A (200% of the rated current), which is still within an acceptable range.

In addition, the capability in the transient of the proposed method is also given. The dynamic characteristic of the studied motor is tested and compared with the analytical and FE model results, the torque–speed characteristic is shown in Fig. 24. The motor runs under double overload condition at 100–600 r/min; then runs at the rated load condition. When the motor speed exceeds 1600 r/min, the line voltage of the motor is close to the bus voltage of the power supply, the motor runs at 1600–2400 r/min in the state of flux-weakening. It can be seen that the proposed method can obtain the dynamic characteristics of the motor in the full speed range, and the analytical results are in good agreement with the FE model results and experimental results.



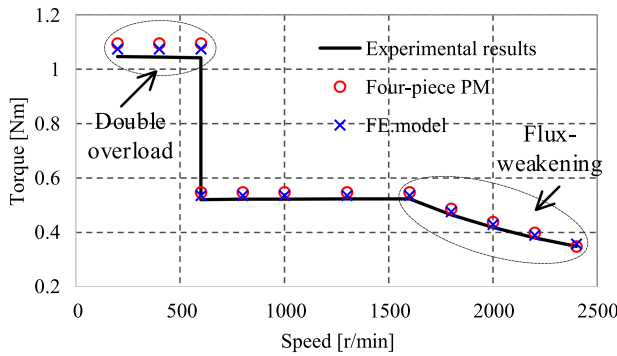


Fig. 24. Torque-speed characteristic of the studied motor.

## VI. CONCLUSION

This article proposed an improved 2-D analytical modeling approach for cubic spoke-type PM machines based on dividing the inconsistent rectangular region into multiple consistent fan-shaped subregions in polar coordinates. To find the appropriate combination of fan-shaped PM fractions and the number of harmonics under the constraints of computation efficiency and accuracy, four cases were investigated. The four fan-shaped PM segments are an appropriate tradeoff between time and accuracy, and the nonlinear SAM can save 20% of the calculation time compared to the nonlinear FE model, while the linear SAM is faster. Furthermore, the approach presented in this research can be extended to V-type or U-type interior PM motors to provide an efficient computing tool to speed up their design and optimization.

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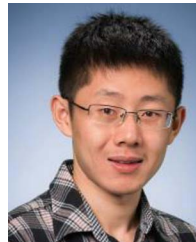
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