

Delta debugging fault-triggering propositional model counting instances To facilitate debugging of unweighted model counters using SharpVelvet

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Abstract

 Propositional model counting (#SAT) is the counting variant of the Boolean Satisfiability (SAT)
 problem. Development of #SAT solvers has seen a boom in recent years. These tools are complex and hard to debug. To address this, we propose a delta debugger that reduces fault-triggering un-

- 7 weighted model counting instances. Our delta de-
- 8 bugger shows an improvement compared to state of
- ⁹ the art in the related field of SAT solvers.

10 1 Introduction

The first three paragraphs of this section are based on Latour's
 project description [2024].

The aim of Propositional Model Counting [Gomes et al., 13 14 2021] is to find the *number* of unique solutions ("models") that satisfy a certain Boolean formula. This is the counting 15 version of the Boolean Satisfiability (SAT) [Biere et al., 2021] 16 NP-complete problem, which aims to answer whether there is 17 at least one solution. Therefore, the problem of model count-18 ing (#SAT) is conjectured to be computationally harder than 19 NP. 20

There are numerous applications of model counting and its variants, three notable examples include: reliability estimation of power grid networks [Duenas-Osorio *et al.*, 2017], optimisation problems in bioinformatics and social sciences [Latour *et al.*, 2022] and verification of neural networks [Baluta *et al.*, 2019].

SharpVelvet [Latour and Soos, 2024] is an ongoing 27 project that aims to provide model counter developers with 28 a fuzzer and a delta debugger. The purpose of the fuzzer is to 29 generate and run problem instances, in order to trigger bugs 30 in a model counter. Once a bug is found, the delta debugger 31 minimises the fault-triggering instance as much as possible, 32 whilst still triggering the bug. As such, the model counter de-33 34 velopers are more likely to locate the incorrect piece of code.

35 Since model counters have seen a boom only in the last few years, there are not many, if any, other fuzzing tools 36 freely available to their developers. Modern model coun-37 ters are complex and hard to debug, also witnessed by a re-38 cently proposed delta debugger for unweighted model coun-39 ters, TestMC [Usman et al., 2020]. We believe we can im-40 prove upon Usman et al. by implementing state of the art in 41 general delta debugging [Wang et al., 2021]. 42

This leads to the research question we answer in this paper: "Given an unweighted model counting instance that triggers a bug in a solver, and means of interacting with that solver, how much can we minimise the instance in such a way that it still triggers a bug, using heuristics based on the CNF structure and properties of individual clauses?".

In Section 2 we provide relevant definitions. Section 3
 presents state of the art in delta debugging and related work.
 Then, in section 4 we introduce the DeltaMC framework. We
 describe our experimental setup in section 5 and analyse the
 results in section 6. We describe how we conducted responsible research in section 7 and conclude in section 8.

2 Preliminaries

This section introduces relevant concepts.

Input format

In boolean logic, a proposition in *Conjunctive Normal Form* (CNF) is defined as a conjunction (\land) of one or more clauses. A clause is a disjunction (\lor) of literals. Lastly, a literal consists of a variable or its negation. Two examples of propositions in CNF are (p) \land (q) and ($p \lor q \lor r$) \land ($o \lor (\neg z)$).

Within general delta debugging, the logical proposition in CNF corresponds to the input ("instance") and a clause corresponds to an input element. For the scope of this work the literals within a clause are kept unchanged by our delta debugger.

Delta debugging

Delta debugging is defined as minimising a fault-triggering input, such that the resulting reduced instance still triggers a fault in the software that is being debugged. We measure the *performance* of a delta debugger in terms of achieved reduction (in %) of the input size (n) and the ratio between the number of *delta-debugging tests* performed and n. A deltadebugging test consists of running the software with an intermediate reduced instance to check whether the bug is reproduced, and a pass is achieved if so.

Model counting flavours

There exist four variations of the model counting problem, *i.e.* unweighted, weighted, projected and projected weighted model counting [Gomes *et al.*, 2021]. In the scope of this paper we focus solely on unweighted model counting. These type of counters accept a proposition in CNF as input, similar to SAT solvers.

3 Background and Related Work

This section presents general delta-debugging techniques, related work in the field of SAT solvers and one proposed delta debugger for model counters.

3.1 General delta-debugging techniques

This section presents the four delta-debugging algorithms we found in the literature.

Leave-one-out

The *naïve* delta-debugging algorithm [Vu *et al.*, 2023] iteratively tries to remove an element from the instance. The average-case asymptotic number of tests performed is bound by $O(n^2)$.

Delta Debugging

Zeller and Hildebrandt introduced the concept of delta de-98 bugging and proposed dd-min [2002], based on the classic 99 algorithm of *binary search*. Initially, tests are performed for 100 instances containing half of the input. If successful, the algo-101 rithm discards the other half. Otherwise, it continues with the 102 original instance. Afterwards, quarters of the instance are re-103 moved and the resulting subsequences are tested. In the same 104 way, the reduction continues until individual elements are re-105 moved, similar to the leave-one-out strategy. The authors 106 bound the worst-case asymptotic number of tests performed 107 by dd-min by $O(n^2)$. 108

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Algorithm 1: The prob-dd algorithm.

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Input: Set S containing the elements of the initial
         instance.
  Output: Set Q containing the elements of the reduced
           instance.
1 n \leftarrow |S|;
2 p[1 \dots n] \leftarrow \sigma; // Initial probabilities.
3 repeat
      // Next delta-debugging test.
      D \leftarrow \text{SelectTest}(p);
4
      // True if fault still present.
      R \leftarrow \text{RunTest}(D);
5
      // Update probabilistic model.
     p \leftarrow \text{UpdateModel}(R, p);
7 until ReductionComplete (p);
s Q \leftarrow \text{ReducedInput}(p);
\mathfrak{s} return Q
```

109 Probabilistic Delta Debugging

Wang et al. recently introduced the **prob-dd** algorithm that employs a *probabilistic model* to guide the reduction of the input. The description of the algorithm is based on the original paper [2021].

A minimal version of the original algorithm can be seen 114 in Algorithm 1. The input S is assumed to be pre-processed, 115 possibly using domain-specific knowledge, such that all sta-116 tistical dependencies between elements are eliminated. Sub-117 sequently, the model assigns each input element a Bernoulli 118 random variable, representing whether the element is in-119 cluded in the final, reduced instance Q. Together with the 120 previous assumption, it immediately follows that these vari-121 ables are mutually independent. All the variables are assigned 122 an initially identical value of σ . 123

Moving on to the delta-debugging part, prob-dd forms a 124 subset D of the last fault-triggering instance, initially S, ac-125 cording to the probabilities p. As explained earlier, a higher 126 probability implies a greater chance of an element belong-127 ing to the set Q. Afterwards, the delta-debugging test is per-128 formed and the model is updated to reflect whether D pro-129 duced a bug. Finally, the reduction concludes when all prob-130 abilities are either 0 or 1. Wang et al. bound the worst-case 131 asymptotic number of tests conducted by prob-dd by O(n). 132 For an in-depth explanation of the prob-dd algorithm, we 133 point the reader to the original article. 134

135 Similarity-Based Isolation

Vu et al. introduced similarity-iso [2023], improving ddmin and dd [Zeller and Hildebrandt, 2002] on localizing the
fault-triggering elements by using a domain-specific distance
metric to group such elements. The algorithm is bound by
the underlying performance of dd-min. We refer the reader
to the full article for more details.

142 **3.2 Delta Debuggers for SAT solvers**

Based on the literature study we conducted, state of the art
in SAT delta debuggers is considered to be the adaptation of
dd-min [Zeller and Hildebrandt, 2002] introduced by Brummayer et al. [2010]. The authors improve the performance

of the original dd-min algorithm by incorporating domainspecific knowledge. We refer the reader to the original paper for technical details.

3.3 Delta Debuggers for Model Counters

The **TestMC** framework [Usman *et al.*, 2020] is the only implementation of a delta debugger, developed specifically for model counters, that we were able to find during our literature study. The proposed delta debugger is based on the ddmin algorithm and achieved a 30% reduction of the input. At the time of submission of this paper the **TestMC** source code is not publicly available. 157

4 Methodology

This section describes the scope of this research, our proposed delta-debugging framework, and the two delta debuggers we applied to unweighted model counting.

4.1 Scope

Given the duration of this project, we implemented a delta 163 debugger solely for unweighted model counters. The pro-164 jected, weighted and projected weighted model counting 165 problems are more complex and therefore a non-trivial delta 166 debugger implementation for these types of model counters 167 would require considerably more effort. Out of the four 168 delta-debugging techniques, we chose to implement prob-169 dd [Wang et al., 2021]. In addition, we apply cnfdd [Brum-170 mayer et al., 2010] to unweighted model counting. The 171 naïve method of leave-one-out [Vu et al., 2023] cannot 172 achieve better performance than dd-min [Zeller and Hilde-173 brandt, 2002], which is implemented by cnfdd. In addition, 174 considering that similarity-iso [Vu et al., 2023] is built on top 175 of dd-min, we decided to apply prob-dd in order to experi-176 ment with a different delta-debugging approach. 177

4.2 DeltaMC framework

We present DeltaMC, an optional extension of SharpVelvet [Latour and Soos, 2024] that enables support for delta debugging model counters.

DeltaMC can be used to debug any type of model counter, *i.e.* unweighted, weighted, projected or projected weighted, if provided with a corresponding delta debugger implementation.

The high-level design can be seen in Algorithm 2. Ini-186 tially, the delta debugger is instantiated for an instance that 187 produced a bug in the debugged model counter. Afterwards, 188 preprocessing of the CNF formula takes place, during which 189 free and fixed variables are removed and equivalent adjacent 190 clauses are merged. Subsequently, the main loop will run un-191 til the delta debugger is unable to minimise the instance fur-192 ther. Within one iteration, a delta-debugging test is selected, 193 then SharpVelvet is employed to fuzz the model counter and 194 lastly the result of the test, *i.e.* pass if fault produced, is passed 195 onto the delta debugger. Finally, the resulting reduced in-196 stance is printed, and as such it can be further manually re-197 viewed and reported to the model counter developers. 198

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Algorithm 2. The DeltaMC framework

Algorithm 2. The Denamo namework.						
Input: Delta debugger DD, fault-triggering input						
<i>instance</i> , debugged solver <i>buggy_mc</i> .						
Output: Reduced instance in CNF.						
1 Function DeltaDebug (<i>instance</i> , <i>buggy_mc</i>)						
begin						
/* Initialise delta debugger with						
the preprocessed instance. */						
$_{2}$ preprocesssed_ins \leftarrow Preprocess						
(instance);						
<pre>3 DD.Initialise (preprocessed_ins);</pre>						
4 while !DD.Finished () do						
/* Select the next						
delta-debugging test. */						
$s test_ins \leftarrow DD.SelectTest();$						
/* Check whether fault is						
triggered. */						
$6 \qquad bug_present \leftarrow \texttt{Fuzz} (buggy_mc, test_ins);$						
<pre>// Process result of test.</pre>						
<pre>7 DD.Update (bug_present);</pre>						
8 end						
/* Print the reduced CNF						
instance. */						
<pre>9 DD.PrintReducedInstance();</pre>						
10 end						

4.3 Prob-dd application 199

Wang et al. assume statistical independence between the in-200 put elements when defining the probabilistic model [2021]. 201 In the context of model counting, some degree of dependence 202 is still present in the preprocessed input. This is caused by 203 propositional variables that occur in more than one clause. 204 Therefore this assumption does not hold, since an instance 205 where each variable belongs to at most one clause can easily 206 be solved by modern model counters. In spite of that, we be-207 lieve that in practice prob-dd will have a good performance, 208 since clauses in the preprocessed input are fairly distinct, re-209 sulting in a low degree of statistical dependence. 210

The authors assume no prior knowledge of the input ele-211 ments. In the original paper, Wang et al. state that the choice 212 of σ does not considerably influence the number of tests per-213 formed, neither the input size reduction. In the scope of this 214 work, we integrate prior knowledge of the input elements in 215 order to improve the performance of prob-dd. Our hypothe-216 sis is that setting higher initial probabilities for the more com-217 plex clauses and lower values for the simpler clauses, could 218 reduce the amount of delta-debugging tests and possibly im-219 prove the input reduction. 220

4.4 Prob-dd Heuristics 221

We now present the three heuristics we used for setting the 222 initial probabilities of the model: 223

Heuristic 1 (H1) 224

We assign each variable an initial probability of 0.1. Wang et 225 al. set the initial probability based on the expected reduction 226 ratio [2021]. 227

Heuristic 2 (H2)

We use the ratio between the number of literals present in the clause and the total number of literals in the proposition as 230 initial probability. 231

Heuristic 3 (H3)

We compute a score for each clause based on the rarity of its 233 literals, *i.e.* how often they appear in the entire proposition. 234 We believe that a literal that appears more frequently results 235 in stronger clauses, *i.e.* harder to solve by the model counters 236 and more likely to trigger bugs. 237

We define the frequency F of a literal p as the number of its 238 occurrences in the proposition L. As can be seen in equation 239 1, the score S of a clause c is calculated as the sum of frequen-240 cies of its literals, divided by the total sum of frequencies. 241

$$S_c = \frac{\sum\limits_{p \in c} F_p}{\sum\limits_{p \in L} F_p} \tag{1}$$

Probabilities scaling

Running prob-dd with the raw scores of H2 and H3 resulted 243 in unexpected behaviour, since the values are often below 0.01. Such values rendered the model unable to select the 245 next delta-debugging test. To address this, we further scale 246 the initial probabilities to [0.1, 0.4]. 247

4.5 Cnfdd application

We obtained the latest version [Artho et al., 2013] of 249 cnfdd¹ [Brummayer et al., 2010]. Since SAT CNF instances 250 are similar to unweighted model counting CNF instances, the 251 only change needed in the source code was printing c t mc252 at the top of the delta debugger output file. This comment 253 line signalled to model counters to treat the instance as un-254 weighted. 255

Experimental Setup 5

This section presents the experimental setup used for the 257 DeltaMC framework, our implementation of prob-dd, the 258 cnfdd setup, our assumptions about faults, the hardware 259 setup, the solvers and generators used. 260

5.1 Research Questions

Through the experiments we aim to answer the following two 262 research questions: 263

Q1: How do the **prob-dd** heuristics perform when applied to 264 unweighted model counting? 265

Q2: How do prob-dd and cnfdd compare in terms of perfor-266 mance? 267

5.2 DeltaMC setup

The framework is implemented in Python 3.11, using 269 Cython $3.0.11^2$ to integrate C++ implementations of delta 270 debuggers. The choice of programming languages followed 271 naturally, given that SharpVelvet [Latour and Soos, 2024] is 272

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¹Source code available at https://fmv.jku.at/

cnfuzzdd/cnfuzzdd2013.zip

²https://cython.org/

implemented in Python while our implementation of prob-273

dd is in C++. In addition, we built the framework decoupled 274

from the actual delta debugger implementation to facilitate 275

future research in this field. 276

5.3 Prob-dd implementation 277

Our prob-dd implementation is exclusively based on the al-278 gorithm described in the original paper [Wang et al., 2021]. 279 The implementation is in C++20, and we reused parts of the 280 GPMC solver [Suzuki et al., 2017] source code³. 281

We chose to build our delta debugger on top of an exist-282 ing model counter since it enabled us to implement solely the 283 prob-dd logic. As such, our implementation makes use of 284 the existing functionality for parsing, printing, preprocessing 285 and storing in-memory CNF instances. 286

5.4 Cnfdd setup 287

Since adapting the implementation to follow the pro-288 posed API was outside the scope of this work, we 289 wrapped cnfdd with a short Python script containing the 290 DeltaMC fuzzing logic. 291

5.5 Solvers 292

We used the binaries [Fichte et al., 2024] submitted to the 293 2024 edition of the Model Counting Competition [Fichte 294 The unweighted track, with exact preet al., 2021]. 295 cision, had ten participants, out of which we selected 296 Ganak [Sharma et al., 2019], D4 [Lagniez and Marquis, 297 2017] and GPMC [Suzuki et al., 2017], corresponding to 298 the first, fourth and eighth positions of the leader-board re-299 spectively. By applying our delta debugger to state-of-the-300 art solvers with different underlying implementations, we 301 302 demonstrate its relevance and future potential to assist devel-303 opment of model counters.

5.6 Fault definition 304

305 We consider three types of faults, namely wrong counts, crashes and timeouts. 306

Wrong count 307

The model count of a solver is considered wrong if the ma-308 jority of the other surveyed solvers agree on a different result. 309

Crash 310

A crash is defined as an abnormal early exit of a solver, with-311 out providing any result. 312

Timeout 313

We expect solvers to finish counting within a limit of 10 sec-314 onds for an easy instance. An instance is considered easy 315 if any of the three model counters is able successfully solve 316 it within the time limit. This limit was chosen to facilitate 317 experimenting with the delta debugger, considering the time 318 frame of this project. 319

5.7 CNF generators

SharpVelvet provides adaptations of the CNFuzz and 321 FuzzSAT generators [Brummayer et al., 2010]. We gen-322 erated 100.000 CNF instances, 70.000 using CNFuzz, and 323 30.000 using FuzzSAT. We used the default configuration of 324 CNFuzz, since the resulting instances were of varying hard-325 ness and size. For FuzzSAT we used three configurations, in 326 order to vary the size and structure of the generated instances. 327

5.8 Hardware

We acknowledge the use of computational resources of the 329 DelftBlue supercomputer [Centre (DHPC), 2025]. We ran 330 experiments on nodes equipped with Intel Xeon E5-6248R 331 CPUs, running at 3.0 GHz. The operating system of the clus-332 ter is Red Hat Enterprise Linux 8.1. Each solver was allocated 333 64 GB of RAM and one core, since the underlying implemen-334 tations do not make use of parallelisation. 335

Results 6

This section presents the fuzzing results and delta-debugging 337 performance achieved. 338

6.1 Triggered faults

Model counting software has improved considerably in re-340 cent years. In addition, it is highly likely these tools were 341 fuzzed and debugged using the CNFuzz and FuzzSAT gen-342 erators [Brummayer et al., 2010]. As a consequence, we were 343 not able to trigger any wrong count or crash bugs. We fuzzed 344 solvers with 100.000 CNF instances, which exhibited a con-345 siderable amount of variety in structure and hardness. While 346 we consider our sample size relevant, finding bugs is an un-347 certain process. 348

In an ideal scenario, the performance of a delta debugger 349 is measured by reducing fault-triggering instances. Consid-350 ering we were not able to produce any bugs, we tested our 351 delta debugger implementation by reducing inputs that trig-352 gered timeouts. This experiment showcases the ability of the 353 delta debugger to narrow the *hardness* of the instance, *i.e.* the 354 subset of clauses which take the longest to solve. We believe 355 this performance would further translate well to reducing in-356 stances that trigger wrong count or crash bugs. Out of the 357 100.000 CNF instances we fuzzed solvers with, a small pro-358 portion triggered timeouts, from which we randomly selected 359 30 CNF instances and delta debugged. 360

6.2 Delta-debugging performance

Table 1 presents the average input reduction performance and 362 Table 2 presents the average ratio between the number of 363 delta-debugging tests performed and input size. 364 365

We now answer our research questions:

Q1: Heuristics performance. While all of the three heuris-366 tics achieve a high reduction of the input, on average H2 per-367 forms better by a small margin, followed by H3. Similarly, 368 H2 conducts the least amount of delta-debugging tests, while 369 H1 requires the most tests. Thus, we show that, in the context 370 of unweighted model counting, prior knowledge of the in-371 put successfully improves the performance of the probabilis-372 tic model by a small yet non-insignificant margin. 373

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³Source code available at https://git.trs.css.i. nagoya-u.ac.jp/k-hasimt/GPMC

Solver	H1	H2	H3	cnfdd
Ganak	84.69	91.46	90.13	89.43
D4	84.06	89.44	87.28	90.41
GPMC	82.89	86.10	84.18	86.52

Table 1: Average input reduction (%) achieved by the three probdd heuristics and cnfdd.

Solver	H1	H2	H3	cnfdd
Ganak	0.44	0.33	0.37	3.26
D4	0.49	0.36	0.42	3.59
GPMC	0.50	0.40	0.47	3.18

Table 2: Average ratio between number of tests and input size, *i.e.* efficiency of the three prob-dd heuristics and cnfdd (lower is better).

Q2: Comparison with cnfdd [Brummayer *et al.*, 2010]. H2 reduces the input approximatively as much as **cnfdd**, while H1 and H3 achieve a slightly weaker reduction. All the heuristics perform considerably less tests compared to **cnfdd**, with H2 performing $\sim 10 \times$ less tests. In practice, this translates to a significantly shorter runtime of the delta debugger. This improvement is explained by the efficiency of **prob-dd**.

7 Responsible Research

This section presents ethical considerations of this work, how scientific integrity was observed while conducting research, and finally the transparency and reproducibility aspects.

385 7.1 Ethical considerations

The resulting tool, DeltaMC, could at most be used for de-386 387 bugging model counting software. This software is already freely and publicly available. To our knowledge there has 388 389 been no malicious use of such solvers at the time of submitting this article. While we consider malignant use unlikely to 390 happen in the future, model counting does have practical ap-391 plications. Considering the example of verifying neural net-392 works [Baluta et al., 2019], one could ask about the ethical 393 implications or intended uses of the verified neural network 394 itself. Therefore, we consider this project does not introduce 395 new ethical concerns. 396

397 7.2 Scientific integrity

All the source code and binaries were obtained and used according to their respective open-source licenses. No use of AI tools was made at any point of this research.

401 7.3 Transparency and Reproducibility

All our research artifacts are available open source and we provide instructions on how to use our delta debugger in the repository.

In order to abide by the terms of the various licenses governing the source code and binaries we made use of, our artifacts are published in two separate repositories.

The DeltaMC code, prob-dd implementation and the CNF instances used are available under MIT license at: https://github.com/davidcoroian/ cse3000-deltamc, commit hash 8d9377f. The adapted cnfdd source code and wrapper script are 412 published under GPLv3 license at: https://github. 413 com/davidcoroian/cse3000-cnfdd, commit hash 414 93dd8d7. 415

8 Conclusions and Future Work

This paper focused on delta debugging unweighted model 417 counters. First, we proposed the DeltaMC framework, an op-418 tional extension of SharpVelvet [Latour and Soos, 2024] that 419 can be coupled with a delta debugger implementation to de-420 bug a model counter. Then, we implemented a delta debugger 421 based on the state-of-the-art technique of probabilistic delta 422 debugging [Wang et al., 2021]. Finally, our empirical evalua-423 tion of the performance of our delta debugger demonstrates a 424 $\sim 10 \times$ improvement in terms of number of delta-debugging 425 tests performed compared to state of the art in the related field 426 of SAT solvers. 427

While our findings are promising, during this research we
were unable to produce wrong count or crash bugs and we
benchmarked our delta debugger by reducing timeouts. We
believe the delta debugger would achieve a good performance
when minimising wrong count or crash bugs, but this remains
to be tested in future experiments.428
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Future work in this field includes implementing delta 434 debuggers for weighted, projected and projected weighted 435 model counters. In addition, it could be worth experimenting with other recently proposed delta-debugging techniques 437 such as similarity-iso [Vu *et al.*, 2023].

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